Name:	
J#:	Dr. Clontz
Date:	

MASTERY QUIZ DAY 13

Math 237 – Linear Algebra Fall 2017

Version 3

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

Standar	d V	2. Mark:				
Determine if	$\begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix}$	can be written as a linear combination of the vectors	$\begin{bmatrix} -1 \\ -9 \\ 15 \end{bmatrix}$	and	$\begin{bmatrix} 1 \\ 5 \\ -5 \end{bmatrix}$	

Solution:

RREF
$$\begin{pmatrix} \begin{bmatrix} -1 & 1 & | & 0 \\ -9 & 5 & | & 0 \\ 15 & -5 & | & 2 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} 1 & 0 & | & 0 \\ 0 & 1 & | & 0 \\ 0 & 0 & | & 1 \end{bmatrix}$$

Since this system has no solution, $\begin{bmatrix} 0\\0\\2 \end{bmatrix}$ cannot be written as a linear combination of the vectors $\begin{bmatrix} -1\\-9\\15 \end{bmatrix}$ and $\begin{bmatrix} 1\\5\\-5 \end{bmatrix}$.

Determine if the set of vectors $\left\{ \begin{bmatrix} 3\\-1\\0\\4 \end{bmatrix}, \begin{bmatrix} 1\\2\\-2\\1 \end{bmatrix}, \begin{bmatrix} 3\\-8\\6\\5 \end{bmatrix} \right\}$ is linearly dependent or linearly independent.

Solution:

$$RREF \left(\begin{bmatrix} 3 & 1 & 3 \\ -1 & 2 & -8 \\ 0 & -2 & 6 \\ 4 & 1 & 5 \end{bmatrix} \right) = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & -3 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Since the reduced row echelon form has a nonpivot column, the vectors are linearly dependent.

Additional Notes/Marks