

Appendix-2.R

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1. Run parallel functions: to assess simulation parameter accuracy

```
options(warn = -1)
source("1.Codes/Appendix 2 parallel functions.R")

## Saving 6.5 x 4.5 in image

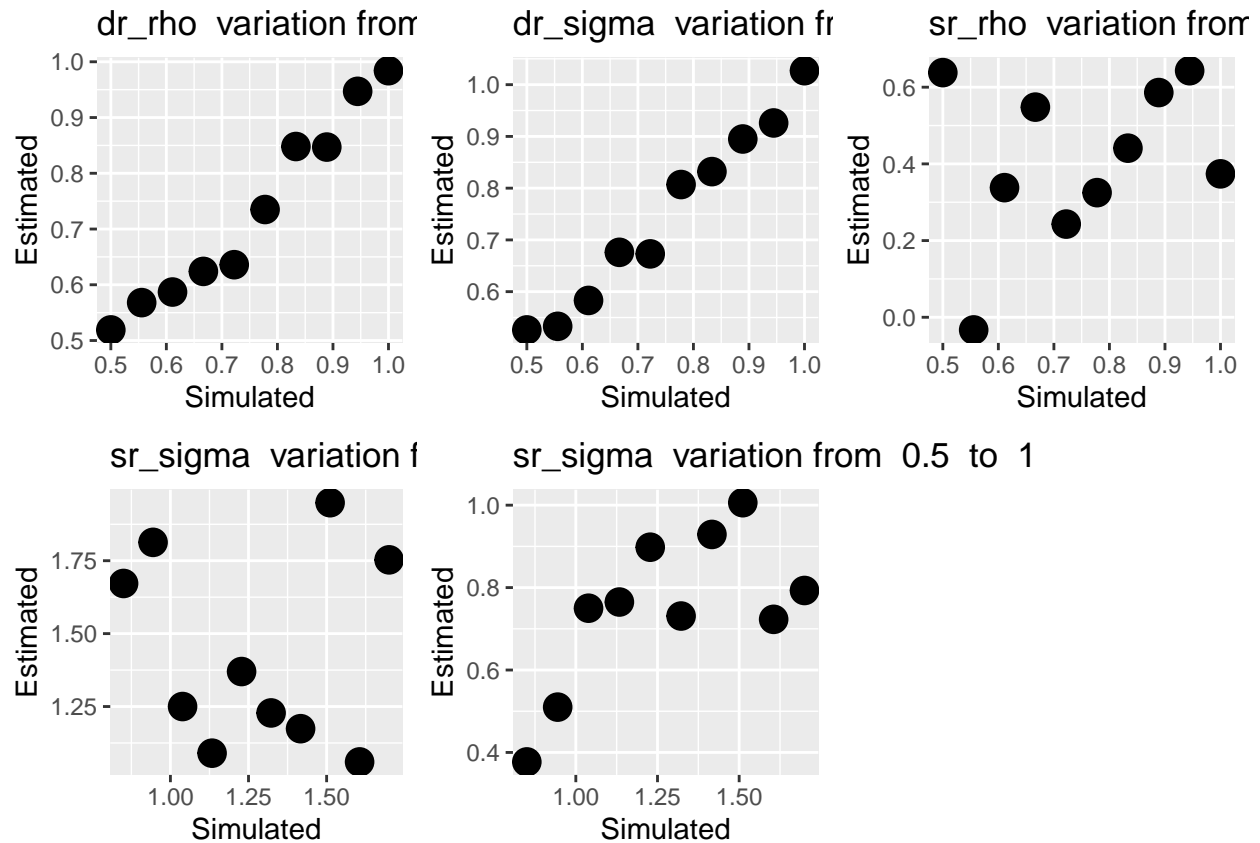
load("2.Results/Appendices/2/dr_rho interactions.Rdata")
p.dr_rho_interactions = plot.function(result)

load("2.Results/Appendices/2/dr_sigma interactions.Rdata")
p.dr_sigma_interactions = plot.function(result)

load("2.Results/Appendices/2/sr_rho interactions.Rdata")
p.sr_rho_interactions = plot.function(result)

load("2.Results/Appendices/2/sr_sigma interactions.Rdata")
p.sr_sigma_interactions = plot.function(result)

ggpubr::ggarrange(p.dr_rho_interactions, p.dr_sigma_interactions, p.sr_rho_interactions, p.sr_sigma_int
```



2. Testing individual characteristics on sociality, exposure, and censoring

```

N_id = 50
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
## Run parallel functions: to assess simulation parameter accuracy..1. Individual characteristics do not
test1 = test.function(att = Hairy,
                      N_id = N_id,
                      individual_predictors=NULL, # individuals characteristics
                      individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals characteristics of
                      exposure_predictors = NULL,
                      exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
                      int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),#no censoring effect
                      simulate.interactions = T,
                      legend = "Figure 1. No Relationship between individuals characteristics (a) sociality, (b) exposure, and (c) censoring")

## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1555.12  -587.03   -86.93   483.17  2572.54

```

```

##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2247.07    119.26  18.842  <2e-16
## att         -96.61    126.77  -0.762    0.45
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 833.5 on 48 degrees of freedom
## Multiple R-squared:  0.01196,    Adjusted R-squared:  -0.008628
## F-statistic: 0.5808 on 1 and 48 DF,  p-value: 0.4497
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -26.294  -8.986  -1.258   9.890  33.705
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  43.0414     2.0486  21.010  <2e-16
## att         -0.1993     2.1776  -0.092    0.927
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.32 on 48 degrees of freedom
## Multiple R-squared:  0.0001746,    Adjusted R-squared:  -0.02066
## F-statistic: 0.00838 on 1 and 48 DF,  p-value: 0.9274
##
## Relationship between individuals characteristics and strength corrected and lm with weigh-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
## -124.558  -41.828   -3.301   48.994  188.013
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  42.5241     1.9923  21.344  <2e-16
## att         -0.1549     2.0007  -0.077    0.939
##

```

```

## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 71.29 on 48 degrees of freedom
## Multiple R-squared:  0.0001249, Adjusted R-squared:  -0.02071
## F-statistic: 0.005996 on 1 and 48 DF,  p-value: 0.9386
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -16.919  -7.329  -2.120   6.883  25.731
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   26.042     1.441   18.074  <2e-16
## att          -1.971     1.532   -1.287   0.204
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.07 on 48 degrees of freedom
## Multiple R-squared:  0.03337, Adjusted R-squared:  0.01323
## F-statistic: 1.657 on 1 and 48 DF,  p-value: 0.2042
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.792e-15  3.950e-17  6.800e-17  1.158e-16
##      2.376e-16
##
## Coefficients:
##              Estimate Std. Error    t value
## (Intercept)  1.000e+00  7.968e-17  1.255e+16
## att         -7.045e-17  8.470e-17 -8.320e-01
##              Pr(>|t|)
## (Intercept)  <2e-16 ***
## att          0.41
## ---
## Signif. codes:

```

```
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.569e-16 on 48 degrees of freedom
## Multiple R-squared:  0.4995, Adjusted R-squared:  0.489
## F-statistic: 47.9 on 1 and 48 DF,  p-value: 9.727e-09
```

```
test1$plots
```

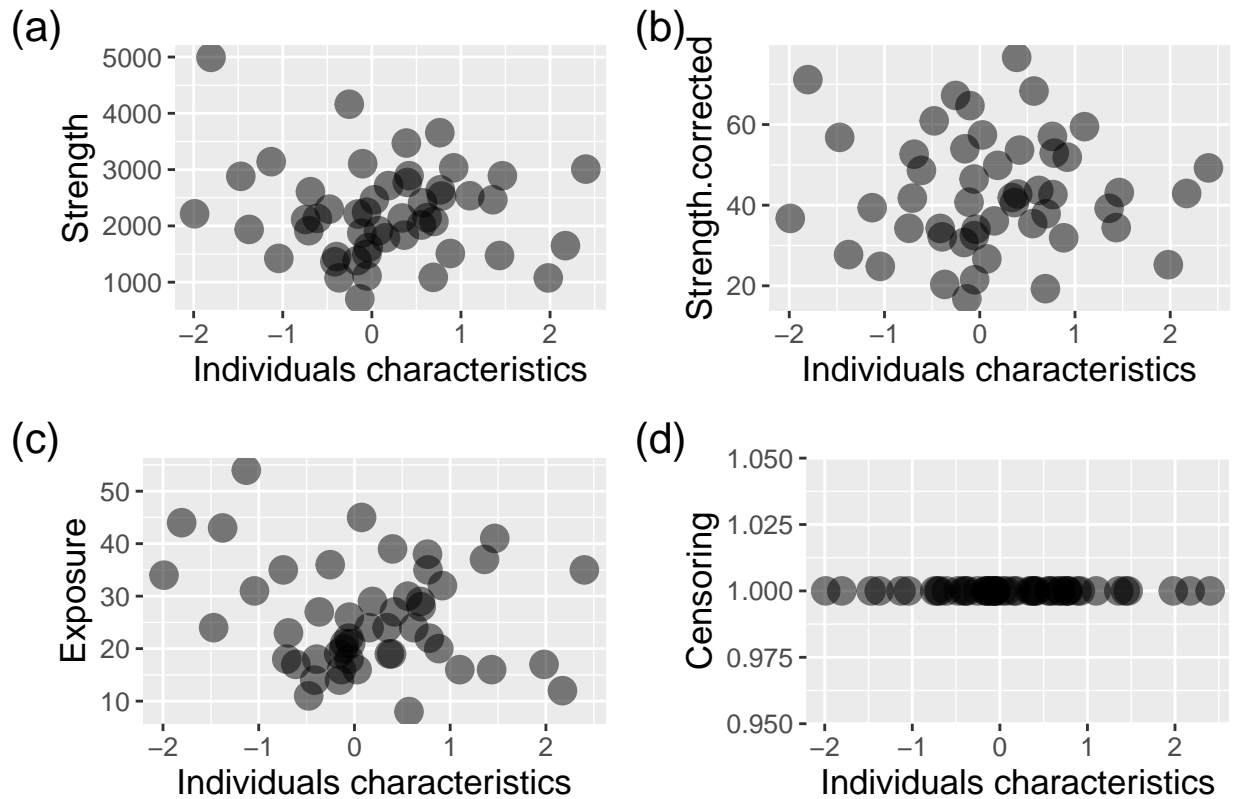


Figure 2: Relationship between individuals characteristics and (a) sociality, (b) sociality corrected by exposure, (c) exposure, or (d) censoring.

The results of the regressions show, as expected, no significant effect in the relationship between individual characteristics, sociality, exposure, or censoring.

2.1. There is a relationship between individual characteristics and sociality, but there is no relationship between individual characteristics, observation bias, and censoring

```
test2 = test.function(att = Hairy,
  N_id = N_id,
  individual_predictors=Hairy, # individuals characteristics
  individual_effects=matrix(c(0.4,0.4),ncol=1, nrow=2), # individuals characteristics
  exposure_predictors = NULL,
  exposure_effects = NULL,exposure_sigma = 1, #no exposure effect
  int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf), #no censoring effect
  simulate.interactions = T,
  legend = "Figure 2. Relationship between individuals characteristics and (a) sociality, (b) sociality corrected by exposure, (c) exposure, (d) censoring, but no relationship between individuals characteristics and (a) sociality, (b) sociality corrected by exposure, (c) exposure, (d) censoring")
```

```
## Relationship between individuals characteristics and strength none corrected-----
```

```

##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2423.60  -866.27   69.53   753.43  2926.24
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2805.6      152.8   18.360  <2e-16
## att           301.7      162.4    1.857   0.0694
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1068 on 48 degrees of freedom
## Multiple R-squared:  0.06704,    Adjusted R-squared:  0.0476
## F-statistic: 3.449 on 1 and 48 DF,  p-value: 0.06943
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
##  -38.775  -7.556   1.357   9.354  24.414
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    51.351      2.139   24.002  <2e-16
## att            4.881      2.274    2.147   0.0369
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.95 on 48 degrees of freedom
## Multiple R-squared:  0.08758,    Adjusted R-squared:  0.06857
## F-statistic: 4.607 on 1 and 48 DF,  p-value: 0.03692
##
## Relationship between individuals characteristics and strength corrected and lm with weigh-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max

```

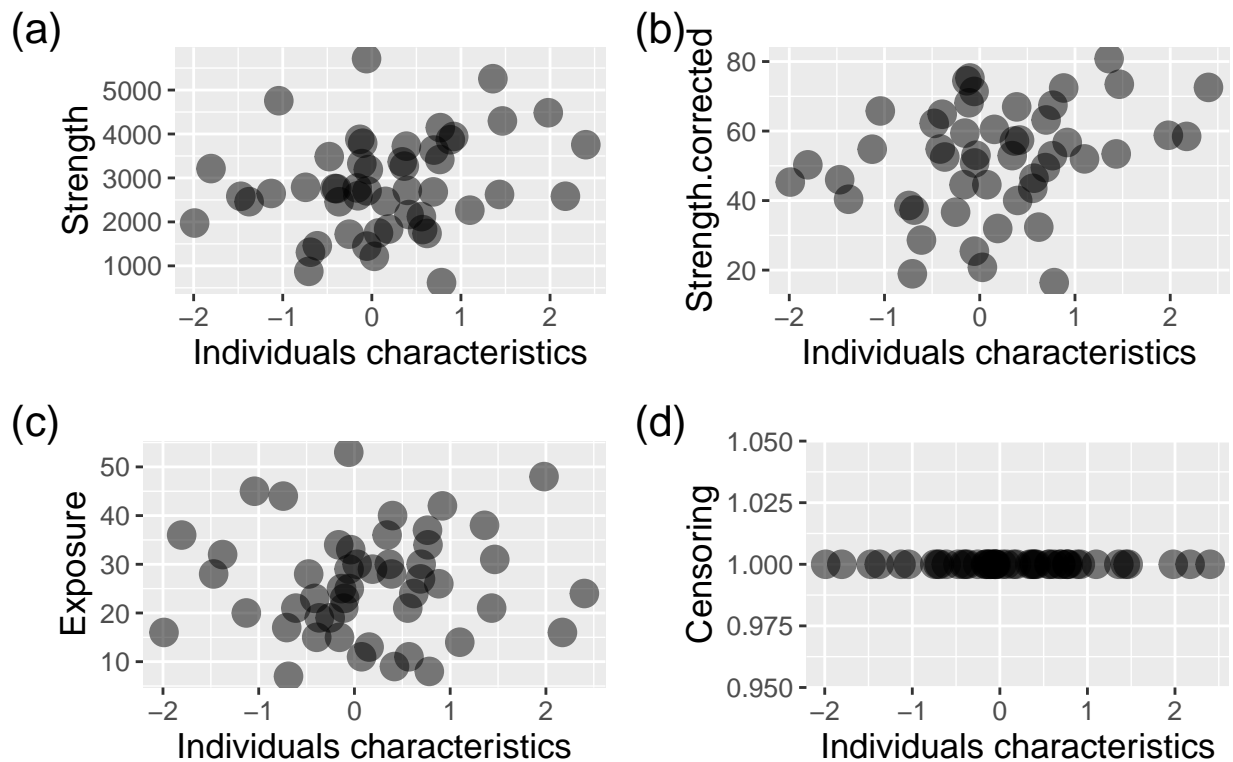
```

## -175.613 -34.250 -0.782 40.254 138.304
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  52.714      2.079  25.356 <2e-16
## att          5.138      2.161   2.378  0.0214
##
## (Intercept) ***
## att          *
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 74.08 on 48 degrees of freedom
## Multiple R-squared:  0.1054, Adjusted R-squared:  0.08674
## F-statistic: 5.654 on 1 and 48 DF,  p-value: 0.02145
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -18.6908  -6.9008  -0.7386   6.8966  26.9845
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  26.0461      1.5513  16.790 <2e-16
## att          0.5159      1.6489   0.313  0.756
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.84 on 48 degrees of freedom
## Multiple R-squared:  0.002035, Adjusted R-squared: -0.01876
## F-statistic: 0.09787 on 1 and 48 DF,  p-value: 0.7558
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.792e-15  3.950e-17  6.800e-17  1.158e-16
##      2.376e-16
##
## Coefficients:
##           Estimate Std. Error    t value

```

```
## (Intercept) 1.000e+00 7.968e-17 1.255e+16
## att        -7.045e-17 8.470e-17 -8.320e-01
##           Pr(>|t|)
## (Intercept) <2e-16 ***
## att         0.41
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.569e-16 on 48 degrees of freedom
## Multiple R-squared: 0.4995, Adjusted R-squared: 0.489
## F-statistic: 47.9 on 1 and 48 DF, p-value: 9.727e-09
```

```
test2$plots
```



re 2. Relationship between individuals characteristics and (a) sociality, (b) sociality corrected by exposure, but no relationship between individuals characteristics (c) exposure, (d) censoring, or (d) censoring.

The results of the regressions show, as expected, a significant effect in the relationship between individual characteristics and sociality, but no significant effect between individuals characteristics exposure, and censoring.

2.2. There is no relationship between individual characteristics, sociality and censoring, but there is a relationship between individual characteristics and exposure

```
test3 = test.function(att = Hairy,
                     N_id = N_id,
                     individual_predictors=Hairy, # individuals characteristics
```



```

individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals characteristics of
exposure_predictors = cbind(rep(1,N_id),Hairy),
exposure_effects = c(-1, 4), exposure_sigma = 1, # exposure effect
int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),#no censoring effect
simulate.interactions = TRUE,
legend = "Figure 3. No relationship between individuals characteristics and (a) strength
but presence of relationship between individuals characteristics and (c) exposure."

## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1812.6  -565.0  -227.3   678.0  2202.8
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2079.2      124.1  16.761  < 2e-16
## att           1112.5      131.9   8.437 4.86e-11
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 867 on 48 degrees of freedom
## Multiple R-squared:  0.5972, Adjusted R-squared:  0.5888
## F-statistic: 71.18 on 1 and 48 DF,  p-value: 4.858e-11
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -30.667 -11.188  -1.074   9.275  31.594
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   40.630      2.158  18.828  < 2e-16
## att           8.891      2.294   3.876 0.000322
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.08 on 48 degrees of freedom
## Multiple R-squared:  0.2384, Adjusted R-squared:  0.2225

```

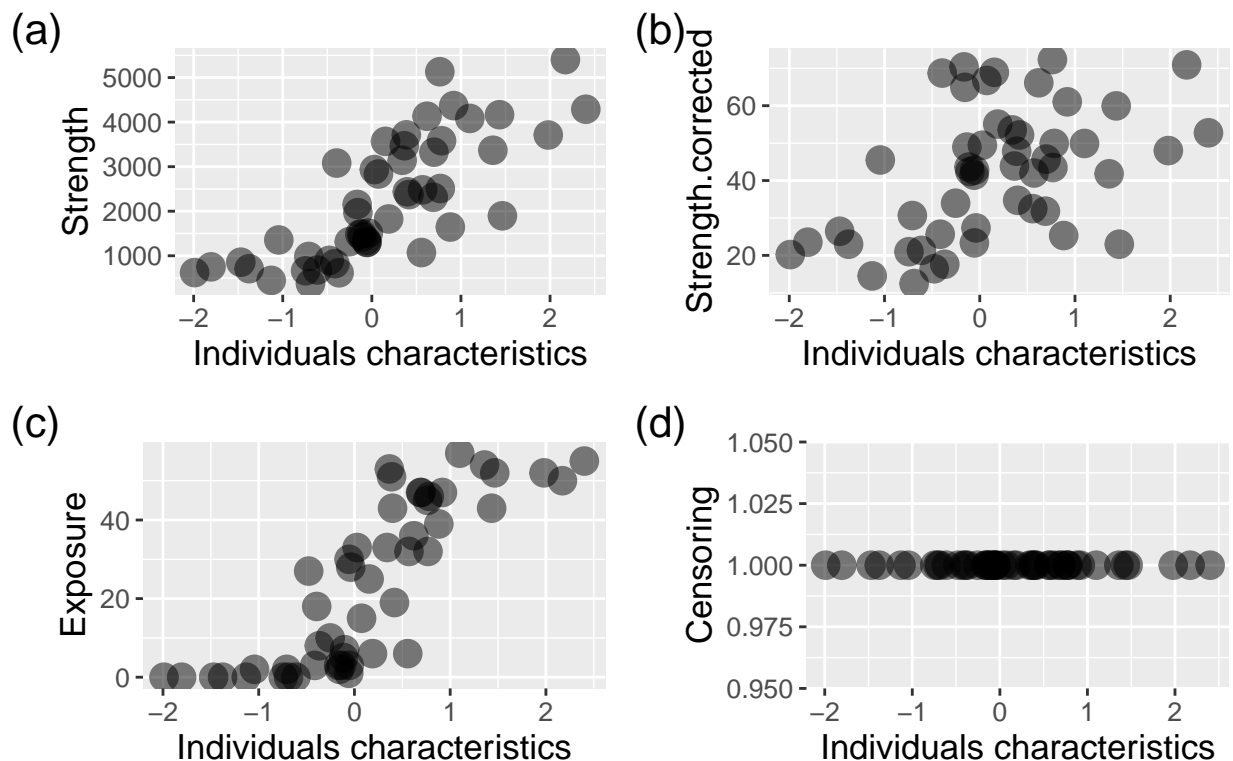
```

## F-statistic: 15.03 on 1 and 48 DF, p-value: 0.0003215
##
## Relationship between individuals characteristics and strength corrected and lm with weighth-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
## -197.39  -22.85    0.00   30.80  171.93
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   42.715      3.369   12.678 1.36e-15
## att           5.220      3.097    1.686  0.0997
##
## (Intercept) ***
## att          .
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 77.13 on 40 degrees of freedom
## Multiple R-squared:  0.06632, Adjusted R-squared:  0.04298
## F-statistic: 2.841 on 1 and 40 DF, p-value: 0.09966
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -24.8448  -9.2760   0.4486  10.0492  25.6136
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   20.822      1.720   12.11 3.37e-16
## att           18.005      1.828    9.85 4.14e-13
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.02 on 48 degrees of freedom
## Multiple R-squared:  0.669, Adjusted R-squared:  0.6621
## F-statistic: 97.02 on 1 and 48 DF, p-value: 4.144e-13
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)

```

```
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.792e-15  3.950e-17  6.800e-17  1.158e-16
##      Max
##  2.376e-16
##
## Coefficients:
##              Estimate Std. Error  t value
## (Intercept)  1.000e+00  7.968e-17  1.255e+16
## att         -7.045e-17  8.470e-17 -8.320e-01
##              Pr(>|t|)
## (Intercept)  <2e-16 ***
## att          0.41
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.569e-16 on 48 degrees of freedom
## Multiple R-squared:  0.4995, Adjusted R-squared:  0.489
## F-statistic:  47.9 on 1 and 48 DF,  p-value: 9.727e-09
```

```
test3$plots
```



hip between individuals characteristics and (a) sociality, (b) sociality corrected by exposure, (d) censoring, but precense of relationship between individuals characteristics and (c) exposure.

The results of the regressions show, as expected, a significant effect in the relationship between individual characteristics and exposure which lead to a significant effect between individuals characteristics and (a) sociality and near significant effect between individuals characteristics and (b) correct ed sociality.

2.3. There is no relationship between individual characteristics, sociality and exposure but there is a relationship between individual characteristics and censoring

```
test4 = test.function(att = Hairy,
                      N_id = N_id,
                      individual_predictors=Hairy, # individuals characteristics
                      individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals characteristics o
                      exposure_predictors = NULL,
                      exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
                      int_intercept = c(0,0), int_slope = c(0.4,0.4),# censoring effect
                      simulate.interactions = T,
                      legend = "Figure 5. No relationship between individuals characteristics and (a) s
                      (c) exposure, but precense of relationship between individuals characteristics and

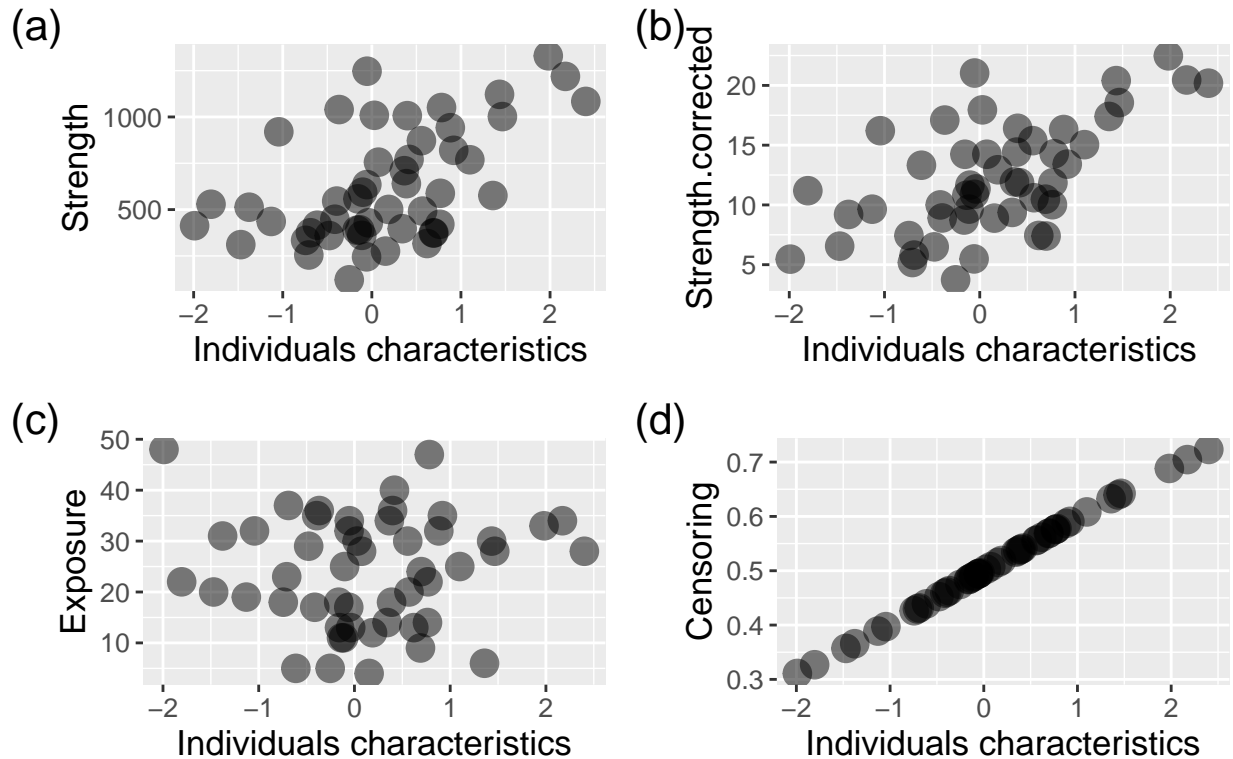
## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -435.03 -185.02  -20.03   160.19   655.90
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    600.56      37.14  16.170  < 2e-16
## att           175.76      39.48   4.452 5.06e-05
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 259.6 on 48 degrees of freedom
## Multiple R-squared:  0.2923, Adjusted R-squared:  0.2775
## F-statistic: 19.82 on 1 and 48 DF,  p-value: 5.059e-05
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
##  -7.2474  -2.4548  -0.2446   2.0042   9.4444
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    11.7568      0.5310  22.140  < 2e-16
## att           3.0661      0.5644   5.432 1.82e-06
##
## (Intercept) ***
```

```

## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.711 on 48 degrees of freedom
## Multiple R-squared:  0.3807, Adjusted R-squared:  0.3678
## F-statistic: 29.51 on 1 and 48 DF,  p-value: 1.824e-06
##
## Relationship between individuals characteristics and strength corrected and lm with weighth-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
## -34.987 -12.581  -3.594   7.032  51.833
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  12.3184     0.5255   23.442 < 2e-16
## att          3.1889     0.5115    6.234 1.1e-07
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 17.97 on 48 degrees of freedom
## Multiple R-squared:  0.4474, Adjusted R-squared:  0.4359
## F-statistic: 38.87 on 1 and 48 DF,  p-value: 1.099e-07
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -19.9434  -9.2230   0.3053   8.3622  24.7791
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  23.8917     1.5794   15.127 <2e-16
## att          0.3372     1.6788    0.201  0.842
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.04 on 48 degrees of freedom

```

```
## Multiple R-squared:  0.0008398, Adjusted R-squared:  -0.01998
## F-statistic: 0.04034 on 1 and 48 DF,  p-value: 0.8417
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.0082853 -0.0012658  0.0000215  0.0015966  0.0028041
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.4999584  0.0003000  1666.6  <2e-16
## att         0.0964259  0.0003189   302.4  <2e-16
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.002097 on 48 degrees of freedom
## Multiple R-squared:  0.9995, Adjusted R-squared:  0.9995
## F-statistic: 9.144e+04 on 1 and 48 DF,  p-value: < 2.2e-16
test4$plots
```



5. No relationship between individuals characteristics and (a) sociality, (b) sociality corrected by exposure, (c) exposure, but precense of relationship between individuals characteristics and (d) censoring.

The results of the regressions show, as expected, a significant effect in the relationship between individual characteristics and censoring which lead to a significant effect between individuals characteristics, (a) sociality and (b) correct ed sociality.

3. Testing when the coefficient of individual characteristics (individual_effects parameter) results in a significant effect on simulated data

```
N_id = 30
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
TEST = seq(from = 0, to = 0.5, by = 0.05)
length(TEST)

## [1] 11

r = NULL
a = 1
for (a in a:length(TEST)) {
  for(b in 1:10){
    r[[length(r)+1]] = test.function(att = Hairy,
                                     N_id = N_id,
                                     individual_predictors=Hairy, # individuals characteristics
                                     individual_effects=matrix(c(TEST[a],TEST[a]),ncol=1, nrow=2), # in
                                     exposure_predictors = NULL,
                                     exposure_effects = c(0, 0), exposure_sigma = 0.5, # exposure effec
```

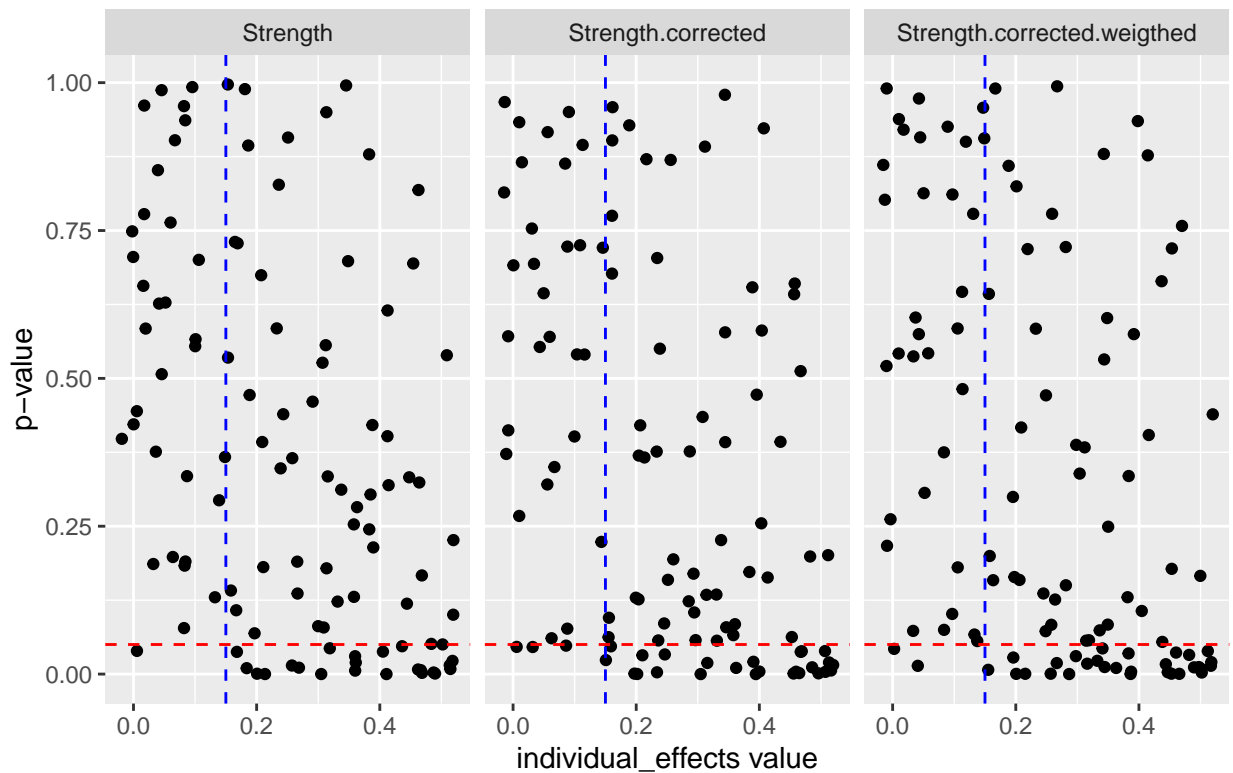
```

int_intercept = c(Inf, Inf), int_slope = c(Inf, Inf), #no censoring e
simulate.interactions = TRUE, print = FALSE)

}
}
d = NULL
test = rep(TEST, each = 10)
for(a in 1:length(r)){
  for (b in 1:length(r[[a]]$result)) {
    s = summary(r[[a]]$result[[b]])
    p = s$coefficients[2,4]
    c = s$coefficients[2,1]
    d = rbind(d, data.frame('coef' = c, 'p' = p, 'effect' = test[a], 'approach' = names(r[[a]]$result)[b]))
  }
}

error.rates(d, threshold = 0.15)

```



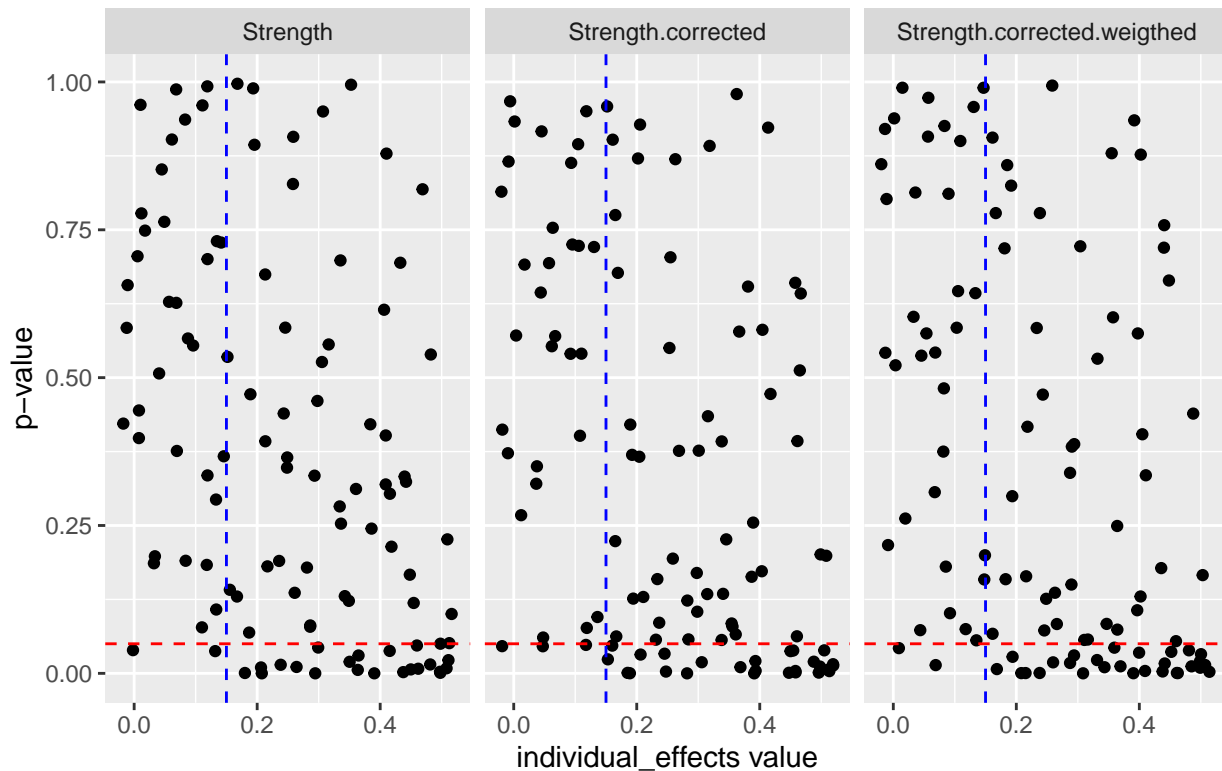
```

## [[1]]
##   false negatives false positives
## 1      100.00      0.000000
## 2      96.25      3.333333
## 3      72.50      3.333333
## 4      67.50     10.000000
## 5      63.75      6.666667
##
##           approaches
## 1           Censoring

```



```
## 2          Exposure
## 3          Strength
## 4      Strength.corrected
## 5 Strength.corrected.weigthed
##
## [[2]]
```



From a visual perspective and error rates we can see that below a value of 0.20 for individual_effects parameters, we obtain no or null effects. We will use values of individual_effects ranging from 0 to 0.19 for simulations without sociality effect and values ranging 0.2 to 0.4 for simulations with sociality effect.

3.1. An example of individual_effects being equal to 0.2 in simulated data

```
N_id = 50
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
test = test.function(att = Hairy,
                    N_id = N_id,
                    individual_predictors=Hairy, # individuals characteristics
                    individual_effects=matrix(c(0.19,0.19),ncol=1, nrow=2), # individuals characterist
                    exposure_predictors = NULL,
                    exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
                    int_intercept = c(Inf,Inf), int_slope = c(-Inf,-Inf),
                    simulate.interactions = T) #no censoring effect

## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
```

```

## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1440.22  -820.80    9.77   585.96  2470.76
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2282.1      138.6   16.468  <2e-16
## att          -135.9      124.1   -1.095    0.279
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 966.2 on 48 degrees of freedom
## Multiple R-squared:  0.02435,    Adjusted R-squared:  0.004028
## F-statistic: 1.198 on 1 and 48 DF,  p-value: 0.2791
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -26.1421 -11.7765  -0.8664   15.2570   27.7550
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    45.565      2.299   19.82  <2e-16
## att           -2.450      2.059   -1.19    0.24
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.03 on 48 degrees of freedom
## Multiple R-squared:  0.02865,    Adjusted R-squared:  0.008409
## F-statistic: 1.416 on 1 and 48 DF,  p-value: 0.24
##
## Relationship between individuals characteristics and strength corrected and lm with weigh-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
## -145.225  -57.389   -4.952   56.704  174.703
##

```

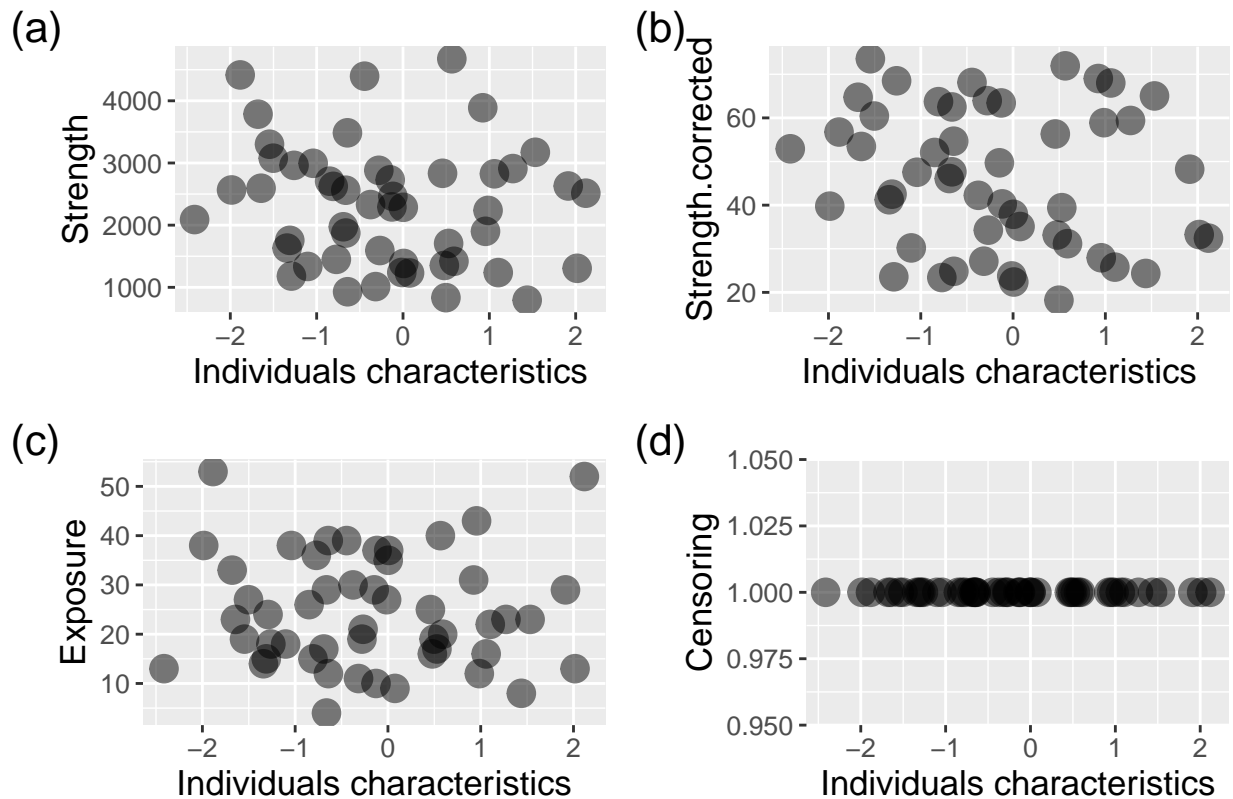
```

## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  45.705      2.274  20.101  <2e-16
## att         -2.465      1.971  -1.251   0.217
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 78.4 on 48 degrees of freedom
## Multiple R-squared:  0.03157,    Adjusted R-squared:  0.01139
## F-statistic: 1.565 on 1 and 48 DF,  p-value: 0.217
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -20.572  -8.323  -1.480   7.857  28.191
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  24.4440      1.6536  14.782  <2e-16
## att         -0.1937      1.4811  -0.131   0.896
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.53 on 48 degrees of freedom
## Multiple R-squared:  0.0003562,    Adjusted R-squared:  -0.02047
## F-statistic: 0.01711 on 1 and 48 DF,  p-value: 0.8965
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.830e-15  5.330e-17  7.920e-17  1.049e-16
##      1.514e-16
##
## Coefficients:
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept) 1.000e+00  8.027e-17 1.246e+16  <2e-16
## att         3.272e-17  7.189e-17 4.550e-01   0.651

```

```
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.597e-16 on 48 degrees of freedom
## Multiple R-squared: 0.494, Adjusted R-squared: 0.4835
## F-statistic: 46.87 on 1 and 48 DF, p-value: 1.266e-08
```

```
test$plots
```



3.2. An example of individual_effects being equal to 0.4 in simulated data

```
N_id = 50
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
test = test.function(att = Hairy,
  N_id = N_id,
  individual_predictors=Hairy, # individuals characteristics
  individual_effects=matrix(c(0.4,0.4),ncol=1, nrow=2), # individuals characteristic
  exposure_predictors = NULL,
  exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
  int_intercept = c(Inf,Inf), int_slope = c(Inf, Inf),
  simulate.interactions = T) #no censoring effect
```

```

## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1594.6  -808.2  -181.9   680.5  2750.4
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2301.0      156.3   14.720  <2e-16
## att           136.7      149.3    0.916   0.364
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1081 on 48 degrees of freedom
## Multiple R-squared:  0.01718,    Adjusted R-squared:  -0.0033
## F-statistic: 0.8388 on 1 and 48 DF,  p-value: 0.3643
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -28.864 -12.829  -5.294   12.768   31.602
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    43.601      2.463   17.704  <2e-16
## att             4.813      2.352    2.046   0.0462
##
## (Intercept) ***
## att          *
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 17.04 on 48 degrees of freedom
## Multiple R-squared:  0.08025,    Adjusted R-squared:  0.06109
## F-statistic: 4.188 on 1 and 48 DF,  p-value: 0.04621
##
## Relationship between individuals characteristics and strength corrected and lm with weigh-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:

```

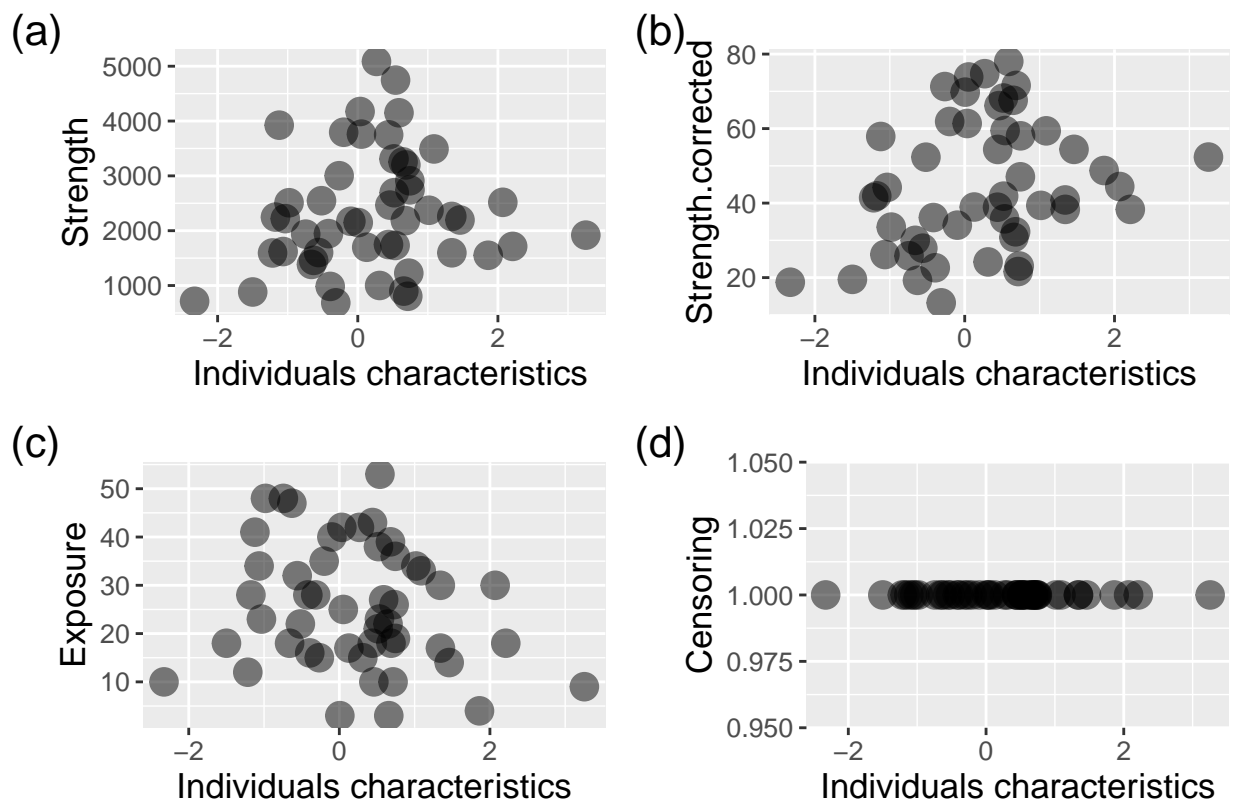
```

##      Min      1Q  Median      3Q      Max
## -152.74 -61.39 -28.80   53.44  190.00
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)   43.887      2.378   18.453  <2e-16
## att           5.724      2.615    2.189  0.0335
##
## (Intercept) ***
## att          *
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 84.4 on 48 degrees of freedom
## Multiple R-squared:  0.09078,    Adjusted R-squared:  0.07183
## F-statistic: 4.792 on 1 and 48 DF,  p-value: 0.03348
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min      1Q  Median      3Q      Max
## -23.134  -9.343  -1.462   10.029   28.117
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)   26.150      1.832   14.278  <2e-16
## att          -2.348      1.749   -1.343   0.186
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.67 on 48 degrees of freedom
## Multiple R-squared:  0.03619,    Adjusted R-squared:  0.01611
## F-statistic: 1.802 on 1 and 48 DF,  p-value: 0.1857
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min      1Q  Median      3Q      Max
## -3.731e-15  7.300e-18  8.520e-17  1.220e-16
##      3.608e-16
##
## Coefficients:

```

```
##           Estimate Std. Error   t value
## (Intercept)  1.000e+00  7.986e-17  1.252e+16
## att         -9.293e-17  7.626e-17 -1.218e+00
##           Pr(>|t|)
## (Intercept)  <2e-16 ***
## att          0.229
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.524e-16 on 48 degrees of freedom
## Multiple R-squared:  0.5052, Adjusted R-squared:  0.4948
## F-statistic: 49 on 1 and 48 DF, p-value: 7.353e-09
```

```
test$plots
```



4. Testing when the coefficient of exposure (exposure_effects parameter) lead to significant effect on simulated data

```
N_id = 30
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
TEST = seq(from = 0, to = 5, by = 0.2)
length(TEST)
```

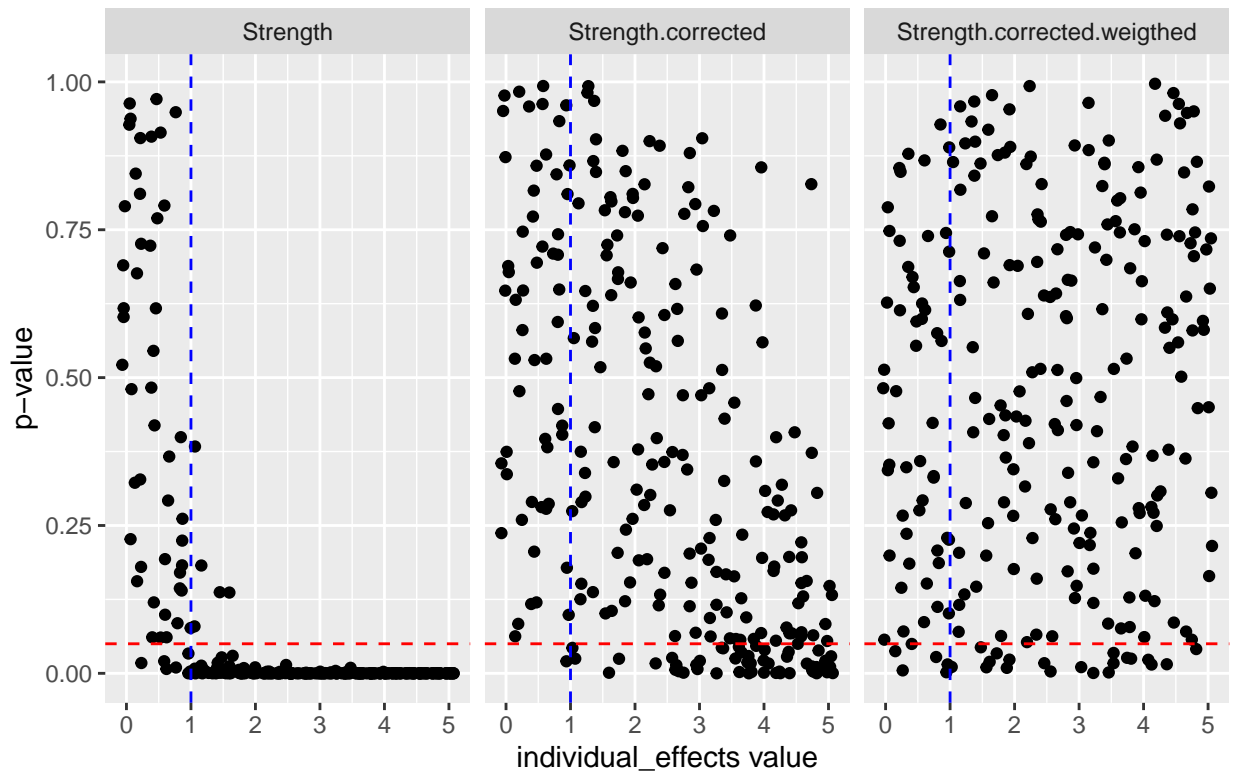
```
## [1] 26
```

```

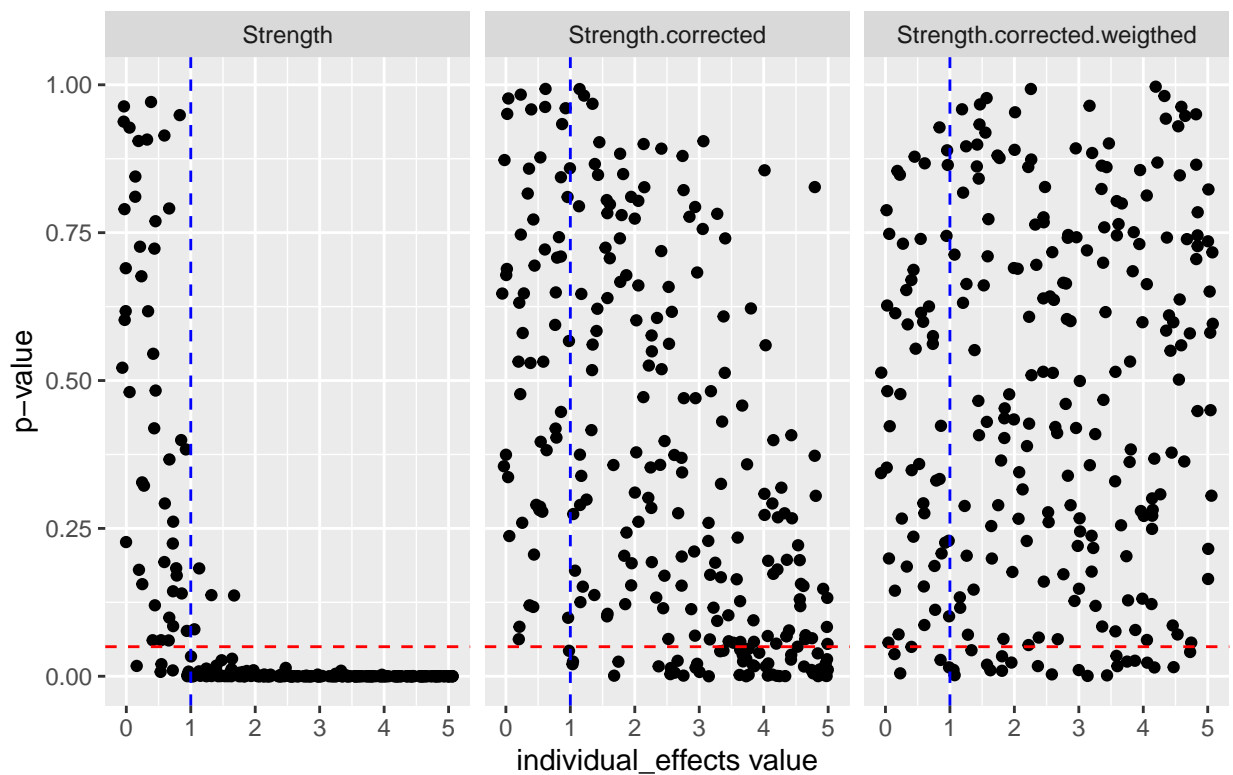
r = NULL
a = 1
for (a in a:length(TEST)) {
  for(b in 1:10){
    r[[length(r)+1]] = test.function(att = Hairy,
                                     N_id = N_id,
                                     individual_predictors=Hairy, # individuals characteristics
                                     individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals ch
                                     exposure_predictors = cbind(rep(1,N_id),Hairy),
                                     exposure_effects = c(-1, TEST[a]), exposure_sigma = 1, # exposure
                                     int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),#no censoring e
                                     simulate.interactions = TRUE, print = FALSE)
  }
}
d = NULL
test = rep(TEST, each = 10)
for(a in 1: length(r)){
  for (b in 1:length(r[[a]]$result)) {
    s = summary(r[[a]]$result[[b]])
    p = s$coefficients[2,4]
    c = s$coefficients[2,1]
    d = rbind(d, data.frame('coef' = c, 'p' = p, 'effect' = test[a], 'approach' = names(r[[a]]$result)[b]))
  }
}

error.rates(d, threshold = 1)

```




```
## [[1]]
##   false negatives false positives
## 1    100.0000000    0.00000
## 2     0.4761905    38.33333
## 3     2.8571429    18.33333
## 4     75.7142857     5.00000
## 5     89.5238095    11.66667
##
##           approaches
## 1           Censoring
## 2           Exposure
## 3           Strength
## 4   Strength.corrected
## 5 Strength.corrected.weigthed
##
## [[2]]
```



From a visual perspective and error rates we can see that above a value of 0.30 for `individual_effects` parameters, we start to observe increase of false positive. We will use values of `exposure_effects` ranging from 0 to 0.20 for simulations without exposure bias and values ranging 0.4 to 0.6 for simulations with exposure bias.

4.1. An example of `exposure_effects` being equal to 0.2 in simulated data

```
N_id = 50
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
test = test.function(att = Hairy,
```

```

        N_id = N_id,
        individual_predictors=Hairy, # individuals characteristics
        individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals characteristics on
        exposure_predictors = cbind(rep(1,N_id),Hairy),
        exposure_effects = c(-1, 0.2), exposure_sigma = 1, # exposure effect
        int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),
        simulate.interactions = T) #no censoring effect

## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1345.1  -535.8  -113.3   523.9  1929.1
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1770.3      108.1  16.374  <2e-16
## att              115.3      105.4   1.094    0.28
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 757.3 on 48 degrees of freedom
## Multiple R-squared:  0.02432,    Adjusted R-squared:  0.003991
## F-statistic: 1.196 on 1 and 48 DF,  p-value: 0.2795
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -30.2805  -9.1502  -0.6431  12.0861  29.5445
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    46.8589      2.1048  22.263  <2e-16
## att           -0.1371      2.0514  -0.067    0.947
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.74 on 48 degrees of freedom
## Multiple R-squared:  9.307e-05,    Adjusted R-squared:  -0.02074

```

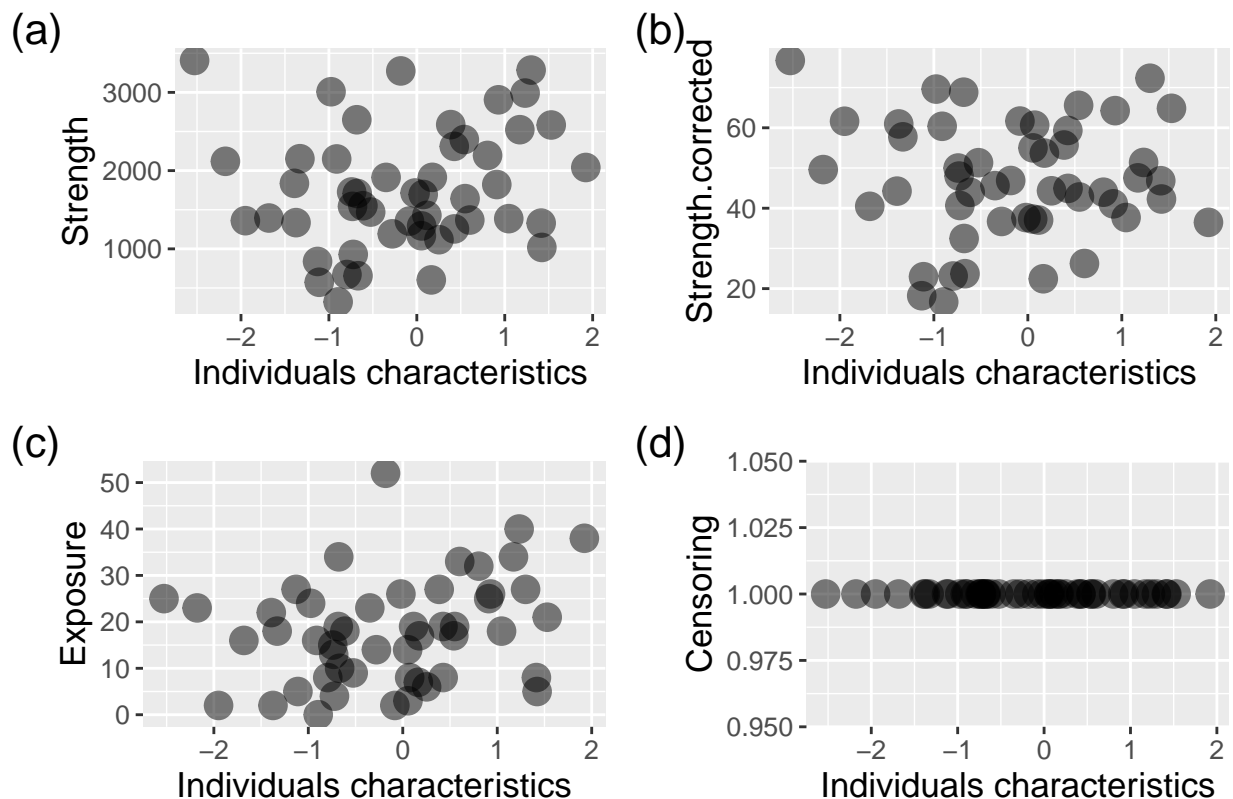
```

## F-statistic: 0.004468 on 1 and 48 DF,  p-value: 0.947
##
## Relationship between individuals characteristics and strength corrected and lm with weighth-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
## -155.917  -36.759   -2.774   28.300  138.204
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   47.544      2.018   23.563  <2e-16
## att          -0.619      1.886   -0.328    0.744
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 60.45 on 47 degrees of freedom
## Multiple R-squared:  0.002287,    Adjusted R-squared:  -0.01894
## F-statistic: 0.1077 on 1 and 47 DF,  p-value: 0.7442
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -17.509  -9.618  -0.788   7.639  34.162
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   18.369      1.577   11.648 1.36e-15
## att           2.911      1.537    1.894  0.0643
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.05 on 48 degrees of freedom
## Multiple R-squared:  0.06953,    Adjusted R-squared:  0.05014
## F-statistic: 3.587 on 1 and 48 DF,  p-value: 0.06428
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)

```

```
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.772e-15  2.370e-17  6.670e-17  1.235e-16
##      Max
## 2.579e-16
##
## Coefficients:
##              Estimate Std. Error  t value Pr(>|t|)
## (Intercept) 1.000e+00  7.930e-17 1.261e+16  <2e-16
## att         7.514e-17  7.729e-17  9.720e-01   0.336
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.554e-16 on 48 degrees of freedom
## Multiple R-squared:  0.5012, Adjusted R-squared:  0.4908
## F-statistic: 48.23 on 1 and 48 DF,  p-value: 8.945e-09
```

```
test$plots
```



4.2. An example of individual_effects being equal to 0.4 in simulated data

```
test = test.function(att = Hairy,
                     N_id = N_id,
                     individual_predictors=Hairy, # individuals characteristics
                     individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals characteristics on
                     exposure_predictors = cbind(rep(1,N_id),Hairy),
                     exposure_effects = c(1, 1), exposure_sigma = 1, # exposure effect
                     int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),
                     simulate.interactions = T) #no censoring effect
```

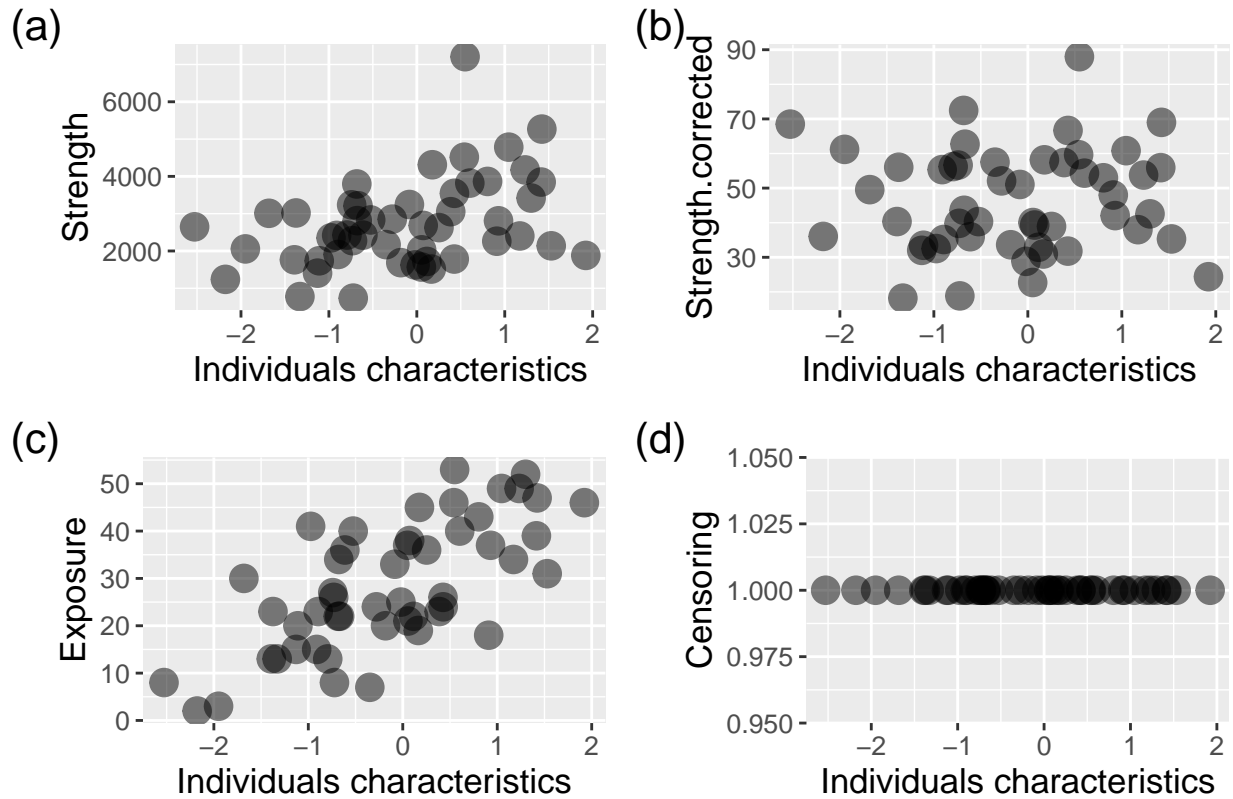
```
## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1836.5  -847.8    -1.7    713.2   4143.6
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2804.7      157.8   17.774 < 2e-16
## att           474.9      153.8    3.088  0.00335
##
## (Intercept) ***
## att          **
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1105 on 48 degrees of freedom
## Multiple R-squared:  0.1657, Adjusted R-squared:  0.1483
## F-statistic: 9.533 on 1 and 48 DF,  p-value: 0.003348
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -27.283 -11.645  -3.447   10.752   41.314
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   46.3217     2.1469   21.576 <2e-16
## att           0.6372     2.0925    0.305  0.762
##
## (Intercept) ***
## att
## ---
```

```

## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.04 on 48 degrees of freedom
## Multiple R-squared:  0.001928,    Adjusted R-squared:  -0.01886
## F-statistic: 0.09274 on 1 and 48 DF,  p-value: 0.762
##
## Relationship between individuals characteristics and strength corrected and lm with weighth-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
## -178.48  -57.03  -11.48   38.55  290.18
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   47.098      2.195   21.457  <2e-16
## att           1.874      2.309    0.811   0.421
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 80.97 on 48 degrees of freedom
## Multiple R-squared:  0.01353,    Adjusted R-squared:  -0.007021
## F-statistic: 0.6584 on 1 and 48 DF,  p-value: 0.4211
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -19.915  -7.750  -1.113   6.678  20.237
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   29.639      1.390   21.330  < 2e-16
## att           9.100      1.354    6.719 1.98e-08
##
## (Intercept) ***
## att          ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.733 on 48 degrees of freedom
## Multiple R-squared:  0.4847, Adjusted R-squared:  0.4739
## F-statistic: 45.15 on 1 and 48 DF,  p-value: 1.984e-08

```

```
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.772e-15  2.370e-17  6.670e-17  1.235e-16
## 2.579e-16
##
## Coefficients:
##              Estimate Std. Error  t value Pr(>|t|)
## (Intercept) 1.000e+00  7.930e-17 1.261e+16  <2e-16
## att         7.514e-17  7.729e-17  9.720e-01   0.336
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.554e-16 on 48 degrees of freedom
## Multiple R-squared:  0.5012, Adjusted R-squared:  0.4908
## F-statistic: 48.23 on 1 and 48 DF,  p-value: 8.945e-09
test$plots
```



Sociality patterns observed in plot (a) are only due to exposure bias (plot (c)).

5. Testing when the coefficient of censoring (int_slope parameter) lead to significant effect on simulated data

```
N_id = 30
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
TEST = seq(from = 0, to = 0.5, by = 0.05)
length(TEST)

## [1] 11

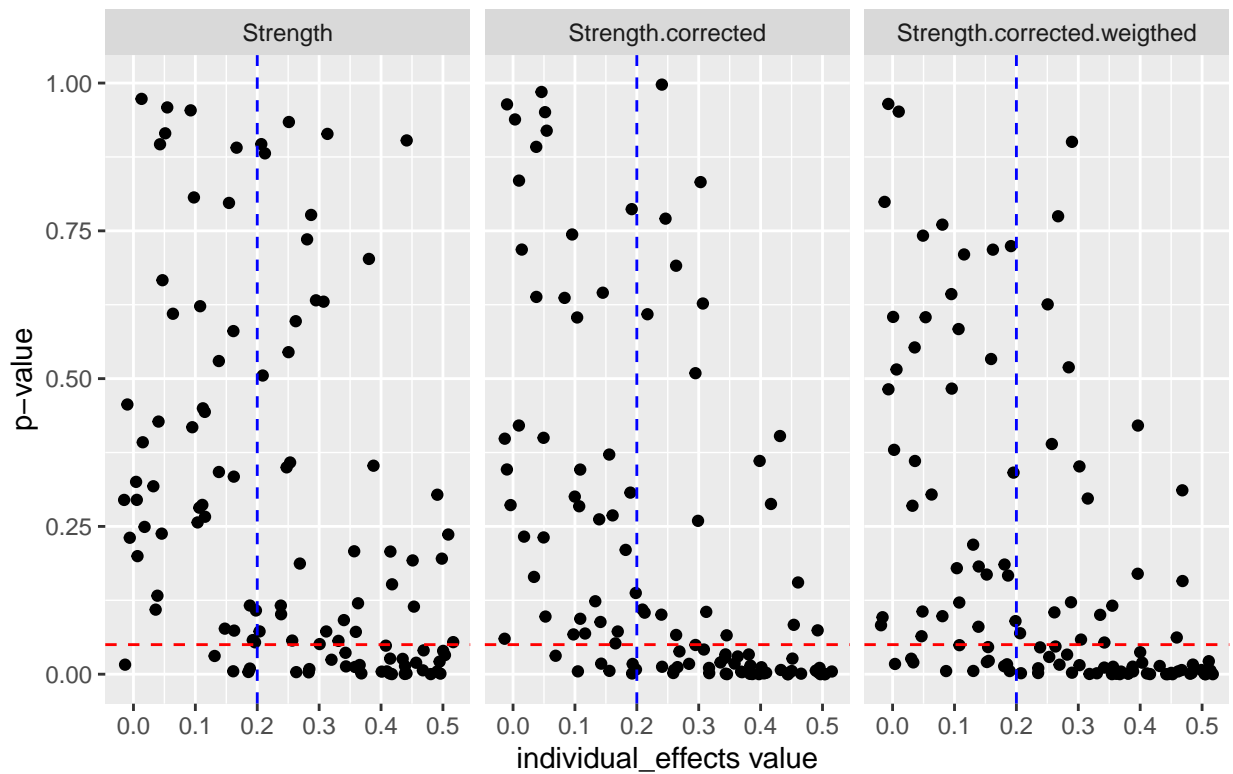
r = NULL
a = 1
for (a in a:length(TEST)) {
  for(b in 1:10){
    r[[length(r)+1]] = test.function(att = Hairy,
                                     N_id = N_id,
                                     individual_predictors=Hairy, # individuals characteristics
                                     individual_effects=matrix(c(0,0),ncol=1, nrow=2), # individuals ch
                                     sr_mu = c(0, 0), sr_sigma = c(1,1), # no sender-receiver effect
                                     dr_mu = c(0,0), dr_sigma = 1, # no dyadic effect
                                     exposure_predictors = NULL,
                                     exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
                                     int_intercept = c(TEST[a],TEST[a]), int_slope = c(TEST[a],TEST[a]))
```



```

simulate.interactions = TRUE, print = FALSE)
}
}
d = NULL
test = rep(TEST, each = 10)
for(a in 1:length(r)){
  for (b in 1:length(r[[a]]$result)) {
    s = summary(r[[a]]$result[[b]])
    p = s$coefficients[2,4]
    c = s$coefficients[2,1]
    d = rbind(d, data.frame('coef' = c, 'p' = p, 'effect' = test[a], 'approach' = names(r[[a]]$result)[b]))
  }
}
error.rates(d, threshold = 0.20)

```

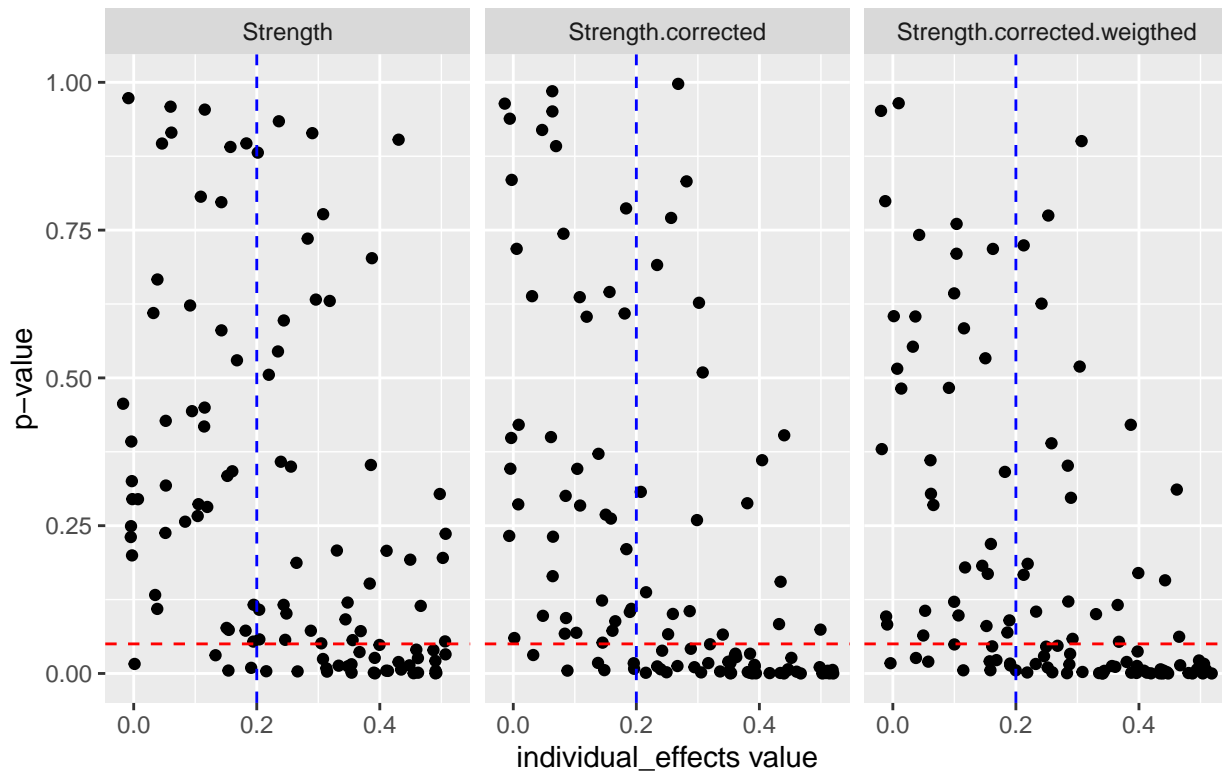


```

## [[1]]
##   false negatives false positives
## 1      0.00000      80
## 2     95.71429      10
## 3     57.14286      10
## 4     34.28571      14
## 5     34.28571      26
##
##           approaches
## 1      Censoring
## 2      Exposure

```

```
## 3          Strength
## 4      Strength.corrected
## 5 Strength.corrected.weigthed
##
## [[2]]
```



From a visual perspective and error rates we can see that above a value of 0.30 for individual_effects parameters, we start to observe increase of false positive. We will use values of exposure_effects ranging from 0 to 0.20 for simulations without exposure bias and values ranging 0.4 to 0.6 for simulations with exposure bias.

5.1. An example of censoring intercept and slope are equal to 0.1 in simulated data

```
N_id = 100
Hairy = matrix(rnorm(N_id, 0, 1), nrow=N_id, ncol=1)
test = test.function(att = Hairy,
                    N_id = N_id,
                    individual_predictors=Hairy, # individuals characteristics
                    individual_effects=matrix(c(0.2,0.2),ncol=1, nrow=2), # individuals characteristic
                    exposure_predictors = NULL,
                    exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
                    int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),
                    simulate.interactions = T) #no censoring effect
```

```
## Relationship between individuals characteristics and strength none corrected-----
```

```

##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3883.1 -1405.0  -213.9  1272.5  4874.0
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   5365.6      210.8   25.458  <2e-16
## att           183.9       217.3    0.846   0.399
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2091 on 98 degrees of freedom
## Multiple R-squared:  0.007255, Adjusted R-squared:  -0.002875
## F-statistic: 0.7162 on 1 and 98 DF, p-value: 0.3994
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
##  -71.60  -19.44    0.70   25.85   59.14
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   104.105      3.359   30.990  <2e-16
## att           3.249       3.464    0.938   0.351
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 33.33 on 98 degrees of freedom
## Multiple R-squared:  0.008899, Adjusted R-squared:  -0.001215
## F-statistic: 0.8799 on 1 and 98 DF, p-value: 0.3505
##
## Relationship between individuals characteristics and strength corrected and lm with weigh-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max

```

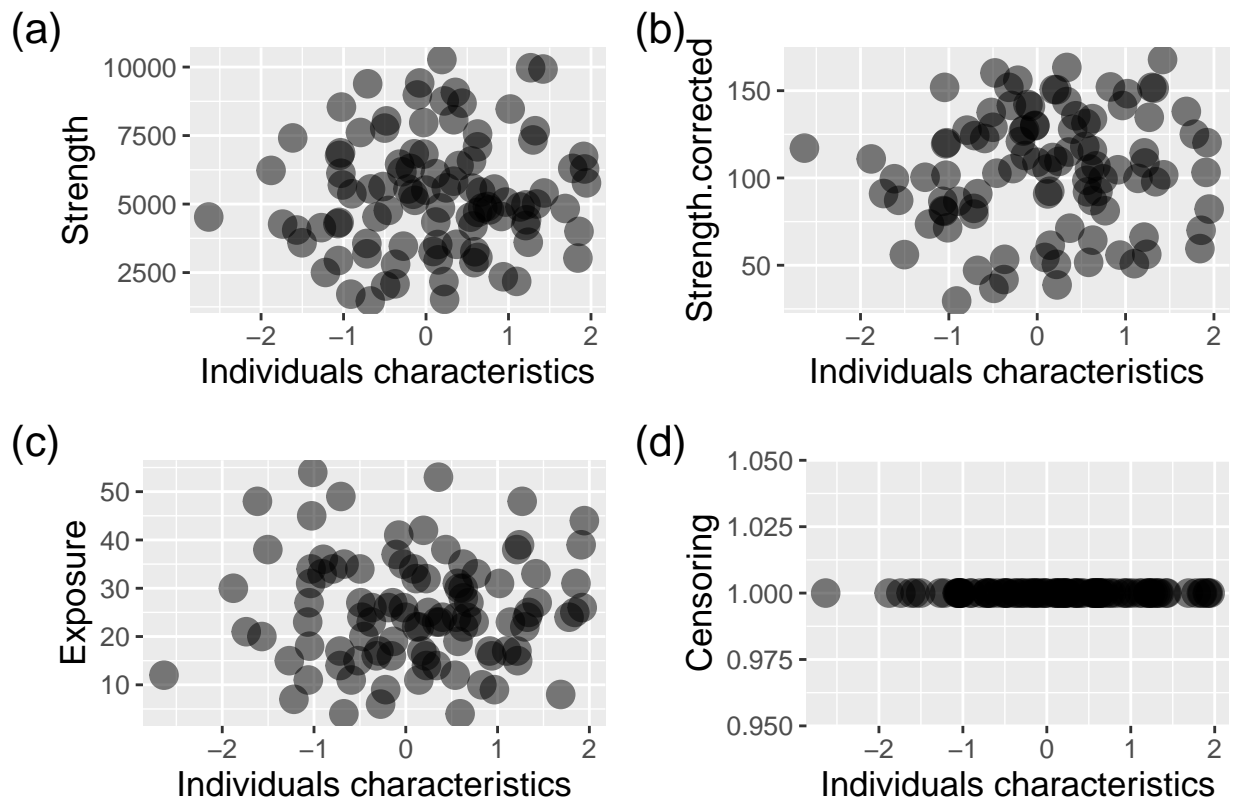
```

## -415.08 -87.38 4.20 127.27 344.28
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 104.191 3.330 31.289 <2e-16
## att 2.630 3.368 0.781 0.437
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 165.9 on 98 degrees of freedom
## Multiple R-squared: 0.006182, Adjusted R-squared: -0.003959
## F-statistic: 0.6096 on 1 and 98 DF, p-value: 0.4368
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
## Min 1Q Median 3Q Max
## -21.410 -8.520 -1.293 7.391 29.068
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 25.2340 1.1163 22.604 <2e-16
## att 0.2982 1.1512 0.259 0.796
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.08 on 98 degrees of freedom
## Multiple R-squared: 0.0006842, Adjusted R-squared: -0.009513
## F-statistic: 0.06709 on 1 and 98 DF, p-value: 0.7962
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
## Min 1Q Median 3Q Max
## -1.861e-14 1.061e-16 1.809e-16 2.709e-16
## 5.318e-16
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)

```

```
## (Intercept) 1.000e+00 1.908e-16 5.241e+15 <2e-16
## att         1.245e-16 1.968e-16 6.330e-01 0.528
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.893e-15 on 98 degrees of freedom
## Multiple R-squared: 0.5013, Adjusted R-squared: 0.4962
## F-statistic: 98.52 on 1 and 98 DF, p-value: < 2.2e-16
```

```
test$plots
```



5.2. An example of individual_effects being equal to 0.4 in simulated data

```
test = test.function(att = Hairy,
  N_id = N_id,
  individual_predictors=Hairy, # individuals characteristics
  individual_effects=matrix(c(0.18,0.18),ncol=1, nrow=2), # individuals characterist
  exposure_predictors = NULL,
  exposure_effects = c(0, 0), exposure_sigma = 1, # exposure effect
  int_intercept = c(Inf,Inf), int_slope = c(Inf,Inf),
  simulate.interactions = T) #no censoring effect
```

```

## Relationship between individuals characteristics and strength none corrected-----
##
## Call:
## lm(formula = Strength ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3468.0 -1638.1  -104.7   1384.8   4744.7
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   4881.5      200.2   24.388  <2e-16
## att           150.5      206.4    0.729   0.468
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1986 on 98 degrees of freedom
## Multiple R-squared:  0.005395, Adjusted R-squared:  -0.004754
## F-statistic: 0.5316 on 1 and 98 DF, p-value: 0.4677
##
## Relationship between individuals characteristics and strength corrected -----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -59.365 -27.297   1.591  22.410  77.286
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   97.2248     3.2492  29.923  <2e-16
## att          -0.5525     3.3506  -0.165   0.869
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 32.24 on 98 degrees of freedom
## Multiple R-squared:  0.0002774, Adjusted R-squared:  -0.009924
## F-statistic: 0.02719 on 1 and 98 DF, p-value: 0.8694
##
## Relationship between individuals characteristics and strength corrected and lm with weigh-----
##
## Call:
## lm(formula = Strength.corrected ~ att, data = df, weights = Exposure)
##
## Weighted Residuals:

```

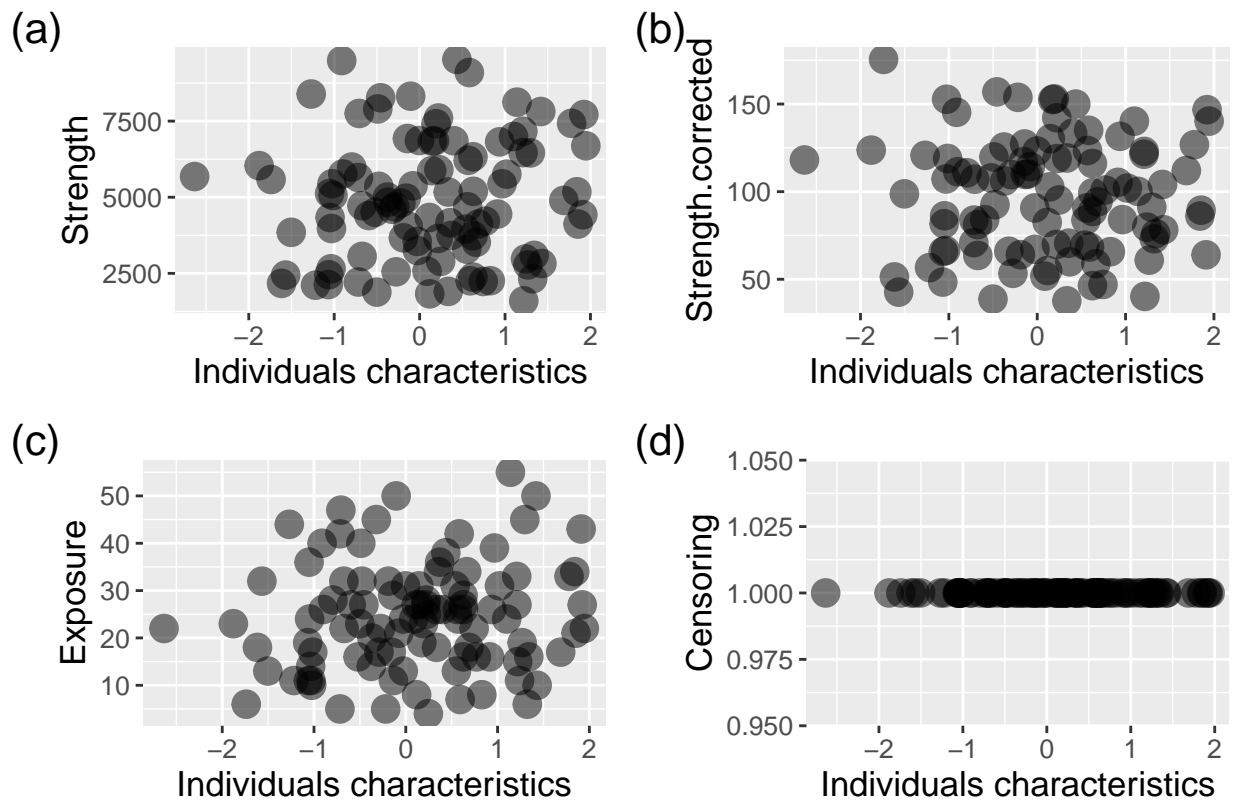
```

##      Min      1Q  Median      3Q      Max
## -308.74 -95.62   6.14  111.58  318.37
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)   97.865      3.148  31.087 <2e-16
## att           1.065      3.249   0.328  0.744
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 153.2 on 98 degrees of freedom
## Multiple R-squared:  0.001094, Adjusted R-squared: -0.009099
## F-statistic: 0.1073 on 1 and 98 DF, p-value: 0.7439
##
## Relationship between individuals characteristics and exposure -----
##
## Call:
## lm(formula = Exposure ~ att, data = df)
##
## Residuals:
##      Min      1Q  Median      3Q      Max
## -20.6682  -8.9314   0.1515   6.5311  29.0624
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)   24.318      1.136  21.412 <2e-16
## att           1.420      1.171   1.212  0.228
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.27 on 98 degrees of freedom
## Multiple R-squared:  0.01478, Adjusted R-squared:  0.004724
## F-statistic:  1.47 on 1 and 98 DF, p-value: 0.2283
##
## Relationship between individuals characteristics and censoring -----
##
## Call:
## lm(formula = Censoring ~ att, data = df)
##
## Residuals:
##      Min      1Q  Median      3Q      Max
## -1.861e-14  1.061e-16  1.809e-16  2.709e-16
##      5.318e-16
##
## Coefficients:

```

```
##           Estimate Std. Error   t value Pr(>|t|)
## (Intercept) 1.000e+00  1.908e-16 5.241e+15  <2e-16
## att         1.245e-16  1.968e-16 6.330e-01   0.528
##
## (Intercept) ***
## att
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.893e-15 on 98 degrees of freedom
## Multiple R-squared:  0.5013, Adjusted R-squared:  0.4962
## F-statistic: 98.52 on 1 and 98 DF,  p-value: < 2.2e-16
```

```
test$plots
```



```
save.image(file='2.Results/Appendices/Appendix.RData')
```