

20/07/2023.

Analytical Questions.

Bharath

1. Find the no. of tokens in the following. SundaraRaman. J

int main()

192011038

{ int a=10, b=30;

if (a < b)

return(b);

else.

return(a);

3.

Tokens :-

'int': Keyword token.

'main': Identifier token.

'(' and ')': Parentheses tokens

'{' and '}': Curly brace tokens.

'int': Keyword token.

'a' and 'b': Identifier tokens.

'=': Assignment operator token.

'10' and '30': Constant tokens.

';': Semicolon token.

'if': Keyword token.

'<': Less than operator token

'return': keyword token.

'else': keyword token.

'a': Identifier token.

';': Semicolon token.

; Total no. of tokens

= 24 tokens.

2. Write a regular expression to denote set of all strings over $\{0, 1\}^*$ containing substring 101.

$$(011)^* \cdot 101 (011)^*$$

$\rightarrow (011)^*$: any sequence of 0's and 1's before substring.

$\rightarrow 101$: matches exact substring.

$\rightarrow (011)^*$: any sequence of 0's and 1's after substring.

3. Write a regular expression, that have at least two consecutive 0's (or) 1's;

$$(0, \{2, 3\} | \{2, 3\})$$

$\rightarrow (0, \{2, 3\})$: Matches two or more consecutive 0's.

$\rightarrow 1^*$: OR operator, want to match either of the conditions.

$\rightarrow (\{2, 3\})$: Matches two or more consecutive 1's.

$$H. \quad a = (b+c)^*(b+c)^*2;$$

Lexical Analysis :-

Identifies : a.

Assignment Operator : =

Left Parenthesis : (

Identifies : b.

Addition Operator : +

Identifies : c

Right Parenthesis :)

Multiplication Operator : *

Left Parenthesis : (

Identifies : b.

Addition Operator : +

Identifies : c

Right Parenthesis :)

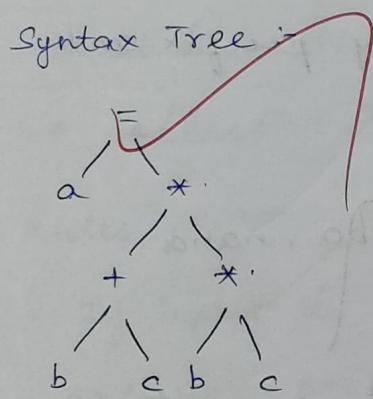
Multiplication operator : *

Constant : 2

Semicolon : ;

Syntax Analysis :-

Syntax Tree :-



Semantic Analysis :-

→ checks if the

variables and expressions
are valid and consistent.

Code optimization :-

→ common optimization.

techniques like constant.

folding, common subexpression.

elimination and strength.

reduction.

Intermediate.

Code Generation :-

$$t_1 = b + c$$

$$t_2 = t_1 * t_1$$

$$a = t_2 * 2$$

Code Generation :-

* The final step is to generate the machine code or assembly code from the optimized intermediate code.

Operation on Strings :-

1. Length of a string :- $s = 10101 \therefore |s| = 5$

2. Empty string :- $s = \emptyset, \epsilon = \emptyset$

3. prefix of string :- Any number of leading symbols in a string.
Let $s = abc$

prefix = \emptyset, abc, a, ab .

4. suffix of string :- Any number of tail symbols in a string.
Let $s = abc$

suffix = \emptyset, abc, c, bc .

5. Substring :- It is added by prefix and suffix.
Let $s = \text{Banana}$.

Substring = $\emptyset, \text{Banana}, ba, nana$

→ A set of string which is generated by alphabets are called languages.

Example :- $\Sigma = \{a, b\}$

$L = \{a, b, ab, ba, ab\dots\}$

Operation Expression on Languages :-

1) Union :-

$L = \{0, 1\} \quad M = \{00, 11\}$

$\therefore L \cup M = \{0, 1, 00, 11\}$

i) Concatenation :-

$$L = \{0, 1\} \quad M = \{00, 11\}$$

$$\therefore LM = \{000, 011, 100, 111\}$$

ii) Kleene closure :- (L^*).

$$E = \{a\}$$

$$\therefore E^* = E, a, aa$$

iii) Positive closure :- (L^+).

$$E = \{a\}$$

$$E^+ = a, aa$$

Recursive Descent parsing :-

→ It is a Top down parser.

→ collection of recursive procedure

Rules :-

- i) If input is non-terminal (upper-case) then.
call the procedure.
- ii) If the input is terminal (lower-case) then.
matched with input.
- iii) If non-terminal produce more than one
production. then all the production score.
should be return.

Example :-

$$E \rightarrow i E' \quad E' \rightarrow + i E' / \epsilon$$

↳ Derive.

E()

{

if (input == 'i').

input ++;

E PRIME();

}

E PRIME().

{

if (input == '+')

input ++;

if (input == 'i')

input ++;

E PRIME();

3.

else.

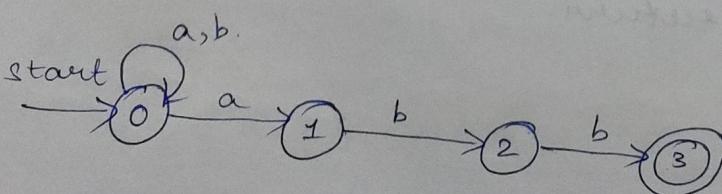
return.

3.

Non-Deterministic Finite Automata (NFA)

Find out the NFA of Regular Expression.

$(a+b)^* abb$.



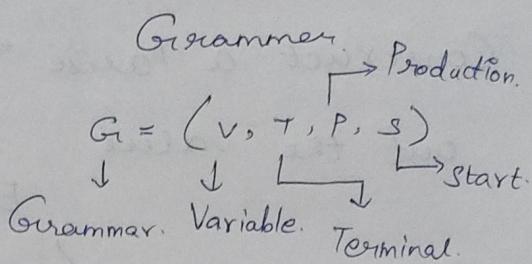
Context Free Grammar.

$$A_0 \rightarrow a A_0 \mid b A_0 \mid a A_1$$

$$A_1 \rightarrow b A_2$$

$$A_2 \rightarrow b A_3$$

$$A_3 \rightarrow \epsilon$$



$$F_2 \rightarrow F_2 + F_2$$

$$\left. \begin{array}{l} / \\ F_2 \times F_2 \end{array} \right\} 3 \text{ Production.}$$

$$\left. \begin{array}{l} / \\ \text{id.} \end{array} \right\} \therefore V = \{ E \} \rightarrow$$

it contains only

$$T = \{ +, *, \text{id.} \}$$

one variable.

on the left side.

$$So V = \{ E \}$$

$\text{id} + \text{id} * \text{id} \rightarrow$ Generate the string.

Left Most Derivation (LMD)

$$E \Rightarrow E + F_2$$

$$\Rightarrow \text{id} + F$$

$$\Rightarrow \text{id} + E * E$$

$$\Rightarrow \text{id} + \text{id} * E$$

$$\Rightarrow \text{id} + \text{id} * \text{id.}$$

Right Most Derivation (RMD)

$$F_2 \Rightarrow F_2 + E$$

$$\Rightarrow F_2 + E * F_2$$

$$\Rightarrow F + E * id.$$

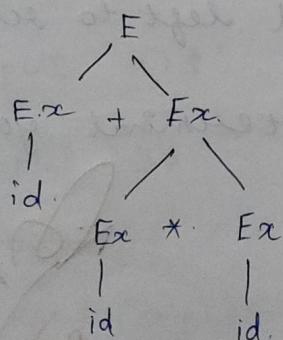
$$\Rightarrow E + id * id.$$

$$\Rightarrow id + id * id.$$

Parse Tree.

construct a parse tree for $\text{id} + \text{id} * \text{id}$. Parse.

Tree.



10/1/2023

Analytical Questions - 2

Q) Predictive parser.

$$S \rightarrow a \uparrow | (T) T \rightarrow T, S | S$$

$$\text{First}(S) = \{a, \uparrow, (\} \quad \text{Follow}(S) = \{,), \$\}$$

$$\text{First}(T) = \{a, \uparrow, (\} \quad \text{Follow}(T) = \{), \$\}$$

+-----+---+---+---+

| a | \uparrow | (|

+-----+---+---+---+

| S | $S \rightarrow a$ | $S \rightarrow \uparrow$ | $S \rightarrow (T)$ |

+-----+---+---+---+

| T | $T \rightarrow S, T$ | $T \rightarrow S$ | $T \rightarrow (T)$ |

+-----+---+---+---+

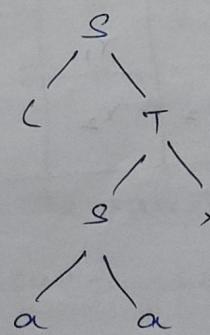
Q) Behaviour of the parser on the sentence.

Parsing steps :-

1. Stack. '\$'
2. Input '(a, a)\$'
3. Input 'a, a)\$'
4. Input ', a)\$'
5. Input 'a)\$'
6. Input ')\$'
7. Input '\$'
8. Input 'empty'

The parse tree.

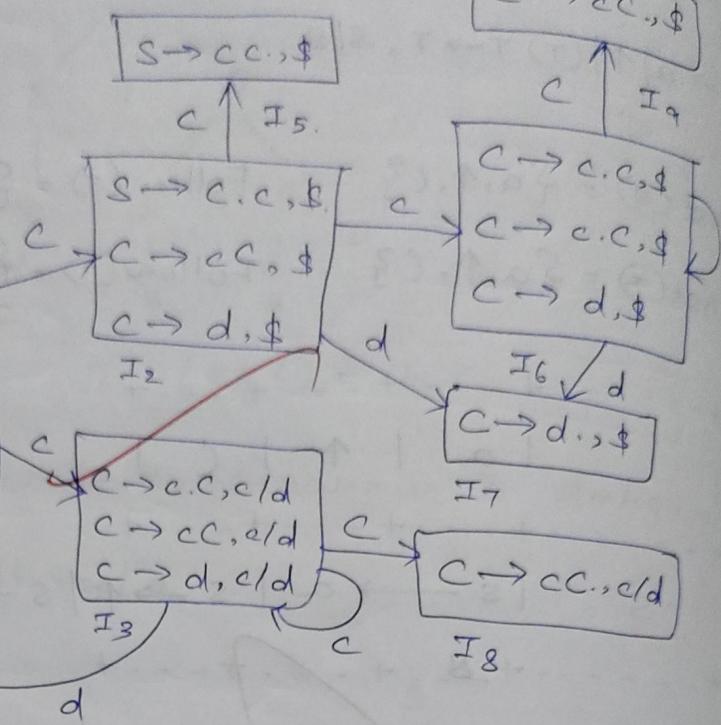
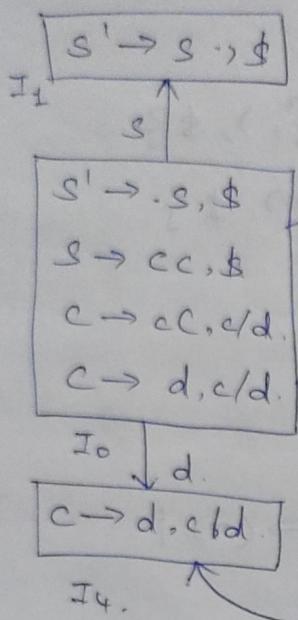
will be.



2. Construct SLR Parsing Table.

$S \rightarrow CC.$

$C \rightarrow cC \mid d.$



State.	ACTION.			GOTO.	
	c	d	\$	s	c
0	S_{36}	S_{47}		4	2
1			acc		
2	S_{36}	S_{47}			5
36	S_{36}	S_{47}			89
47	r_3	r_3	r_3		
5				r_1	
89	r_2	r_2	r_2		

3. Given Grammar :-

$$S \rightarrow AaAb \mid BbBa.$$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$

FOLLOW SETS :-

$$\text{FOLLOW}(S) = \{\$\}$$

$$\text{FOLLOW}(A) = \{a, b\}$$

$$\text{FOLLOW}(B) = \{a, b\}$$

FIRST sets :

$$\text{FIRST}(S) = \{a, b\}$$

$$\text{FIRST}(A) = \{\epsilon\}$$

$$\text{FIRST}(B) = \{\epsilon\}$$

Check. for LL(1) Conditions :-

i) No Two. Productions with.
the same left- Hand side.

ii) FIRST./ FOLLOW. sets conflict

$$\text{FIRST}(A) = \{\epsilon\} \text{ and } \text{FOLLOW}(S) = \{\$\}$$

$$\text{FIRST}(B) = \{\epsilon\} \text{ and } \text{FOLLOW}(S) = \{\$\}$$

3. Empty Productions :-

There are empty productions for A and B. However,

since they have distinct right-hand sides, they
do not cause conflicts.

∴ The given grammar is LL(1).

$$E \rightarrow 2E2.$$

$$E \rightarrow 3E3.$$

$$E \rightarrow A.$$

S : Shift.

R : Reduce.

Parsing Table

1 state. | 1 | 2 | 3 | 4 | 1

| 0 | S¹ | S² | S³ |

| 1 | S¹ | S² | S³ |

| 2 | R³ | R³ | R³ |

| 3 | R¹ | R¹ | R¹ |

∴ The parsing is

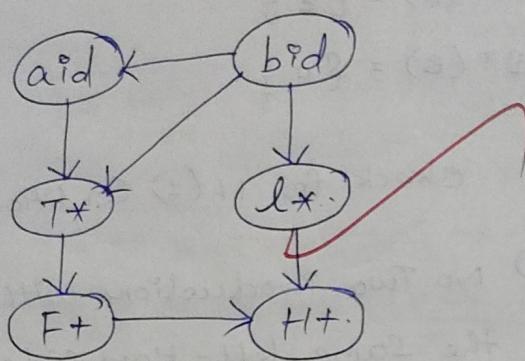
successful, and the

input string "32 423" is valid according to

the given grammar.

22/07/2023.

operator precedence.
flow graph.



Operator precedence
relation. function.

	id	*	*
F.			
T			2
l			1
A.	4		

Longest path.

aid \rightarrow T* \rightarrow F+ \rightarrow H+.

bid \rightarrow T* \rightarrow F+ \rightarrow H+.

bid \rightarrow aid \rightarrow T* \rightarrow F+ \rightarrow H+.

T* \rightarrow F+ \rightarrow H+.

l* \rightarrow H+.

bid. \rightarrow l* \rightarrow H+.

YACC \rightarrow Yet Another compiler compiler

Top Down Parser

\rightarrow This parser construct

from ~~group~~ root to.

leaves with non-terminal.

\rightarrow Top-Down Parser construct

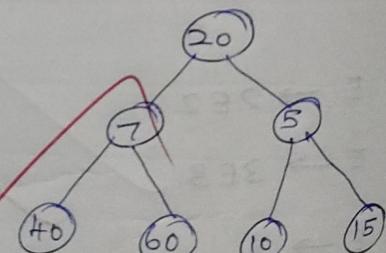
parse tree as output

(pre-order traversal)

20 \rightarrow 7 \rightarrow 40 \rightarrow 60

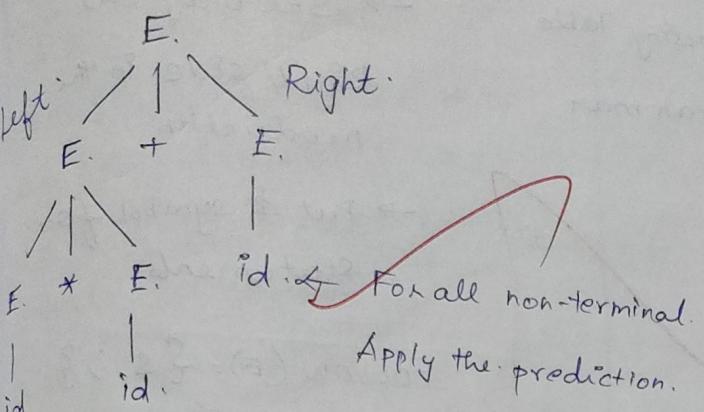
\rightarrow It gives us pre-ordered

traversal (Root, left, Right)

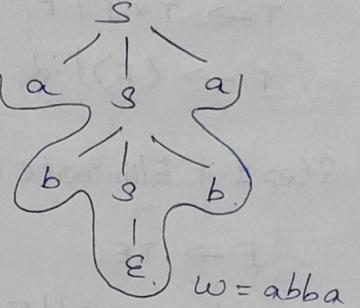


$$E \rightarrow E + E \mid E * E \mid \text{id}.$$

Eg :-



$$\begin{aligned} T &= \{ S \rightarrow aSa \} \\ S &\rightarrow bSb, \quad \left\{ \begin{array}{l} \text{Apply} \\ \text{with} \\ \text{word} \end{array} \right. \\ S &\rightarrow \epsilon \\ w &= abba. \end{aligned}$$

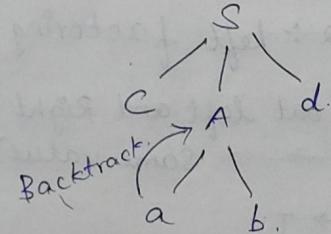
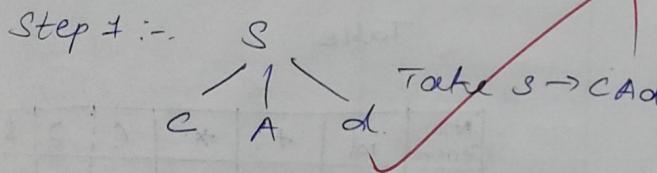


a) Backtracking. In. Top. Down. Parser.

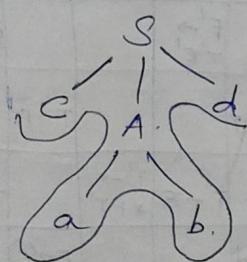
Construct the Grammar.

$$\begin{aligned} S &\rightarrow CAd. \\ A &\rightarrow ab \mid d \end{aligned} \quad \left\{ \begin{array}{l} \text{Apply with} \\ \text{word } w = cdd. \end{array} \right.$$

Step 1 :-



Step 2 :-



Now take

$$A \rightarrow \underline{ab}.$$

↓
First variable.

Now take the next alternative.

$$A \rightarrow ab \mid d.$$

↓

Next Alternative variable

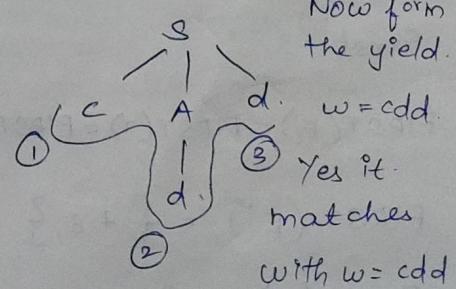
Step 3 :- Now Form. the yield

Step 5 :-

whether. it matches. $w = cdd$.

No it forms cabb., so we

backtrack.



Analytical Questions - 3.

1. SDT Scheme for $2 * (A+5)$.

Expression \rightarrow Term. { code = Term. code }

Term \rightarrow Factor. { code = Factor. code }

Term \rightarrow Term. '*' Factor. {

$t = \text{new-temporary-variable.}$

code = Term. code + Factor. code + t + '=' + Term. place
+ '*' + Factor. place + '\n'

place = t.

}

Factor \rightarrow Number { code = '' ; place = Number. value }

Factor \rightarrow '(' Expression. ')' { code = Expression. code ;
place = Expression. place }

Number \rightarrow [0-9] + { value = parseInt(\$#) }

Q. Expression : $3 * 5 + 6 * 3$.

1. For $F \rightarrow \text{num}(\text{num}, \text{val} = 3)$:

$$F \cdot \text{val} = 3.$$

2. For $F \rightarrow \text{num}(\text{num}, \text{val} = 5)$:

$$F \cdot \text{val} = 5.$$

3. For $T \rightarrow F$:

$$T \cdot \text{val} = F \cdot \text{val} = 5.$$

4. For $F \rightarrow \text{num}(\text{num}, \text{val} = 6)$:

$$F \cdot \text{val} = 6.$$

5. For $F \rightarrow \text{num}(\text{num}, \text{val} = 3)$:

$$F \cdot \text{val} = 3.$$

6. For $T \rightarrow F$:

$$E \cdot \text{val} = T \cdot \text{val} =$$

Stack : $\{\$ \}$, Input : "n+n\$"

Stack : $\{n\}$, Input : "+n\$".

Stack : $\{n, +\}$, Input : "n\$".

Stack : $\{E\}$, Input : "n\$"

Stack : $\{E'\}$, Input : "\$"

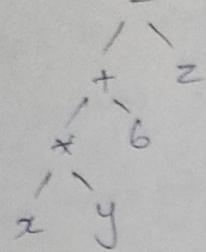
Final Configuration

Stack : $\{E'\}$.

Input : "\$"

Action : Parsing completed successfully.

H. Syntax Tree :-



5. LR Parsing :-

Stack : [0].

Input : 5 * 3 + 2 ; \$

Action : Shift.

Stack : [0, 5]

Input : * 3 + 2 ; \$

Action : Reduce.

Stack : [0, 3]

Input : * 3 + 2 ; \$

Action : Shift.

Stack : [0, 3, 6].

Input : 3 + 2 ; \$

Action : Shift.

Stack : [0, 3, 6, 3]

Input : + 2 ; \$

Action : Reduce.

Stack : [0, 3, 6, 3, 4]

Input : + 2 ; \$

Action : Reduce

Stack : [0, 3, 6, 2]

Input : + 2 ; \$

Action : Shift.

Stack : [0, 3, 6, 2, 7]

Input : . 2 ; \$

Action : Shift.

Stack : [0, 10]

Input : \$

Action : Reduce.

∴ The string is
accepted

24/07/2023

Operator Precedence :-

→ Bottom up parsing.

→ class of Grammars.

The properties are no two variables are adjacent.

No E production.

id - highest precedence. when compared with all the operators.

\$ - Lowest precedence. when compared with all the operators.

Using the Grammar. $E \rightarrow E + E \mid E * E \mid id$.

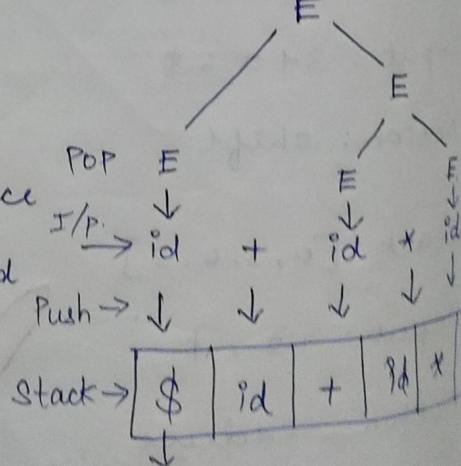
Form a operator precedence table.

	id	+	*	\$
id	-	>	>	>
+	<	>	<	>
*	<	>	>	>
\$	<	<	<	-

} Top of the Stack < Input String P
 } Top of the Stack > Input String P

Using the operator precedence table parse the assumed input.

Input = id + id * id \$



→ Whenever the top of the stack.

is less than or equal in the.

Input string then you have to PUSH.

procedure :-

Step 1 :- Compare \$ and id. in the op. precedence table.
It shows \prec so push id inside the stack.

Now increment the pointer.

It goes to + .

Step 2 :- Now compare id and + in the table.

It shows \succ so pop id out of the stack and.

reduce the pointer, so the pointer goes to id.

again since it is popped.

Step 3 :- Now compare \$ and + it shows \prec in the table., so push + inside the stack, now increment the pointer, it goes to id.

Step 4 :- Now compare + and id , it shows \prec ,
so push id inside the stack., Now increment.
the pointer it goes to *.

Step 5 :- Now compare id and *., it shows \succ in the table., so pop id out of the stack and reduce the pointer, Pt moves to +.

Step 6 :- Now compare + and id., it shows \prec symbol in the table., so push * inside the stack., now increment the pointer, it moves to id.

Step 7 :- Now compare * and id., it shows \prec in the table , so push id inside the stack, and increment the pointer, it moves to \$.

Analytical Topic - 4.

1. $-(a+b)^*(c+d)^* + (a+b+c)$.

Quadruples :-

$$\text{Quadruple. 1 : } t_4 = a+b.$$

$$t_2 = -t_4.$$

$$t_3 = c+d.$$

$$t_4 = t_2 * t_3$$

$$t_5 = a+b.$$

$$t_6 = t_5 + c.$$

$$t_7 = t_4 + t_6.$$

Triples :-

$$t_1 = a+b.$$

$$t_2 = -t_1.$$

$$t_3 = c+d.$$

$$t_4 = t_2 * t_3$$

$$t_5 = a+b.$$

$$t_6 = t_5 + c$$

$$t_7 = t_6 + t_4.$$

Indirect
Triples :-

$$* t_1 = a+b$$

$$* t_2 = -* t_1$$

$$* t_3 = c+d$$

$$* t_4 = * t_2 *$$

$$* t_5 = a+b$$

$$* t_6 = * t_5 + c$$

$$* t_7 = * t_6 + c$$

2. $a^* - (b+c)$.

Quadruples :-

$$t_1 = b+c.$$

$$t_2 = -t_1.$$

$$t_3 = a^* t_2.$$

Postfix :-

$$abc + - *$$

Three-Address

Code :-

$$t_1 = b+c$$

$$t_2 = -t_1$$

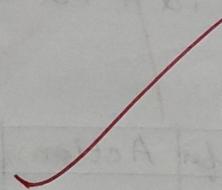
$$t_3 = a^* t_2.$$

3. Translation scheme :-

$$t_1 := a+b.$$

$$t_2 := c*d.$$

$$g := t_1 - t_2.$$



Result three-address

code.

$$t_1 = a+b$$

$$t_2 = c*d$$

$$g = t_1 - t_2.$$

H. Resulting three-address code. using backpatching :-

if ($a < b$) goto L4.

L2 : $t_3 = t_1$ and t_2 .

$t_1 = 1$.

goto L2.

L4 : $t_4 = 0$.

if ($c < d$) goto L3.

$t_2 = 1$.

goto L2.

L3 : $t_2 = 0$.

25/01/23

25/01/2023.

SYNTAX DIRECT TRANSLATION (SDT) :-

Context free Grammar.

(Semantic Action)

For Declaration.

(Production Rule).

P \rightarrow D.

{ Enter (id.name, T.type,
offset = offset + T.width)}

D \rightarrow D . D.

{ T.Type = integer
T.width = 4 }

D \rightarrow id. T

T \rightarrow integer.

{ T.Type = real.

T \rightarrow real.

T.width = 8 }

T \rightarrow array [num] of T.

{ T.Type = array (num val,
T.type) }

T \rightarrow \uparrow T,

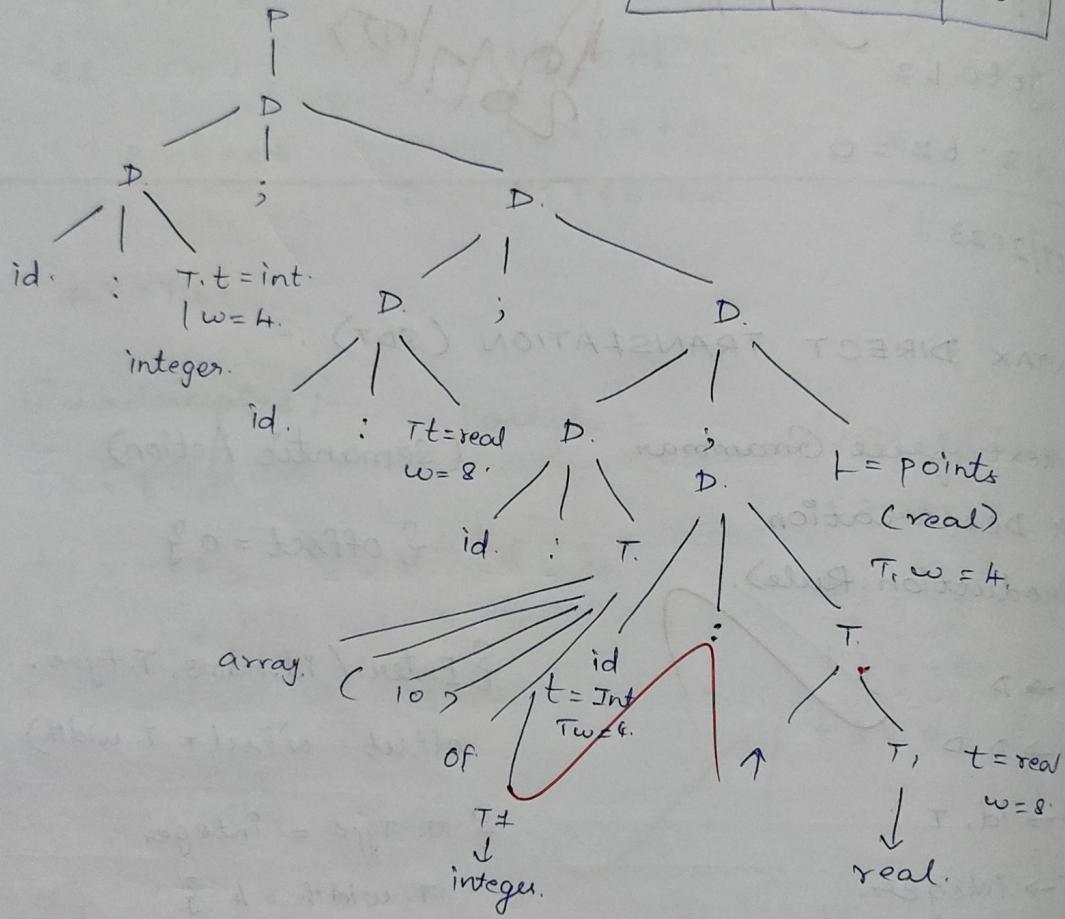
T.width = num.val * T.
width.)

Grammars

{ a: integer
 b: real.
 c: array [10] of integer
 d: T real.

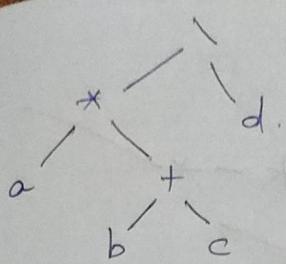
3.

Parse Tree.



INTERMEDIATE CODE GENERATION.

- SYNTAX TREE. → The root node represents operator
 $a * (b + c) / d$
 ↗ leaf node represents operand
 Eg.: construct a syntax tree
 for the following grammar
- Brackets as the highest priority
- Then the operators as the second priority



Post-fix expression :-

$$\text{i)} (a+b)*c \rightarrow abc+*$$

$$\text{ii)} a+(b*c) \rightarrow abc+*$$

$$\text{iii)} (a-b)*(c/d) \rightarrow ab-cd/*$$

Three-address code :-

Condition :-

- i) each instruction should contain three address
- ii) one operator on right side, example :-

Using the grammar. $a = b * - c + b * - c$

Find out the three address code representation

having :- a) quadruples b) Triples c) Indirect Triples.

Four fields.

operator,

argument 1 ,

argument 2 ,

result .

$$t_4 = -c$$

$$t_2 = b * t_4$$

$$t_3 = -c$$

$$t_4 = b * t_3$$

$$t_5 = t_2 + t_4$$

b) TRIPLE.

	operator	Arg1	Arg2
$t_4(0)$	-	c	
$t_2(1)$	*	b	$(0)t_4$
$t_3(2)$	-	c	
$t_4(3)$	*	b	$(2)t_3$
$t_5(4)$	+	(1)	$(3)t_4$

	OP	arg1(i)	arg2(j)	Res
(0)	-	c		t_4 .
(1)	*	b	t_4	t_2 .
(2)	-	c		t_3 .
(3)	*	b	t_3	t_4 .
(4)	+	t_2	t_4	t_5 .

c) INDIRECT TRIPLE.

	statement	OP	arg1	arg2
(0)	100	-	c	
(1)	101	*	b	(100).
(2)	102	-	c	
(3)	103	*	b	(102)
(4)	104	+	100	(103)

25/07/2023.

Analytical Topic - 5

i). Directed Acyclic Graph :- (DAG)

b c

+

|

a

|

x

|

t₂

|

a

|

+

|

b

|

x

|

c

|

+

|

t₂

|

(+)

|

a

|

(+)

|

a

|

a

→ In the DAG, each node represents an operation, and the arrows indicate the flow of data from one operation to another.

(ii) $+ \rightarrow I = Y$.

|

|

$+ \rightarrow T4 = 4 \times I$.

$PROD = 0 \rightarrow T2 = \text{addr}(A) - 4 \rightarrow T3 = T2[1]$
 $+ \rightarrow T4 = 4 \times I \rightarrow T6 = T3[1]$
 $+ \rightarrow \text{IF } I < 20 \text{ GOTO } (5) \rightarrow T4 = \text{addr}(B) - 4 \rightarrow T6 = T3[1]$

$| \quad | \quad PROD = PROD + T6$

Basic Block 1.

Basic Block 2.

Basic Block 3

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

|

(iii). Three address code.

LOAD R4, [A-ADDR]

ADD R7, R6, R5

LOAD R2, [B-ADDR]

STORE RT, [W-ADDR]

LOAD R3, [C-ADDR]

ADD RH, R4, R2

ADD R5, R4, R3

ADD R6, RH, R5

iv). Construct Basic Blocks.

Basic Block 1 :-

$$\text{PROD} = 0.$$

$$I = 4.$$

Basic Block 2 :-

$$T_2 = \text{addr}(A) - 4.$$

$$T_4 = \text{addr}(B) - 4.$$

$$T_4 = 4 \times I.$$

Basic Block 3 :-

$$T_3 = T_2[T_4].$$

$$T_5 = T_4[T_4].$$

$$T_6 = T_3 \times T_5.$$

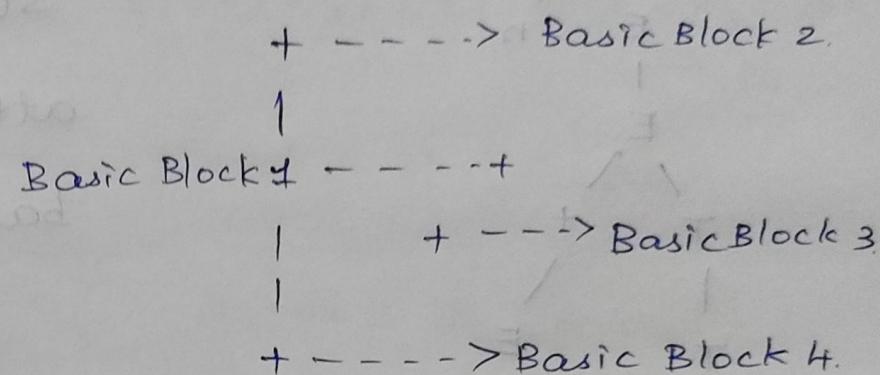
$$\text{PROD} = \text{PROD} + T_6$$

$$I = I + 4.$$

Basic Block 4 :-

$$\text{IF } I <= 20 \text{ GOTO } (5)$$

Flow Graph :-



Loop Invariant Statements :-

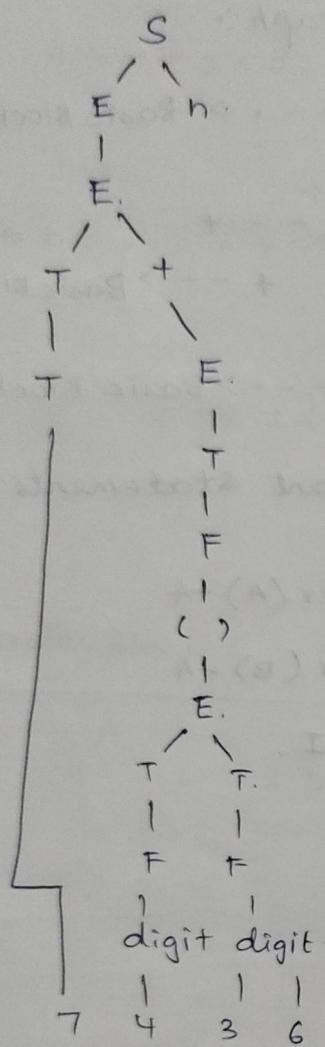
$$T_2 = \text{addr}(A) - 4.$$

$$T_4 = \text{addr}(B) - 4.$$

$$T_4 = 4 \times I.$$

Analytical Question.

1. Step 1 :- Tokenize the expression and build the parse tree.



Step 2 :- Evaluate the attributes for each node based on the SDD rules

$$F.\text{attr} = 7$$

$$F.\text{attr} = 4,$$

$$T.\text{attr} = F.\text{attr} = 4$$

$$F.\text{attr} = 3.$$

$$F.\text{attr} = 6.$$

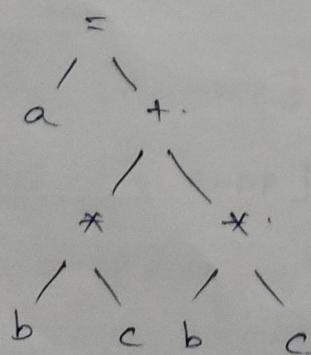
$$T.\text{attr} = F.\text{attr} = 6$$

$$E.\text{attr} = T.\text{attr} = 6$$

$$T.\text{attr} = F.\text{attr} = 10.$$

$$E.\text{attr} = E.\text{attr} + T.\text{attr}$$

2. Syntax Tree :-



$$3. E.\text{val} = 5. (\text{digit}).$$

$$F.\text{val} = 5. (E.\text{val})$$

$$T.\text{val} = 5. (F.\text{val})$$

$$E.\text{val} = 5. (T.\text{val})$$

$$E.\text{val} = 6. (\text{digit})$$

$$F.\text{val} = 6. (E.\text{val})$$

$$T.\text{val} = 6. (F.\text{val})$$

$$E.\text{val} = 6. (T.\text{val})$$

$$T.\text{val} = 5. (T.\text{val}) * 6. (F.\text{val}) \\ = 30.$$

$$T.\text{val} = 30. (T.\text{val})$$

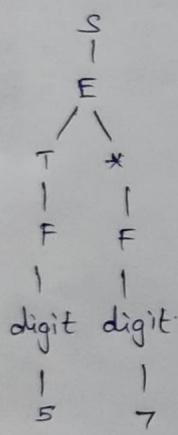
$$E.\text{val} = 30. (E.\text{val}) + 4. (T.\text{val}) \\ = 34.$$

$$E.\text{val} = 34. (E.\text{val}).$$

$$S.\text{val} = 34. (E.\text{val}).$$

4. Input: '5*7'

Parse Tree :-



$$E.\text{postfix} = T.\text{postfix} = F.\text{postfix} = \\ \text{digit.lexeme} = 5$$

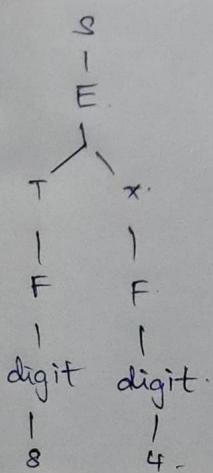
$$T.\text{postfix} = F.\text{postfix} + " " + \text{digit.lexeme} = 5 \\ + " * " = 5 " " + 7 + " * " = " 57* "$$

$$E.\text{postfix} = T.\text{postfix} = " 57* "$$

$$S.\text{postfix} = E.\text{postfix} = " 57* "$$

Input : "8*4"

Parse Tree :-



$$E.\text{postfix} = T.\text{postfix} = F.\text{postfix} = \\ \text{digit.lexeme} = 8.$$

$$T.\text{postfix} = F.\text{postfix} + " " + \text{digit.lexeme} \\ + " * " = 8 + " " + 4 + " * " = " 84* "$$

$$E.\text{postfix} = T.\text{postfix} = " 84* "$$

$$S.\text{postfix} = E.\text{postfix} = " 84* "$$