Readiness Assurance Outcomes

Before beginning this module, each student should be able to...

- Solve a system of linear equations (including finding a basis of the solution space if it is homogeneous) by interpreting as an augmented matrix and row reducing (Standard(s) E1, E2, E3, E4).
- State the definition of linear independence, and determine if a set of vectors is linearly dependent or independent (Standard(s) V5).
- State the definition of a spanning set, and determine if a set of vectors spans a vector space or subspace (Standard(s) V6, V7).
- State the definition of a basis, and determine if a set of vectors is a basis (Standard(s) V8, V9).

Readiness Assurance Resources

The following resources will help you prepare for this module.

• Review the supporting Standards listed above.

Readiness Assurance Test

Choose the most appropriate response for each question.

1) Which of the following is a solution to the system of linear equations

$$x + 3y - z = 2$$

 $2x + 8y + 3z = -1$
 $-x - y + 9z = -10$

- (a) $\begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$
- (b) $\begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix}$
- $(c) \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$
- $(d) \begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$

2) Find a basis for the solution set of the following homogeneous system of linear equations

$$x + 2y + -z - w = 0$$
$$-2x - 4y + 3z + 5w = 0$$

- $(a) \ \left\{ \begin{bmatrix} 2\\1\\0\\0 \end{bmatrix}, \begin{bmatrix} 2\\0\\3\\1 \end{bmatrix} \right\}$
- $\left\{ \begin{bmatrix} 2\\2\\0\\0\\0 \end{bmatrix}, \begin{bmatrix} 0\\0\\3\\0 \end{bmatrix} \right\}$
- (c) $\left\{ \begin{bmatrix} 2\\1\\3\\1 \end{bmatrix} \right\}$
- (d) None of these are a basis.

3) Determine which property applies to the set of vectors

$$\left\{ \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \right\} \subset \mathbb{R}^3.$$

- (a) It does not span and is linearly dependent
- (b) It does not span and is linearly independent
- (c) It spans but it is linearly dependent
- (d) It is a basis of \mathbb{R}^3 .

4) Determine which property applies to the set of vectors

$$\left\{ \begin{bmatrix} 1\\0\\0 \end{bmatrix}, \begin{bmatrix} 2\\1\\0 \end{bmatrix}, \begin{bmatrix} 1\\1\\3 \end{bmatrix} \right\} \subset \mathbb{R}^3.$$

- (a) It does not span and is linearly dependent
- (b) It does not span and is linearly independent
- (c) It spans but it is linearly dependent
- (d) It is a basis of \mathbb{R}^3 .

5) Determine which property applies to the set of vectors

$$\left\{ \begin{bmatrix} 1\\0\\0 \end{bmatrix}, \begin{bmatrix} -2\\0\\-2 \end{bmatrix}, \begin{bmatrix} 1\\1\\0 \end{bmatrix}, \begin{bmatrix} 3\\3\\-3 \end{bmatrix} \right\} \subset \mathbb{R}^3.$$

- (a) It does not span and is linearly dependent
- (b) It does not span and is linearly independent
- (c) It spans but it is linearly dependent
- (d) It is a basis of \mathbb{R}^3 .
- 6) Determine which property applies to the set of vectors

$$\left\{ \begin{bmatrix} 2\\2\\-1 \end{bmatrix}, \begin{bmatrix} -3\\1\\-2 \end{bmatrix}, \begin{bmatrix} 1\\5\\-4 \end{bmatrix} \right\} \subset \mathbb{R}^3.$$

- (a) It does not span and is linearly dependent
- (b) It does not span and is linearly independent
- (c) It spans but it is linearly dependent
- (d) It is a basis of \mathbb{R}^3 .
- 7) Find a basis for the subspace of \mathbb{R}^4 spanned by the vectors ...
- 8) Suppose you know that every vector in \mathbb{R}^5 can be written as a linear combination of the vectors $\{\vec{v}_1,\ldots,\vec{v}_n\}$. What can you conclude about n?
 - (a) $n \le 5$
 - (b) n = 5
 - (c) $n \ge 5$
 - (d) n could be any positive integer
- 9) Suppose you know that every vector in \mathbb{R}^5 can be written uniquely as a linear combination of the vectors $\{\vec{v}_1,\ldots,\vec{v}_n\}$. What can you conclude about n?
 - (a) $n \le 5$
 - (b) n = 5
 - (c) $n \ge 5$
 - (d) n could be any positive integer
- 10) Suppose you know that every vector in \mathbb{R}^5 can be written uniquely as a linear combination of the vectors $\{\vec{v}_1, \ldots, \vec{v}_n\}$. What can you conclude about the set $\{\vec{v}_1, \ldots, \vec{v}_n\}$?
 - (a) It does not span and is linearly dependent
 - (b) It does not span and is linearly independent
 - (c) It spans but it is linearly dependent
 - (d) It is a basis of \mathbb{R}^3 .