Name:	
J#:	Dr. Clontz
Date:	

MIDTERM EXAM

Math 237 – Linear Algebra Fall 2017

Version 1

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

	Mark:
Standard E1.	

Write a system of linear equations corresponding to the following augmented matrix.

$$\begin{bmatrix} -4 & -1 & 3 & 2 \\ 1 & 2 & -1 & 0 \\ -1 & 4 & 1 & 4 \end{bmatrix}$$

Standard	E2.

Mark:

Find RREF A, where

$$A = \begin{bmatrix} 2 & 2 & 1 & 2 & | & -1 \\ 1 & 1 & 2 & 4 & | & 5 \\ 3 & 3 & -1 & -2 & | & 1 \end{bmatrix}$$

	Mark:
Standard E3.	

Solve the following linear system.

$$4x_1 + 4x_2 + 3x_3 - 6x_4 = 5$$
$$-2x_3 - 4x_4 = 3$$
$$2x_1 + 2x_2 + x_3 - 4x_4 = -1$$

Standard E4.

Mark:

Find a basis for the solution set to the homogeneous system of equations

$$4x_1 + 4x_2 + 3x_3 - 6x_4 = 0$$
$$-2x_3 - 4x_4 = 0$$
$$2x_1 + 2x_2 + x_3 - 4x_4 = 0$$

Standard V1. Mark:

Let V be the set of all points on the line x + y = 2 with the operations, for any $(x_1, y_1), (x_2, y_2) \in V$, $c \in \mathbb{R}$,

$$(x_1, y_1) \oplus (x_2, y_2) = (x_1 + x_2 - 1, y_1 + y_2 - 1)$$

 $c \odot (x_1, y_1) = (cx_1 - (c - 1), cy_1 - (c - 1))$

- (a) Show that this vector space has an additive identity element $\mathbf{0}$ satisfying $(x,y) \oplus \mathbf{0} = (x,y)$.
- (b) Determine if V is a vector space or not. Justify your answer.

Standard V2.

Determine if $\begin{bmatrix} 3 \\ -2 \\ 4 \end{bmatrix}$ belongs to the span of the set $\left\{ \begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix}, \begin{bmatrix} 2 \\ 4 \\ -6 \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \right\}$.

Mark: Standard V3.

Determine if the vectors $\begin{bmatrix} 8\\21\\-7 \end{bmatrix}$, $\begin{bmatrix} -3\\-8\\3 \end{bmatrix}$, $\begin{bmatrix} -1\\-3\\2 \end{bmatrix}$, and $\begin{bmatrix} 4\\11\\-5 \end{bmatrix}$ span \mathbb{R}^3 .

Standard V4.

Mark:

subspace of \mathbb{R}^3 .

Let W be the set of all \mathbb{R}^3 vectors $\begin{bmatrix} x \\ y \\ z \end{bmatrix}$ satisfying x + y + z = 1 (this forms a plane). Determine if W is a

Standard S1.	Mark:

Determine if the set of polynomials $\{-3x^3-8x^2, x^3+2x^2+2, -x^2+3\}$ is linearly dependent or linearly independent

Standard S2.
$$\begin{bmatrix} & & & \\ & & &$$

Standard S3.

$$\begin{bmatrix}
\begin{bmatrix} 2 \\ 0 \\ -2 \\ 0 \end{bmatrix}, \begin{bmatrix} 3 \\ 1 \\ 3 \\ 6 \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 2 \\ 0 \\ 1 \end{bmatrix} \\
\end{bmatrix}$$
Let $W = \operatorname{span} \left(\left\{ \begin{bmatrix} 2 \\ 0 \\ -2 \\ 0 \end{bmatrix}, \begin{bmatrix} 3 \\ 1 \\ 3 \\ 6 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 2 \\ 0 \\ 1 \end{bmatrix} \right\} \right)$. Find a basis of W .

Standard S4.
$$\begin{bmatrix} 1 \\ -1 \\ 3 \\ -3 \end{bmatrix}, \begin{bmatrix} 2 \\ 0 \\ 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 3 \\ -1 \\ 4 \\ -2 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \\ 1 \\ -7 \end{bmatrix}$$
 Compute the dimension of W .