

Name: _____

MASTERY QUIZ DAY 10

Math 237 – Linear Algebra

Version 5

Fall 2017

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

E1. Write an augmented matrix corresponding to the following system of linear equations.

$$x_1 + 3x_2 - 4x_3 + x_4 = 5$$

$$3x_1 + 9x_2 + x_3 - 7x_4 = 0$$

$$x_1 - x_3 + x_4 = 1$$

E3. Solve the system of equations

$$x + 3y - 4z = 5$$

$$3x + 9y + z = 2$$

E4. Find the solution set for the following system of linear equations.

$$\begin{aligned}2x_1 - 2x_2 + 6x_3 - x_4 &= 0 \\3x_1 + 6x_3 + x_4 &= 0 \\-4x_1 + x_2 - 9x_3 + 2x_4 &= 0\end{aligned}$$

V1. Let V be the set of all pairs of real numbers with the operations, for any $(x_1, y_1), (x_2, y_2) \in V$, $c \in \mathbb{R}$,

$$\begin{aligned}(x_1, y_1) \oplus (x_2, y_2) &= (x_1 + x_2, y_1 + y_2) \\c \odot (x_1, y_1) &= (c^2 x_1, c^3 y_1)\end{aligned}$$

- (a) Show that this scalar multiplication \odot distributes over vector addition \oplus .
(b) Determine if V is a vector space or not. Justify your answer.

E1:

E3:

E4:

V1:

E2: