## Readiness Assurance Outcomes

Before beginning this module, each student should be able to...

- $\bullet$  Add Euclidean vectors and multiply Euclidean vectors by scalars.
- Perform basic manipulations of augmented matrices and linear systems (Standard(s) E1,E2,E3).
- Apply linear combinations and spanning sets (Standard(s) V2,V3).

## Readiness Assurance Resources

The following resources will help you prepare for this module.

- https://www.khanacademy.org/math/precalculus/vectors-precalc/vector-addition-subtraction/v/adding-and-subtracting-vectors
- https://www.khanacademy.org/math/precalculus/vectors-precalc/combined-vector-operations/v/combined-vector-operations-example

## Readiness Assurance Test

Choose the most appropriate response for each question.

21) Simplify the following vector expression.

$$4\begin{bmatrix}1\\2\\3\end{bmatrix}-2\begin{bmatrix}1\\2\\3\end{bmatrix}$$

- 22) Express the following system of linear equations as an augmented matrix.

$$2x_1 + x_2 + 4x_3 = 0$$
$$x_1 + x_2 + x_3 = 1$$
$$-3x_1 + 4x_2 + x_3 = -7$$

- (a)  $\begin{bmatrix} 2 & 1 & | & -3 \\ 1 & 1 & | & 4 \\ 4 & 1 & | & 1 \\ 0 & 1 & | & -7 \end{bmatrix}$  (b)  $\begin{bmatrix} 2 & 1 & | & 4 & | & 0 \\ 1 & 1 & 1 & | & 1 \\ -3 & 4 & 1 & | & -7 \end{bmatrix}$  (c)  $\begin{bmatrix} 1 & 1 & | & 1 \\ 1 & -2 & | & 4 \\ 4 & 1 & | & 1 \\ 0 & 1 & | & -7 \end{bmatrix}$  (d)  $\begin{bmatrix} 2 & 1 & | & 4 \\ 1 & 1 & | & 1 \\ -3 & 4 & | & -7 \end{bmatrix}$

- 23) Find RREF  $\begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 5 \\ -2 & 0 & -2 \end{bmatrix}$ .

  - (a)  $\begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix}$  (b)  $\begin{bmatrix} 1 & 2 & 3 \\ 1 & 3 & 4 \\ 0 & 0 & 0 \end{bmatrix}$  (c)  $\begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix}$  (d)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

24) Solve the following system of linear equations.

$$2x_1 + x_2 + 4x_3 = 0$$
$$x_1 + x_2 + x_3 = 1$$
$$-3x_1 + 4x_2 + x_3 = -7$$

- (a)  $\begin{vmatrix} x_1 \\ x_2 \\ x_3 \end{vmatrix} = \begin{vmatrix} 2 \\ 0 \\ -1 \end{vmatrix}$

- (c)  $\begin{vmatrix} x_1 \\ x_2 \\ x_3 \end{vmatrix} = \begin{bmatrix} 1 \\ -2 \\ 1 \end{bmatrix} + a \begin{bmatrix} 1 \\ 0 \\ 3 \end{bmatrix}$  for all real numbers a
- (d) No solutions

25) Solve the following system of linear equations.

$$x_1 + x_2 + x_3 + x_4 = 4$$
$$2x_1 + 3x_2 + x_4 = 0$$

- (c)  $\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 12 \\ -8 \\ 0 \\ 0 \end{bmatrix} + a \begin{bmatrix} -3 \\ 2 \\ 1 \\ 0 \end{bmatrix} + b \begin{bmatrix} -2 \\ 1 \\ 0 \\ 1 \end{bmatrix}$  for all real (a)  $\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 0 \\ 1 \end{bmatrix}$ (b)  $\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 4 \end{bmatrix} + a \begin{bmatrix} 0 \\ 3 \\ 1 \end{bmatrix}$  for all real numbers a(d) No solutions
- 26) How many vectors are required to span all of  $\mathbb{R}^4$  (the space of Euclidean vectors with four components)?
  - (a) 2

(b) 3

(c) 4

- (d) 5
- 27) How many vectors are required to span all of  $\mathcal{P}^4$  (the space of polynomials of degree four or less)?
  - (a) 2

(b) 3

(c) 4

(d) 5

- 28) Which vector is a linear combination of  $\begin{bmatrix} -3\\2\\1\\0 \end{bmatrix}$  and  $\begin{bmatrix} -2\\1\\0\\1 \end{bmatrix}$ ?
- (b)  $\begin{bmatrix} 0\\0\\3\\-7 \end{bmatrix}$  (c)  $\begin{bmatrix} 2\\2\\0\\1 \end{bmatrix}$

- 29) Which vector belongs to span  $\left\{ \begin{bmatrix} -3\\2\\1\\0 \end{bmatrix}, \begin{bmatrix} -2\\1\\0\\1 \end{bmatrix} \right\}$ ?
  - (a)  $\begin{bmatrix} 3 \\ -7 \\ 1 \\ 1 \end{bmatrix}$
- (b)  $\begin{bmatrix} 4 \\ 1 \\ 2 \\ 3 \end{bmatrix}$  (c)  $\begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \end{bmatrix}$
- 30) The graphical representation of span  $\left\{ \begin{bmatrix} 1\\2\\3 \end{bmatrix} \right\}$  in three-dimensional Euclidean space  $\mathbb{R}^3$  would be which of the following?

(a) a line

(b) a plane

(c) a sphere

(d) all of  $\mathbb{R}^3$