Name: _____

MASTERY QUIZ DAY 8 Math 237 – Linear Algebra
Version 3 Fall 2017

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

E1. Write a system of linear equations corresponding to the following augmented matrix.

$$\left[\begin{array}{ccc|c} 1 & 0 & 4 & 1 \\ 0 & 1 & -1 & 7 \\ 1 & -1 & 3 & -1 \end{array}\right]$$

E3. Solve the following linear system.

$$\begin{aligned} 3x + 2y + z &= 7 \\ x + y + z &= 1 \\ -2x + 3z &= -11 \end{aligned}$$

E4. Find a basis for the solution set to the system of equations

$$\begin{aligned} x + 2y - 3z &= 0 \\ 2x + y - 4z &= 0 \\ 3y - 2z &= 0 \\ x - y - z &= 0 \end{aligned}$$

V1. Let V be the set of all real numbers together with the operations $\oplus$ and $\odot$ defined by, for any $x, y \in V$ and $c \in \mathbb{R}$,

$$\begin{aligned} x \oplus y &= x + y - 3 \\ c \odot x &= cx - 3(c-1) \end{aligned}$$

(a) Show that this scalar multiplication $\odot$ is associative.

(b) Determine if V is a vector space or not. Justify your answer

E1: **E3:** **E4:** **V1:** **E2:**