Name:	
J#:	Dr. Clontz
Date:	

## MASTERY QUIZ DAY 21

Math 237 – Linear Algebra Fall 2017

## Version 2

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

Mark: Standard A3.

Determine if each of the following linear transformations is injective (one-to-one) and/or surjective (onto).

(a) 
$$T: \mathbb{R}^3 \to \mathbb{R}^3$$
 given by  $T\left(\begin{bmatrix} x \\ y \\ z \end{bmatrix}\right) = \begin{bmatrix} x+y+z \\ 2y+3z \\ x-y-2z \end{bmatrix}$   
(b)  $S: \mathbb{R}^2 \to \mathbb{R}^3$  given by  $S\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 3x+2y \\ x-y \\ x+4y \end{bmatrix}$ 

(b) 
$$S: \mathbb{R}^2 \to \mathbb{R}^3$$
 given by  $S\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 3x + 2y \\ x - y \\ x + 4y \end{bmatrix}$ 

Mark: Standard A4.

Let  $T: \mathbb{R}^4 \to \mathbb{R}^4$  be the linear transformation given by

$$T\left(\begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}\right) = \begin{bmatrix} x + 3y + 3z + 7w \\ x + 3y - z - w \\ 2x + 6y + 3z + 8w \\ x + 3y - 2z - 3w \end{bmatrix}$$

Compute the kernel and image of T.