

# BEE 4750 Homework 3: Dissolved Oxygen and Monte Carlo

Due Date

Thursday, 10/03/23, 9:00pm

## Overview

### Instructions

- Problem 1 asks you to implement a model for dissolved oxygen in a river with multiple waste releases and use this to develop a strategy to ensure regulatory compliance.
- Problem 2 asks you to use Monte Carlo simulation to assess how well your strategy from Problem 1 performs under uncertainty.
- Problem 3 (5750 only) asks you to identify where a third discharge should be placed to maintain regulatory compliance.

### Load Environment

The following code loads the environment and makes sure all needed packages are installed. This should be at the start of most Julia scripts.

```
import Pkg
Pkg.activate(@__DIR__)
Pkg.instantiate()
```

```
using Random
using Plots
using LaTeXStrings
using Distributions
```

## Problems (Total: 50/60 Points)

### Problem 1 (30 points)

A river which flows at 6 km/d is receiving waste discharges from two sources which are 15 km apart. The oxygen reaeration rate is  $0.55 \text{ day}^{-1}$ , and the decay rates of CBOD and NBOD are 0.35 and  $0.25 \text{ day}^{-1}$ , respectively. The river's saturated dissolved oxygen concentration is 10 mg/L.

If the characteristics of the river inflow and waste discharges are given in Table 1, write a Julia model to compute the dissolved oxygen concentration from the first wastewater discharge to an arbitrary distance  $d$  km downstream. Use your model to compute the maximum dissolved oxygen concentration up to 50 km downstream and how far downriver this maximum occurs.

Table 1: River inflow and waste stream characteristics for Problem 1.

Parameter	River Inflow	Waste Stream 1	Waste Stream 2
Inflow	100,000 m <sup>3</sup> /d	10,000 m <sup>3</sup> /d	15,000 m <sup>3</sup> /d
DO Concentration	7.5 mg/L	5 mg/L	5 mg/L
CBOD	5 mg/L	50 mg/L	45 mg/L
NBOD	5 mg/L	35 mg/L	35 mg/L

#### In this problem:

- Plot the dissolved oxygen concentration from the first waste stream to 50 km downriver. What is the minimum value in mg/L?
- What is the minimum level of treatment (% removal of organic waste) for waste stream 1 that will ensure that the dissolved oxygen concentration never drops below 4 mg/L, assuming that waste stream 2 remains untreated? How about if only waste stream 2 is treated?
- Suppose you are responsible for designing a waste treatment plan for discharges into the river, with a regulatory mandate to keep the dissolved oxygen concentration above 4 mg/L. Discuss whether you'd opt to treat waste stream 2 alone or both waste streams equally. What other information might you need to make a conclusion, if any?

### Problem 2 (20 points)

A coastal community has a 3.0 m tall levee (relative to present-day mean sea level). From analyzing tide gauge records, you determine that the annual maximum water levels (in m) follow a [Generalized Extreme Value distribution](#) with parameters  $\text{GEV}(1.5, 0.2, 0.1)$ . The target levee reliability standard is a 1% probability of overtopping (extreme water levels exceeding the levee height).

**In this problem:**

- Use Monte Carlo simulation to estimate the present-day reliability of the levee along with a 95% confidence interval for the reliability estimate. Does it comply with the reliability standard? How many samples did you need to determine that?
- Over the lifetime of the levee, mean local sea levels are anticipated to rise by 0.3m with a standard deviation of 0.2m. How does this impact the future reliability of the levee? Discuss how the sea-level uncertainty impacts the uncertainty of your Monte Carlo estimate.

**Problem 3 (10 points)**

**This problem is only required for students in BEE 5750.**

A factory is planning a third wastewater discharge into the river downstream of the second plant. This discharge would consist of  $5 \text{ m}^3/\text{day}$  of wastewater with a dissolved oxygen content of 4.5 mg/L and CBOD and NBOD levels of 50 and 45 mg/L, respectively.

**In this problem:**

- Assume that the treatment plan you identified in Problem 1 is still in place for the existing discharges. If the third discharge will not be treated, under the original inflow conditions (7.5 mg/L DO), how far downstream from the second discharge does this third discharge need to be placed to keep the river concentration from dropping below 4 mg/L?

**References**

List any external references consulted, including classmates.