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## **MASTERY QUIZ DAY 17**

Math 237 – Linear Algebra Fall 2017

Version 4

Show all work. Answers without work will not receive credit. You may use a calculator, but you must show all relevant work to receive credit for a standard.

**V3.** Determine if the vectors  $\begin{bmatrix} 1\\1\\2\\1 \end{bmatrix}$ ,  $\begin{bmatrix} 3\\3\\6\\3 \end{bmatrix}$ ,  $\begin{bmatrix} 3\\-1\\3\\-2 \end{bmatrix}$ , and  $\begin{bmatrix} 7\\-1\\8\\-3 \end{bmatrix}$  span  $\mathbb{R}^4$ .

Solution:

$$RREF \left( \begin{bmatrix} 1 & 3 & 3 & 7 \\ 1 & 3 & -1 & -1 \\ 2 & 6 & 3 & 8 \\ 1 & 3 & -2 & -3 \end{bmatrix} \right) = \begin{bmatrix} 1 & 3 & 0 & 1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Since there are zero rows, they do not span. Alternatively, by inspection  $\begin{bmatrix} 3 \\ 3 \\ 6 \\ 3 \end{bmatrix} = 3 \begin{bmatrix} 1 \\ 1 \\ 2 \\ 1 \end{bmatrix}$ , so the set is linearly

dependent, so it spans a subspace of dimension at most 3, therefore it does not span  $\mathbb{R}^4$ .

 ${f V4.}$  Let W be the set of all polynomials of even degree. Determine if W is a subspace of the vector space of all polynomials.

**Solution:** W is closed under scalar multiplication, but not under addition. For example,  $x - x^2$  and  $x^2$  are both in W, but  $(x - x^2) + (x^2) = x \notin W$ .

**S2.** Determine if the set  $\left\{ \begin{bmatrix} 0\\1\\1\\1 \end{bmatrix}, \begin{bmatrix} 1\\-1\\0\\2 \end{bmatrix}, \begin{bmatrix} 1\\0\\-1\\0 \end{bmatrix}, \begin{bmatrix} 0\\2\\0\\-1 \end{bmatrix} \right\}$  is a basis of  $\mathbb{R}^4$ .

Solution:

$$\text{RREF} \left( \begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & -1 & 0 & 2 \\ 1 & 0 & -1 & 0 \\ 1 & 2 & 0 & -1 \end{bmatrix} \right) = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Since this is not the identity matrix, the set is not a basis.

V3: V4: S2: