

Leetcode problem no. 221

Link- (<https://leetcode.com/problems/maximal-square/description/>)

Problem Description:

Given an $m \times n$ binary matrix filled with 0's and 1's, *find the largest square containing only 1's and return its area.*

Example 1:

Input: matrix =

```
[["1","0","1","0","0"],["1","0","1","1","1"],["1","1","1","1","1"],["1","0","0","1","0"]]
```

Output: 4

Intuition:

We want the **largest square of all 1s** in a binary matrix.

Instead of the classic DP approach, this code uses a **binary search on side length x**:

1. Preprocessing with prefix row sums (prefRow)

- For each row, store prefix sums so that we can quickly check how many 1s are in any segment of that row.
- This allows us to test if a row segment of length x is all 1s in $O(1)$ time.

2. Binary search over possible square sizes

- Low = 1, High = min(rows, cols).

- b. For each candidate size x , scan all possible $x \times x$ submatrices.
- c. For each row in that square, check if the entire segment of length x is all 1s using prefix sums.
- d. If every row inside this square has all 1s, then this size works (here = true).
- e. If some square of size x exists, we move low up (try bigger squares); otherwise, shrink high.

3. Final Answer

- a. ans keeps track of the largest side length found, and we return $\text{ans} * \text{ans}$ as the maximum area.

So the approach is: **binary search the side length \rightarrow verify squares using row prefix sums.**

Code:

```
class Solution {
public int maximalSquare(char[][] matrix) {
    int rl = matrix.length;
    int cl = matrix[0].length;
    int n = Math.min(matrix.length, matrix[0].length);
    int[][] prefRow = new int[rl][cl];
    for(int i=0; i<rl; i++){
        int sum = 0;
        for(int j=0; j<cl; j++){
            sum += (matrix[i][j] - '0');
            prefRow[i][j] = sum;
        }
    }
    int low = 1;
    int ans = 0;
    int high = n;
    while(low <= high){
        int x = (low + high) / 2;
        boolean here = false;
        for(int i=0; i<=rl-x; i++){
            for(int j=0; j<=cl-x; j++){
                boolean found = false;
                int sr = i;
```

```

int er = i+x-1;
int sc = j;
int ec = j+x-1;
for(int k=sr;k<=er;k++){
if(prefRow[k][ec]-prefRow[k][sc]+(matrix[k][sc]-'0')!=x){
found = true;
break;
}
}
if(!found) {
here = true;
break;
}
}
if(here) break;
}
if(here){
low = x+1;
ans = x;
}else{
high = x-1;
}
}
return ans*ans;
}
}

```

Time Complexity:

$O(n*m*\log(\min(m,n)))$

Space Complexity:

$O(nm)$

Best Time Complexity:

$O(nm)$

Best space complexity:

$O(nm)$