Name:

J#:

Dr. Clontz

Date:

## MASTERY QUIZ DAY 23

Math 237 – Linear Algebra Fall 2017

## Version 4

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

Standard A3.

Mark:

Determine if each of the following linear transformations is injective (one-to-one) and/or surjective (onto).

- (a)  $S: \mathbb{R}^2 \to \mathbb{R}^3$  where  $S(\vec{e}_1) = \begin{bmatrix} 2\\1\\0 \end{bmatrix}$  and  $S(\vec{e}_2) = \begin{bmatrix} 1\\2\\1 \end{bmatrix}$ .
- (b)  $T: \mathbb{R}^3 \to \mathbb{R}^2$  where  $T(\vec{e}_1) = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$ ,  $T(\vec{e}_2) = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ , and  $T(\vec{e}_3) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ .

Standard A4.

Let  $T: \mathbb{R}^{2\times 3} \to \mathbb{R}^3$  be the linear map given by  $T\left(\begin{bmatrix} a & b & c \\ x & y & z \end{bmatrix}\right) = \begin{bmatrix} a+x \\ b+y \\ c+z \end{bmatrix}$ . Compute a basis for the kernel and a basis for the image of T.

Additional Notes/Marks