Definition 8.3 A linear combination of a set of vectors $\{\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_m\}$ is given by $c_1\mathbf{v}_1 + c_2\mathbf{v}_2 + \dots + c_m\mathbf{v}_m$ for any choice of scalar multiples c_1, c_2, \dots, c_m .

Definition 8.4 The **span** of a set of vectors is the collection of all linear combinations of that set:

$$\operatorname{span}\{\mathbf{v}_1,\mathbf{v}_2,\ldots,\mathbf{v}_m\}=\{c_1\mathbf{v}_1+c_2\mathbf{v}_2+\cdots+c_m\mathbf{v}_m:c_i\text{ is a real number}\}$$