

**Table 2**Comparison of BMO with CEP, FEP, CES, and FES on benchmark functions  $f_1$ – $f_7$ . All results have been averaged over 50 runs.

Function	Index	BMO	CEP	FEP	CES	FES
$f_1$	Mean	<b>1.2932e–246</b>	2.2e–4	5.7e–4	3.4e–5	2.5e–4
	Std.	0	5.9e–4	1.3e–4	8.6e–6	6.8e–4
	Rank	1	3	5	2	4
$f_2$	Mean	<b>1.3939e–131</b>	2.6e–3	8.1e–3	2.1e–2	6.0e–2
	Std.	8.1401e–131	1.7e–4	7.7e–4	2.2e–3	9.6e–3
	Rank	1	2	3	4	5
$f_3$	Mean	<b>6.4322e–16</b>	5.0e–2	1.6e–2	1.3e–4	1.4e–3
	Std.	4.4102e–15	6.6e–2	1.4e–2	8.5e–5	5.3e–4
	Rank	1	5	4	2	3
$f_4$	Mean	<b>1.9308e–8</b>	2.0	0.3	0.35	5.5e–3
	Std.	1.2335e–7	1.2	0.5	0.42	6.5e–4
	Rank	1	5	3	4	2
$f_5$	Mean	7.5401	6.17	<b>5.06</b>	6.69	33.28
	Std.	16.9421	13.61	5.87	14.45	43.13
	Rank	4	2	1	3	5
$f_6$	Mean	<b>0</b>	577.76	<b>0</b>	411.16	<b>0</b>
	Std.	0	1125.76	0	695.35	0
	Rank	1	5	1	4	1
$f_7$	Mean	<b>5.4117e–4</b>	1.8e–2	7.6e–3	3.0e–2	1.2e–2
	Std.	2.6162e–4	6.4e–3	2.6e–3	1.5e–2	5.8e–3
	Rank	1	4	2	5	3
Average rank		1.43	3.71	2.71	3.43	3.29
Final rank		1	5	2	4	3

**Table 5**Comparison of BMO with CEP, FEP, CES, and FES on benchmark functions  $f_8$ – $f_{13}$ . All results have been averaged over 50 runs.

Function	Index	BMO	CEP	FEP	CES	FES
$f_8$	Mean	<b>–12569.5</b>	–7917.1	–12554.5	–7549.9	–12556.4
	Std.	2.1761e–5	634.5	52.6	631.39	32.53
	Rank	1	4	3	5	2
$f_9$	Mean	<b>9.2371e–16</b>	89.0	4.6e–2	70.82	0.16
	Std.	4.9768e–15	23.1	1.2e–2	21.49	0.33
	Rank	1	5	2	4	3
$f_{10}$	Mean	<b>4.4409e–15</b>	9.2	1.8e–2	9.07	1.2e–2
	Std.	0	2.8	2.1e–2	2.84	1.8e–3
	Rank	1	5	3	4	2
$f_{11}$	Mean	<b>0.0032</b>	8.6e–2	1.6e–2	0.38	3.7e–2
	Std.	0.0051	0.12	2.2e–2	0.77	5.0e–2
	Rank	1	4	2	5	3
$f_{12}$	Mean	<b>1.5705e–32</b>	1.76	9.2e–6	1.18	2.8e–2
	Std.	5.4738e–48	2.4	6.1395e–5	1.87	8.1e–11
	Rank	1	5	2	4	3
$f_{13}$	Mean	4.3949e–4	1.4	1.6e–4	1.39	<b>4.7e–5</b>
	Std.	0.0022	3.7	7.3e–5	3.33	1.5e–5
	Rank	3	5	2	4	1
Average rank		1.33	4.67	2.33	4.33	2.33
Final rank		1	5	2	4	2

1. Recreate the tables above as one table where only functions  $f_1$ ,  $f_2$ ,  $f_3$ ,  $f_5$ ,  $f_6$ ,  $f_7$ ,  $f_8$ , and  $f_9$  are included.
2. Create 4 new columns for each test of our collected data
  - a. Column 1: FA-1
  - b. Column 2: FA-2
  - c. Column 3: FA-3
  - d. Column 4: FA-4
3. Input our collected data into the corresponding region

## OUTPUT

fly\_Optimization/firefly\_algo\_code.py

Begin testing -->

Initial test: move\_restriction = False, alpha = 0.25

Type Begin

f1 1 / 5

f1 2 / 5

f1 3 / 5

f1 4 / 5

f1 5 / 5

f1 --> Mean: 8.804607158189983    STD: 20.27430731088028    Expected min: 0

f2 1 / 5

f2 2 / 5

f2 3 / 5

f2 4 / 5

f2 5 / 5

f2 --> Mean: 0.4026983410215202    STD: 0.3469171387814413    Expected min: 0

f3 1 / 5

f3 2 / 5

f3 3 / 5

f3 4 / 5

f3 5 / 5

f3 --> Mean: 4.398467896436651    STD: 9.639486744002895    Expected min: 0

f5 1 / 5

f5 2 / 5

f5 3 / 5

f5 4 / 5

f5 5 / 5

f5 --> Mean: 0.0    STD: 0.0    Expected min: 0

f6 1 / 5

f6 2 / 5

f6 3 / 5

f6 4 / 5

f6 5 / 5

f6 --> Mean: 5.22    STD: 10.452349018282924    Expected min: 0

f7 1 / 5

f7 2 / 5

f7 3 / 5  
f7 4 / 5  
f7 5 / 5  
f7 --> Mean: 0.0009258111019656999    STD: 0.0008579346822992977    Expected min: 0  
Type Begin  
f8 1 / 5  
f8 2 / 5  
f8 3 / 5  
f8 4 / 5  
f8 5 / 5  
f8 --> Mean: -405.2042411582503    STD: 18.849481449898363    Expected min: -12569.5  
f9 1 / 5  
f9 2 / 5  
f9 3 / 5  
f9 4 / 5  
f9 5 / 5  
f9 --> Mean: 0.7954406778975947    STD: 0.6630645698884579    Expected min: 0

Second test [Alpha Increased]: move\_restriction = False, alpha = 0.50

Type Begin  
f1 1 / 5  
f1 2 / 5  
f1 3 / 5  
f1 4 / 5  
f1 5 / 5  
f1 --> Mean: 4.619742368412366    STD: 10.106013437387189    Expected min: 0  
f2 1 / 5  
f2 2 / 5  
f2 3 / 5  
f2 4 / 5  
f2 5 / 5  
f2 --> Mean: 0.3424607352697079    STD: 0.33227441626899823    Expected min: 0  
f3 1 / 5  
f3 2 / 5  
f3 3 / 5  
f3 4 / 5  
f3 5 / 5  
f3 --> Mean: 5.332849228137406    STD: 8.652767492819825    Expected min: 0  
f5 1 / 5  
f5 2 / 5  
f5 3 / 5

f5 4 / 5  
f5 5 / 5  
f5 --> Mean: 0.0 STD: 0.0 Expected min: 0  
f6 1 / 5  
f6 2 / 5  
f6 3 / 5  
f6 4 / 5  
f6 5 / 5  
f6 --> Mean: 6.02 STD: 11.289800706832695 Expected min: 0  
f7 1 / 5  
f7 2 / 5  
f7 3 / 5  
f7 4 / 5  
f7 5 / 5  
f7 --> Mean: 0.0009451994342463574 STD: 0.0007203362132429637 Expected min: 0  
Type Begin  
f8 1 / 5  
f8 2 / 5  
f8 3 / 5  
f8 4 / 5  
f8 5 / 5  
f8 --> Mean: -398.16843009496256 STD: 35.4144019913257 Expected min: -12569.5  
f9 1 / 5  
f9 2 / 5  
f9 3 / 5  
f9 4 / 5  
f9 5 / 5  
f9 --> Mean: 0.7200558988720727 STD: 0.808784866444068 Expected min: 0

Third test [Alpha Decreased]: move\_restriction = True, alpha = 0.10

Type Begin  
f1 1 / 5  
f1 2 / 5  
f1 3 / 5  
f1 4 / 5  
f1 5 / 5  
f1 --> Mean: 5.253634139416854 STD: 7.33252716535573 Expected min: 0  
f2 1 / 5  
f2 2 / 5  
f2 3 / 5  
f2 4 / 5  
f2 5 / 5

f2 --> Mean: 0.3461227674024942    STD: 0.35190630144014434    Expected min: 0  
 f3 1 / 5  
 f3 2 / 5  
 f3 3 / 5  
 f3 4 / 5  
 f3 5 / 5  
 f3 --> Mean: 4.86082994569671    STD: 9.578980449895367    Expected min: 0  
 f5 1 / 5  
 f5 2 / 5  
 f5 3 / 5  
 f5 4 / 5  
 f5 5 / 5  
 f5 --> Mean: 0.0    STD: 0.0    Expected min: 0  
 f6 1 / 5  
 f6 2 / 5  
 f6 3 / 5  
 f6 4 / 5  
 f6 5 / 5  
 f6 --> Mean: 4.24    STD: 6.0549483895405745    Expected min: 0  
 f7 1 / 5  
 f7 2 / 5  
 f7 3 / 5  
 f7 4 / 5  
 f7 5 / 5  
 f7 --> Mean: 0.0009055386832270415    STD: 0.0007456908160043751    Expected min: 0  
 Type Begin  
 f8 1 / 5  
 f8 2 / 5  
 f8 3 / 5  
 f8 4 / 5  
 f8 5 / 5  
 f8 --> Mean: -408.0492844172145    STD: 20.79488370078856    Expected min: -12569.5  
 f9 1 / 5  
 f9 2 / 5  
 f9 3 / 5  
 f9 4 / 5  
 f9 5 / 5  
 f9 --> Mean: 0.8549341635951809    STD: 0.8440996261869481    Expected min: 0

Fourth test [Move Restriction True]: move\_restriction = True, alpha = 0.25

Type Begin

f1 1 / 5  
f1 2 / 5  
f1 3 / 5  
f1 4 / 5  
f1 5 / 5  
f1 --> Mean: 4.541067202321007    STD: 8.565334595661803    Expected min: 0  
f2 1 / 5  
f2 2 / 5  
f2 3 / 5  
f2 4 / 5  
f2 5 / 5  
f2 --> Mean: 0.34956109359157755    STD: 0.2958266548577681    Expected min: 0  
f3 1 / 5  
f3 2 / 5  
f3 3 / 5  
f3 4 / 5  
f3 5 / 5  
f3 --> Mean: 7.0194159457769505    STD: 12.791660778043592    Expected min: 0  
f5 1 / 5  
f5 2 / 5  
f5 3 / 5  
f5 4 / 5  
f5 5 / 5  
f5 --> Mean: 0.0    STD: 0.0    Expected min: 0  
f6 1 / 5  
f6 2 / 5  
f6 3 / 5  
f6 4 / 5  
f6 5 / 5  
f6 --> Mean: 4.34    STD: 6.7278822819665915    Expected min: 0  
f7 1 / 5  
f7 2 / 5  
f7 3 / 5  
f7 4 / 5  
f7 5 / 5  
f7 --> Mean: 0.0009893942366814815    STD: 0.0007679200866013155    Expected min: 0  
Type Begin  
f8 1 / 5  
f8 2 / 5  
f8 3 / 5  
f8 4 / 5  
f8 5 / 5  
f8 --> Mean: -408.5167461332259    STD: 15.191733676849683    Expected min: -12569.5  
f9 1 / 5

f9 2 / 5

f9 3 / 5

f9 4 / 5

f9 5 / 5

f9 --> Mean: 0.7186045809773287    STD: 0.5376510050965286    Expected min: 0