

Name: \_\_\_\_\_

**MASTERY QUIZ DAY 6**

Math 237 – Linear Algebra

**Version 3**

Fall 2017

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

**E1.** Write an augmented matrix corresponding to the following system of linear equations.

$$\begin{aligned}x + 3y - 4z + w &= 5 \\ 3x + 9y + z - 7w &= 0 \\ x - z + w &= 1\end{aligned}$$

**Solution:**

$$\left[ \begin{array}{cccc|c} 1 & 3 & -4 & 1 & 5 \\ 3 & 9 & 1 & -7 & 0 \\ 1 & 0 & -1 & 1 & 1 \end{array} \right]$$

□

**E3.** Solve the system of equations

$$\begin{aligned}x + 3y + 3z + 7w &= 0 \\ x + 3y - z - w &= 0 \\ 2x + 6y + 3z + 8w &= 0 \\ x + 3y - 2z - 3w &= 0\end{aligned}$$

**Solution:**

$$\text{RREF} \left( \left[ \begin{array}{cccc} 1 & 3 & 3 & 7 \\ 1 & 3 & -1 & -1 \\ 2 & 6 & 3 & 8 \\ 1 & 3 & -2 & -3 \end{array} \right] \right) = \left[ \begin{array}{cccc} 1 & 3 & 0 & 1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

Then the solution set is

$$\left\{ \left[ \begin{array}{c} -3a - b \\ a \\ -2b \\ b \end{array} \right] \mid a, b \in \mathbb{R} \right\} = \text{span} \left( \left\{ \left[ \begin{array}{c} 3 \\ -1 \\ 0 \\ 0 \end{array} \right], \left[ \begin{array}{c} 1 \\ 0 \\ 2 \\ -1 \end{array} \right] \right\} \right)$$

□

**E4.** Find a basis for the solution set of the system ...

**E1:**

**E3:**

**E4:**

**E2:**