Name:	

MASTERY QUIZ DAY 20

Math 237 – Linear Algebra

Version 2

Fall 2017

Show all work and justify all of your answers. Answers without work or sufficient reasoning will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

S3. Let
$$W = \text{span} \left\{ \begin{bmatrix} 2\\0\\2\\1 \end{bmatrix}, \begin{bmatrix} 3\\1\\-1\\1 \end{bmatrix}, \begin{bmatrix} 0\\2\\-8\\-1 \end{bmatrix} \right\}$$
. Find a basis for this vector space.

Solution:

$$RREF \begin{pmatrix} \begin{bmatrix} 2 & 3 & 0 \\ 0 & 1 & 2 \\ 2 & -1 & -8 \\ 1 & 1 & -1 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} 1 & 0 & -3 \\ 0 & 1 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Thus
$$\left\{ \begin{bmatrix} 2\\0\\2\\1 \end{bmatrix}, \begin{bmatrix} 3\\1\\-1\\1 \end{bmatrix} \right\}$$
 is a basis of W .

S4. Let W be the subspace of \mathcal{P}_3 given by $W = \text{span} (\{x^3 - x^2 + 3x - 3, 2x^3 + x + 1, 3x^3 - x^2 + 4x - 2, x^3 + x^2 + x - 7\})$. Compute the dimension of W.

Solution:

$$RREF \left(\begin{bmatrix} 1 & 2 & 3 & 1 \\ -1 & 0 & -1 & 1 \\ 3 & 1 & 4 & 1 \\ -3 & 1 & -2 & -7 \end{bmatrix} \right) = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

This has 3 pivot columns so dim(W) = 3.

A1. Let $T: \mathbb{R}^3 \to \mathbb{R}^4$ be the linear transformation given by

$$T\left(\begin{bmatrix} x \\ y \\ z \end{bmatrix}\right) = \begin{bmatrix} -3x + y \\ -8x + 2y - z \\ 2y + 3z \\ 0 \end{bmatrix}.$$

Write the matrix for T with respect to the standard bases of \mathbb{R}^3 and \mathbb{R}^4 .

Solution:

$$\begin{bmatrix} 3 & 1 & 0 \\ -8 & 2 & -1 \\ 0 & 2 & 3 \\ 0 & 0 & 0 \end{bmatrix}$$

Determine if the map $T: \mathcal{P}^6 \to \mathcal{P}^6$ given by T(f) = xf(x) - f(1) is a linear transformation or not.

S3:

A1:

A2: