



Using  $(Closed\ Loop) = \frac{(Direct)}{1 - (Loop)}$  and superposition:

$$\hat{E} = \frac{V \left( \frac{1}{L_s s + R} \right) \left( \frac{K_p s + K_i}{s} \right) - I \left( \frac{K_p s + K_i}{s} \right)}{1 + \left( \frac{1}{L_s s + R} \right) \left( \frac{K_p s + K_i}{s} \right)}$$

Multiplying top and bottom by  $L_s s + R$  :

$$\hat{E} = \frac{V \left( \frac{K_p s + K_i}{s} \right) - I (L_s s + R) \left( \frac{K_p s + K_i}{s} \right)}{L_s s + R + \left( \frac{K_p s + K_i}{s} \right)}$$

Factoring out  $\frac{K_p s + K_i}{s}$  :

$$\hat{E} = [V - I(L_s s + R)] \frac{\left( \frac{K_p s + K_i}{s} \right)}{L_s s + R + \left( \frac{K_p s + K_i}{s} \right)}$$

Clean up:

$$\hat{E} = [V - IR - IL_s s] \frac{K_p s + K_i}{L_s s^2 + (R + K_p)s + K_i}$$

Integrate both sides:

$$\frac{1}{s} \hat{E} = \frac{1}{s} [V - IR - IL_s s] \frac{K_p s + K_i}{L_s s^2 + (R + K_p)s + K_i}$$

$$\hat{\lambda} = \underbrace{\left( \frac{1}{s} [V - IR] - IL_s \right)}_{\text{What I currently use on my controller.}} \underbrace{\left( \frac{K_p s + K_i}{L_s s^2 + (R + K_p)s + K_i} \right)}_{\text{Additional 2DLPF.}}$$

What I currently  
use on my controller.

Additional 2DLPF.