

## Readiness Assurance Test

Choose the most appropriate response for each question.

- 31) Suppose  $f(x)$  and  $g(x)$  are real-valued functions satisfying

$$\begin{array}{ll} f(2) = 4 & g(2) = 4 \\ f(3) = 5 & g(3) = 5 \\ f(4) = 3 & g(4) = 2 \end{array}$$

Compute  $(f \circ g)(2)$ .

- (a) 3                      (b) 4                      (c) 5                      (d) 6

- 32) Let  $f(x) = x^2 - 2$  and  $g(x) = x^2 + 1$ . Compute the composition function  $(f \circ g)(x)$ .

- (a)  $x^2 - 1$                       (b)  $x^4 - 4x^2 + 5$                       (c)  $x^4 + 2x^2 - 1$                       (d)  $x^4 - x^2 - 2$

- 33) What is the standard matrix corresponding to the linear transformation  $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$  given by  $T \left( \begin{bmatrix} x \\ y \\ z \end{bmatrix} \right) =$

$$\begin{bmatrix} x + 2y - z \\ y + 3z \\ x + 7y \end{bmatrix} ?$$

- (a)  $\begin{bmatrix} 1 & 2 & -1 \\ 1 & 3 & 0 \\ 1 & 7 & 0 \end{bmatrix}$                       (b)  $\begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 7 \\ -1 & 0 & 0 \end{bmatrix}$                       (c)  $\begin{bmatrix} 1 & 2 & -1 \\ 0 & 1 & 3 \\ 1 & 7 & 0 \end{bmatrix}$                       (d)  $\begin{bmatrix} 1 & 0 & 1 \\ 2 & 1 & 7 \\ -1 & 3 & 0 \end{bmatrix}$

- 34) Let  $T : \mathbb{R}^3 \rightarrow \mathbb{R}^2$  be the linear map corresponding to the standard matrix  $\begin{bmatrix} 2 & 1 & -1 \\ 0 & 1 & 3 \end{bmatrix}$ . Compute

$$T \left( \begin{bmatrix} 1 \\ -1 \\ 3 \end{bmatrix} \right).$$

- (a)  $\begin{bmatrix} -2 \\ 8 \end{bmatrix}$                       (b)  $\begin{bmatrix} -2 \\ -8 \end{bmatrix}$                       (c)  $\begin{bmatrix} 2 \\ -4 \end{bmatrix}$                       (d)  $\begin{bmatrix} 2 \\ 4 \end{bmatrix}$

- 35) Let  $T : \mathbb{R}^2 \rightarrow \mathbb{R}^3$  be the linear transformation corresponding to the standard matrix  $A = \begin{bmatrix} 2 & 3 \\ -1 & -1 \\ 0 & 4 \end{bmatrix}$ .

Compute  $T \left( \begin{bmatrix} 2 \\ -1 \end{bmatrix} \right)$ .

- (a)  $\begin{bmatrix} 2 \\ -1 \\ 0 \end{bmatrix}$                       (b)  $\begin{bmatrix} 5 \\ 7 \\ 4 \end{bmatrix}$                       (c)  $\begin{bmatrix} 4 \\ -1 \\ 8 \end{bmatrix}$                       (d)  $\begin{bmatrix} 1 \\ -1 \\ -4 \end{bmatrix}$

- 36) Let  $T : \mathbb{R}^4 \rightarrow \mathbb{R}^2$  be the linear transformation corresponding to the standard matrix  $\begin{bmatrix} 3 & -1 & 0 & 2 \\ -2 & -4 & -1 & 1 \end{bmatrix}$ .

What are the domain and codomain of  $T$ ?

- (a) The domain is  $\mathbb{R}^2$  and the codomain is  $\mathbb{R}^4$
- (b) The domain and codomain are both  $\mathbb{R}^2$
- (c) The domain is  $\mathbb{R}^4$  and the codomain is  $\mathbb{R}^2$
- (d) The domain and codomain are both  $\mathbb{R}^4$

- 37) Which of the following is true of the linear transformation  $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$  given by

$$T \left( \begin{bmatrix} x \\ y \\ z \end{bmatrix} \right) = \begin{bmatrix} x + 3y - 4z \\ x + y \\ 3z \end{bmatrix} ?$$

- (a)  $T$  is neither injective nor surjective
- (b)  $T$  is both injective and surjective
- (c)  $T$  is injective but not surjective
- (d)  $T$  is surjective but not injective

- 38) Which of the following is true of the linear transformation  $T : \mathbb{R}^3 \rightarrow \mathbb{R}^2$  given by

$$T \left( \begin{bmatrix} x \\ y \\ z \end{bmatrix} \right) = \begin{bmatrix} x - y \\ x + z \end{bmatrix} ?$$

- (a)  $T$  is injective but not surjective
- (b)  $T$  is both injective and surjective
- (c)  $T$  is surjective but not injective
- (d)  $T$  is neither injective nor surjective

- 39) Let  $T : \mathbb{R}^n \rightarrow \mathbb{R}^m$  be a linear transformation with standard matrix  $A$ . Which of the following is **not** a characterization of the statement “ $T$  is injective”?

- (a) If  $T(\vec{v}) = T(\vec{w})$  for some  $\vec{v}, \vec{w} \in \mathbb{R}^n$ , then  $\vec{v} = \vec{w}$ .
- (b)  $T$  has a non-trivial kernel, i.e.  $\ker T \neq \{\vec{0}\}$
- (c) The columns of  $A$  are linearly independent
- (d)  $\text{RREF}(A)$  has a pivot in every column

- 40) Let  $T : \mathbb{R}^n \rightarrow \mathbb{R}^m$  be a linear transformation with standard matrix  $A$ . Which of the following is **not** a characterization of the statement “ $T$  is surjective”?

- (a)  $\text{RREF}(A)$  has a pivot in every row
- (b)  $\text{Im } T = \mathbb{R}^m$
- (c) The columns of  $A$  span  $\mathbb{R}^m$
- (d)  $\text{RREF}(A)$  has a pivot in every column