

Import biblioteki **TensorFlow** (<https://www.tensorflow.org/>) z której będziemy korzystali w **uczeniu maszynowym**:

```
import tensorflow as tf
```

Gradient

Możliwe jest wyliczenie gradientu dowolnego wyrażenia różniczkowalnego. Wykorzystujemy do tego metodę **tf.GradientTape()**

Funkcja **jednej zmiennej**:

```
x = tf.Variable(4.0)

with tf.GradientTape() as tape:
    f = x**3          #definicja funkcji f(x)=x^3
    df_dx = tape.gradient(f, x) #gradient 'f' ze względu na zmienną 'x'

df_dx.numpy()

48.0
```

Funkcja **dwóch zmiennych**:

```
x = tf.Variable(4.0)
y = tf.Variable(3.0)

with tf.GradientTape() as tape:
    f = x**3+y**2          #definicja funkcji f(x,y)=x^3+y^2
    df_dx,df_dy = tape.gradient(f,(x,y)) #gradient 'f' ze względu na zmienną 'x' i ze wzg

print(df_dx)
print(df_dy)

tf.Tensor(48.0, shape=(), dtype=float32)
tf.Tensor(6.0, shape=(), dtype=float32)
```

Przykład z **prezentacji**:

```
x = tf.Variable(3.0)
y = tf.Variable(2.0)

with tf.GradientTape() as tape:
    f = (x**2)*y          #definicja funkcji f(x,y)=x^2*y
    df_dx,df_dy = tape.gradient(f,(x,y)) #gradient 'f' ze względu na zmienną 'x' i ze wzg
```

```
print(df_dx)
print(df_dy)

tf.Tensor(12.0, shape=(), dtype=float32)
tf.Tensor(9.0, shape=(), dtype=float32)
```

Trochę skomplikujemy:

```
x = tf.Variable([3.0,2.0])

with tf.GradientTape() as tape:
    f = (x**3) #definicja funkcji f(x)=x^3
    df_dx = tape.gradient(f,x) #gradient 'f' ze względu na zmienną 'x'

print(df_dx)

tf.Tensor([27. 12.], shape=(2,), dtype=float32)
```

I jeszcze trochę skomplikujemy:

```
x = tf.Variable([3.0,2.0])
y = tf.Variable([1.0,0.0])

with tf.GradientTape() as tape:
    f = (x**3)+y**2 #definicja funkcji f(x)=x^3+y^2
    df_dx,df_dy = tape.gradient(f,(x,y)) #gradient 'f' ze względu na zmienną 'x'

print(df_dx)
print(df_dy)

tf.Tensor([27. 12.], shape=(2,), dtype=float32)
tf.Tensor([2. 0.], shape=(2,), dtype=float32)
```

Zmienne mogą być zastąpione przez tensory, wówczas konieczne jest **rejestrowanie wprost** operacji zastosowanych do tych sensorów. Służy do tego metoda **watch()**. W przypadku zmiennych operacje są rejestrowane automatycznie.

```
x = tf.random.normal([2])
y = tf.random.normal([2])

print(x)
print(y)
print("")

with tf.GradientTape() as tape:
    tape.watch(x)
    tape.watch(y)
    f = (x**3)+y**2 #definicja funkcji f(x)=x^3+y^2
    df_dx,df_dy = tape.gradient(f,(x,y)) #gradient 'f' ze względu na zmienną 'x'
```

```

print(ar_ax)
print(df_dy)

tf.Tensor([ 0.5899918 -1.3989412], shape=(2,), dtype=float32)
tf.Tensor([-1.1552613  0.48971453], shape=(2,), dtype=float32)

tf.Tensor([1.044271 5.871109], shape=(2,), dtype=float32)
tf.Tensor([-2.3105226  0.97942907], shape=(2,), dtype=float32)

```

```

import matplotlib.pyplot as plt
import numpy as np

```

```

number_of_points = 1000
x_point = []
y_point = []

```

```

a = 0.22
b = 0.78

```

```

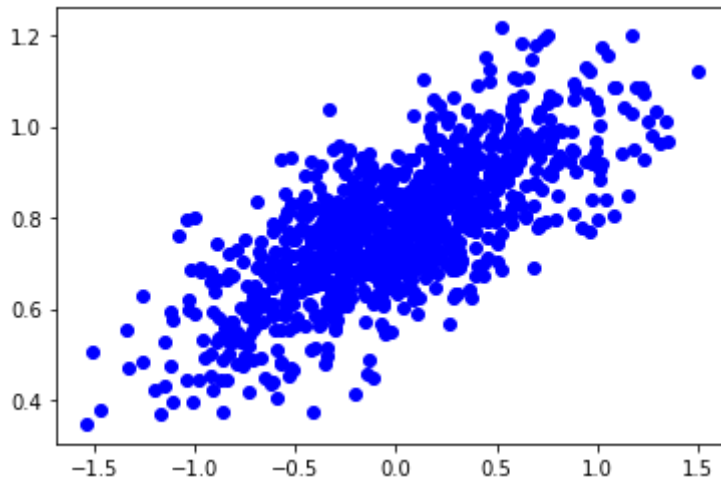
for i in range(number_of_points):
    x = np.random.normal(0.0,0.5)
    y = (a*x+b)+np.random.normal(0.0,0.1)
    x_point.append(x)
    y_point.append(y)

```

```

plt.scatter(x_point,y_point,c='b')
plt.show()

```



```

real_x = np.array(x_point)
real_y = np.array(y_point)

```

Definicja błędu:

```

x = tf.constant([1.0, 2.0, 3.0, 4.0])
tf.reduce_mean(x)

```

```
<tf.Tensor: shape=(), dtype=float32, numpy=2.5>
```

```
def loss_fn(real_y, pred_y):  
    return tf.reduce_mean((real_y - pred_y)**2)
```

```
import random  
a = tf.Variable(random.random())  
b = tf.Variable(random.random())
```

```
Loss = []  
epochs = 50
```

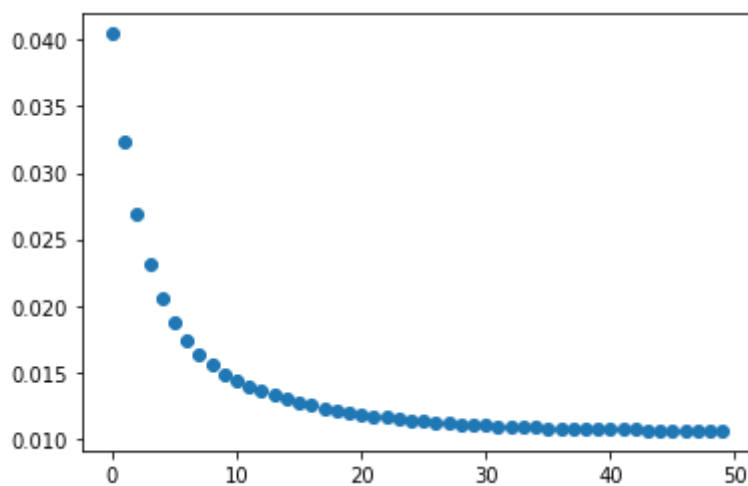
```
for _ in range(epochs):  
    with tf.GradientTape() as tape:  
        pred_y = a * real_x + b  
        loss = loss_fn(real_y, pred_y)  
        Loss.append(loss.numpy())  
  
    dloss_da, dloss_db = tape.gradient(loss,(a, b))  
  
    a.assign_sub(0.1*dloss_da)  
    b.assign_sub(0.1*dloss_db)
```

```
np.max(Loss),np.min(Loss)  
  
(0.040465012, 0.010614281)
```

```
print(a.numpy())  
print(b.numpy())
```

```
0.20191799  
0.7786026
```

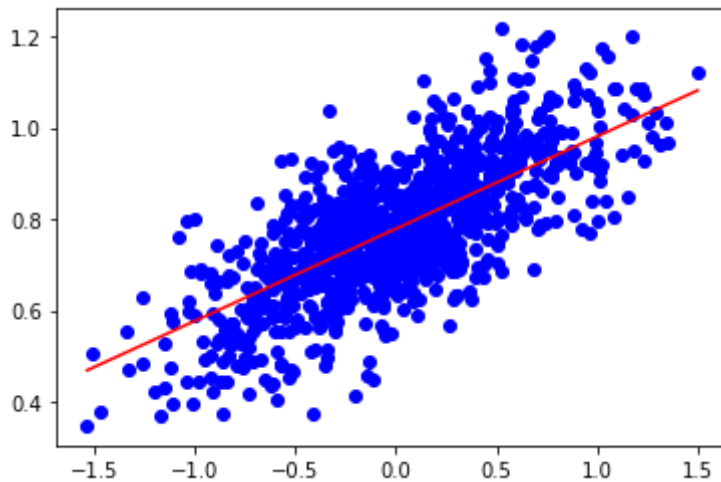
```
plt.scatter(np.arange(epochs),Loss)  
plt.show()
```



```
max = np.max(x_point)
```

```
min = np.min(x_point)
```

```
X = np.linspace(min, max, num=10)  
plt.plot(X,a.numpy()*X+b.numpy(),c='r')  
plt.scatter(x_point,y_point,c="b")  
plt.show()
```



zad.1 a)

```
x = tf.Variable(4.0)
```

```
with tf.GradientTape() as tape:  
    f = ((2*x) ** 2) + 3*x + 4  
    df_dx = tape.gradient(f, x)
```

```
df_dx.numpy()
```

```
35.0
```

b)

```
x = tf.Variable(4.0)
```

```
y = tf.Variable(5.0)
```

```
with tf.GradientTape() as tape:  
    f = ((2*x) ** 3) + ((3*y) ** 2) + 4  
    df_dx, df_dy = tape.gradient(f, (x,y))
```

```
print(df_dx)
```

```
print(df_dy)
```

```
tf.Tensor(384.0, shape=(), dtype=float32)
```

```
tf.Tensor(90.0, shape=(), dtype=float32)
```

c)

```

x = tf.constant([1.0, 3.0])
y = tf.constant([2.0, 1.0])

print(x)
print(y)
print("")

with tf.GradientTape() as tape:
    tape.watch(x)
    tape.watch(y)
    f = ((2*x) ** 3) + ((3*y) ** 2) + 4
    df_dx, df_dy = tape.gradient(f, (x, y))

print(df_dx)
print(df_dy)

tf.Tensor([1. 3.], shape=(2,), dtype=float32)
tf.Tensor([2. 1.], shape=(2,), dtype=float32)

tf.Tensor([ 24. 216.], shape=(2,), dtype=float32)
tf.Tensor([36. 18.], shape=(2,), dtype=float32)

```

zad.2

```

import matplotlib.pyplot as plt

# 1) (4,5)
x = tf.Variable(4.0)
y = tf.Variable(5.0)

with tf.GradientTape() as tape:
    f = (2*x) ** 3 + (3*y) ** 2 + 4
    df_dx, df_dy = tape.gradient(f, (x, y))

print(df_dx)
print(df_dy)
plt.scatter(df_dx, df_dy, c = "red")
print("-----")

# 2) (2,3) -> decrease
x = tf.Variable(2.0)
y = tf.Variable(3.0)

with tf.GradientTape() as tape:
    f = (2*x) ** 3 + (3*y) ** 2 + 4
    df_dx, df_dy = tape.gradient(f, (x, y))

print(df_dx)
print(df_dy)
plt.scatter(df_dx, df_dy, c = "orange")
print("-----")

# 3) (1,2) -> decrease
x = tf.Variable(1.0)

```

```

y = tf.Variable(2.0)

with tf.GradientTape() as tape:
    f = (2*x) ** 3+(3*y) ** 2+4
    df_dx,df_dy = tape.gradient(f, (x,y))

print(df_dx)
print(df_dy)
plt.scatter(df_dx, df_dy, c = "yellow")
print("-----")
#plt.show()

# 4) (5,7) -> increase
x = tf.Variable(5.0)
y = tf.Variable(7.0)

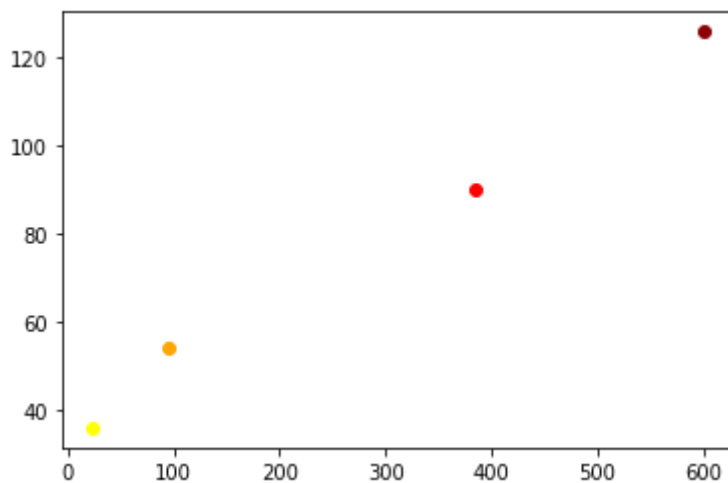
with tf.GradientTape() as tape:
    f = (2*x) ** 3+(3*y) ** 2+4
    df_dx,df_dy = tape.gradient(f, (x,y))

print(df_dx)
print(df_dy)
plt.scatter(df_dx, df_dy, c = "#8b0000") # dark red color

plt.show()

tf.Tensor(384.0, shape=(), dtype=float32)
tf.Tensor(90.0, shape=(), dtype=float32)
-----
tf.Tensor(96.0, shape=(), dtype=float32)
tf.Tensor(54.0, shape=(), dtype=float32)
-----
tf.Tensor(24.0, shape=(), dtype=float32)
tf.Tensor(36.0, shape=(), dtype=float32)
-----
tf.Tensor(600.0, shape=(), dtype=float32)
tf.Tensor(126.0, shape=(), dtype=float32)

```



zad.3

```

import matplotlib.pyplot as plt
import numpy as np

```

```

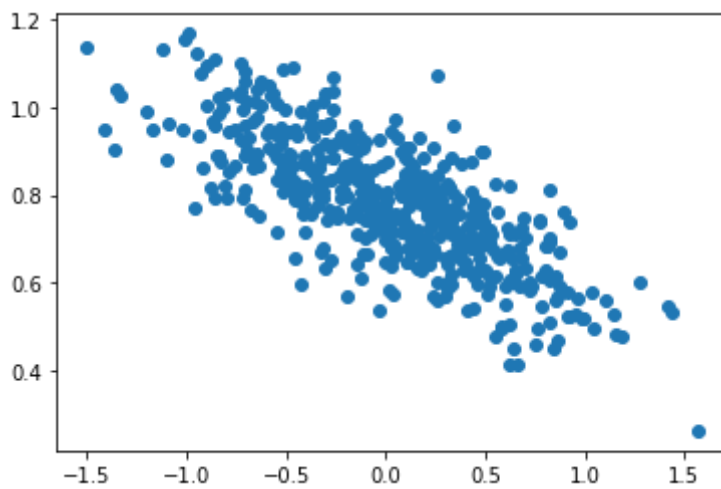
number_of_points = 500
x_point = []
y_point = []

a = 0.22
b = 0.78

for i in range(number_of_points):
    x = np.random.normal(0.0,0.5)
    y = (-a*x+b)+np.random.normal(0.0,0.1)
    x_point.append(x)
    y_point.append(y)

plt.scatter(x_point,y_point,c='tab:blue')
plt.show()

```



```

real_x = np.array(x_point)
real_y = np.array(y_point)

# Definicja błędu:

x = tf.constant([1.0, 2.0, 3.0, 4.0])
tf.reduce_mean(x)

def loss_fn(real_y, pred_y):
    return tf.reduce_mean((real_y - pred_y)**2)

import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())

Loss = []
epochs = 50

for _ in range(epochs):
    with tf.GradientTape() as tape:
        pred_y = a * real_x + b
        loss = loss_fn(real_y, pred_y)
    Loss.append(loss.numpy())

```



```

dloss_da, dloss_db = tape.gradient(loss,(a, b))

a.assign_sub(0.1*dloss_da)
b.assign_sub(0.1*dloss_db)

np.max(Loss),np.min(Loss)

print(a.numpy())
print(b.numpy())

plt.scatter(np.arange(epochs),Loss)
plt.show()

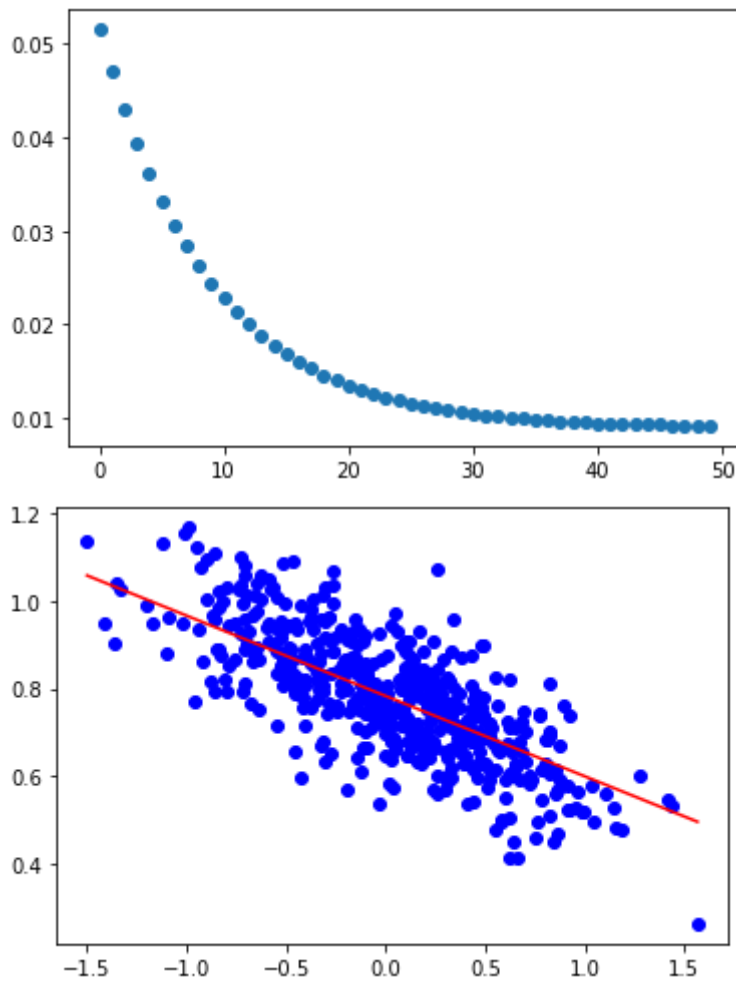
max = np.max(x_point)
min = np.min(x_point)

X = np.linspace(min, max, num=10)
plt.plot(X,a.numpy()*X+b.numpy(),c='r')
plt.scatter(x_point,y_point,c="b")
plt.show()

```

-0.18407144

0.7833143



zad.4

```
import numpy as np
```

```
import pandas as pd
import tensorflow as tf
import matplotlib.pyplot as plt

from google.colab import drive
drive.mount('/content/drive',force_remount=True)

import os
os.chdir('/content/drive/My Drive/DM')
```

Mounted at /content/drive

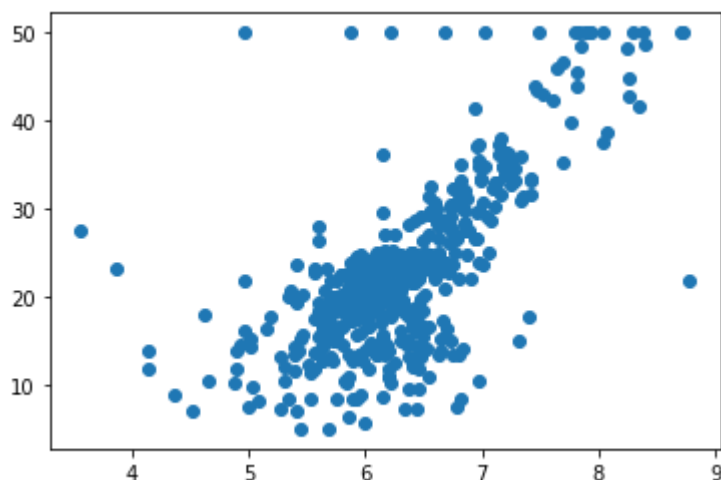
```
data = pd.read_csv('Boston.csv')
print(data)
```

```
rm = data['rm']
medv = data['medv']
```

	Unnamed: 0	crim	zn	indus	chas	...	tax	ptratio	black	lstat	medv
0	1	0.00632	18.0	2.31	0	...	296	15.3	396.90	4.98	24.0
1	2	0.02731	0.0	7.07	0	...	242	17.8	396.90	9.14	21.6
2	3	0.02729	0.0	7.07	0	...	242	17.8	392.83	4.03	34.7
3	4	0.03237	0.0	2.18	0	...	222	18.7	394.63	2.94	33.4
4	5	0.06905	0.0	2.18	0	...	222	18.7	396.90	5.33	36.2
..
501	502	0.06263	0.0	11.93	0	...	273	21.0	391.99	9.67	22.4
502	503	0.04527	0.0	11.93	0	...	273	21.0	396.90	9.08	20.6
503	504	0.06076	0.0	11.93	0	...	273	21.0	396.90	5.64	23.9
504	505	0.10959	0.0	11.93	0	...	273	21.0	393.45	6.48	22.0
505	506	0.04741	0.0	11.93	0	...	273	21.0	396.90	7.88	11.9

[506 rows x 15 columns]

```
plt.scatter(rm, medv, c='tab:blue')
plt.show()
```



```
real_x = np.array(rm)
real_y = np.array(medv)
```

Definicja błędu:

```
x = tf.constant([1 0 2 0 3 0 4 0])
```

```

x = tf.constant([1.0, 2.0, 3.0, 4.0])
tf.reduce_mean(x)

def loss_fn(real_y, pred_y):
    return tf.reduce_mean((real_y - pred_y)**2)

import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())

Loss = []
epochs = 1000
learning_rate = 0.0001
# zmniejszamy "learning_rate"
print("epochs:", epochs, "and learning_rate:", learning_rate, "\n")

for _ in range(epochs):
    with tf.GradientTape() as tape:
        pred_y = a * real_x + b
        loss = loss_fn(real_y, pred_y)
        Loss.append(loss.numpy())

    dloss_da, dloss_db = tape.gradient(loss, (a, b))

    a.assign_sub(learning_rate*dloss_da)
    b.assign_sub(learning_rate*dloss_db)

np.max(Loss), np.min(Loss)

print(a.numpy())
print(b.numpy())

plt.scatter(np.arange(epochs), Loss)
plt.show()

max = np.max(rm)
min = np.min(rm)

X = np.linspace(min, max, num=10)
plt.plot(X, a.numpy()*X+b.numpy(), c='r')
plt.scatter(rm, medv, c="b")
plt.show()

```



epochs: 1000 and learning_rate: 0.0001

3.526375

0.792127

