Wyznaczanie tabeli liczności krok po kroku

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Opis zbioru danych

Za przykład posłuży zbiór danych *contact lenses*¹. Zawiera on cztery atrybuty (tyle samo powstanie tabelek liczności):

• age: young, pre-presbyopic, presbyopic,

• spectacle-prescip: myope, hypermetrope,

• astigmatism: no, yes,

• tear-prod-rate: reduced, normal,

oraz klasę decyzyjną **contact-lenses** przyjmującą wartości: *soft*, *hard*, *none*. Liczba próbek wynosi 24.

Tabela: Liczność poszczególnych klas.

soft	5
hard	4
none	15

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

$$\#(\mathbf{age} = young \land \mathbf{contact} - \mathbf{lenses} = soft) = 2$$

	soft	hard	none
young	2		
pre-presbyopic			
presby opic			

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

$$\#(\mathbf{age} = young \land \mathbf{contact} - \mathbf{lenses} = hard) = 2$$

	soft	hard	none
young	2	2	
pre-presbyopic			
presby opic			

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

$$\#(\mathbf{age} = young \land \mathbf{contact} - \mathbf{lenses} = none) = 4$$

	soft	hard	none
young	2	2	4
pre-presbyopic			
presby opic			

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

$$\#(\mathbf{age} = pre\text{-}presbyopic \land \mathbf{contact}\text{-}\mathbf{lenses} = soft) = 2$$

	soft	hard	none
young	2	2	4
$pre ext{-}presbyopic$	2		
presby opic			

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

 $\#(\mathbf{age} = pre\text{-}presbyopic \land \mathbf{contact}\text{-}\mathbf{lenses} = hard) = 1$

	soft	hard	none
young	2	2	4
pre-presbyopic	2	1	
presby opic			

1	Troung.	nono	9	nuo nuoshvonia	nono	17	nuochronia	none
1	young	none	9	pre-presbyopic	none	11	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

 $\#(\mathbf{age} = pre - presbyopic \land \mathbf{contact} - \mathbf{lenses} = none) = 5$

	soft	hard	none
young	2	2	4
pre-presbyopic	2	1	5
presby opic			

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

 $\#(\mathbf{age} = presbyopic \land \mathbf{contact} - \mathbf{lenses} = soft) = 1$

	soft	hard	none
young	2	2	4
pre-presbyopic	2	1	5
presby opic	1		

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

$\#(\mathbf{age} = presbyopic \land \mathbf{contact} - \mathbf{lenses} = hard) = 1$

	soft	hard	none
young	2	2	4
pre-presbyopic	2	1	5
presby opic	1	1	

1	young	none	9	pre-presbyopic	none	17	presbyopic	none
2	young	soft	10	pre-presbyopic	soft	18	presbyopic	none
3	young	none	11	pre-presbyopic	none	19	presbyopic	none
4	young	hard	12	pre-presbyopic	hard	20	presbyopic	hard
5	young	none	13	pre-presbyopic	none	21	presbyopic	none
6	young	soft	14	pre-presbyopic	soft	22	presbyopic	soft
7	young	none	15	pre-presbyopic	none	23	presbyopic	none
8	young	hard	16	pre-presbyopic	none	24	presbyopic	none

$$\#(\mathbf{age} = presbyopic \land \mathbf{contact} - \mathbf{lenses} = none) = 6$$

	soft	hard	none
young	2	2	4
pre-presbyopic	2	1	5
presby opic	1	1	6

1	myope	none	9	myope	none	17	myope	none
2	myope	soft	10	myope	soft	18	myope	none
3	myope	none	11	myope	none	19	myope	none
4	myope	hard	12	myope	hard	20	myope	hard
5	hypermetrope	none	13	hypermetrope	none	21	hypermetrope	none
6	hypermetrope	soft	14	hypermetrope	soft	22	hypermetrope	soft
7	hypermetrope	none	15	hypermetrope	none	23	hypermetrope	none
8	hypermetrope	hard	16	hypermetrope	none	24	hypermetrope	none

$\#(\mathbf{spectacle} - \mathbf{prescrip} = myope \land \mathbf{contact} - \mathbf{lenses} = soft) = 2$

	soft	hard	none
myope	2		
hypermetrope			

1	myope	none	9	myope	none	17	myope	none
2	myope	soft	10	myope	soft	18	myope	none
3	myope	none	11	myope	none	19	myope	none
4	myope	hard	12	myope	hard	20	myope	hard
5	hypermetrope	none	13	hypermetrope	none	21	hypermetrope	none
6	hypermetrope	soft	14	hypermetrope	soft	22	hypermetrope	soft
7	hypermetrope	none	15	hypermetrope	none	23	hypermetrope	none
8	hypermetrope	hard	16	hypermetrope	none	24	hypermetrope	none

 $\#(\mathbf{spectacle} - \mathbf{prescrip} = myope \land \mathbf{contact} - \mathbf{lenses} = hard) = 3$

	soft	hard	none
myope	2	3	
hypermetrope			

1	myope	none	9	myope	none	17	myope	none
2	myope	soft	10	myope	soft	18	myope	none
3	myope	none	11	myope	none	19	myope	none
4	myope	hard	12	myope	hard	20	myope	hard
5	hypermetrope	none	13	hypermetrope	none	21	hypermetrope	none
6	hypermetrope	soft	14	hypermetrope	soft	22	hypermetrope	soft
7	hypermetrope	none	15	hypermetrope	none	23	hypermetrope	none
8	hypermetrope	hard	16	hypermetrope	none	24	hypermetrope	none

 $\#(\mathbf{spectacle}\text{-}\mathbf{prescrip}=myope \land \mathbf{contact}\text{-}\mathbf{lenses}=none)=7$

	soft	hard	none
myope	2	3	7
hypermetrope			

1	myope	none	9	myope	none	17	myope	none
2	myope	soft	10	myope	soft	18	myope	none
3	myope	none	11	myope	none	19	myope	none
4	myope	hard	12	myope	hard	20	myope	hard
5	hypermetrope	none	13	hypermetrope	none	21	hypermetrope	none
6	hypermetrope	soft	14	hypermetrope	soft	22	hypermetrope	soft
7	hypermetrope	none	15	hypermetrope	none	23	hypermetrope	none
8	hypermetrope	hard	16	hypermetrope	none	24	hypermetrope	none

 $\#(\mathbf{spectacle\text{-}prescrip} = hypermetrope \land \mathbf{contact\text{-}lenses} = soft) = 3$

	soft	hard	none
myope	2	3	7
hypermetrope	3		

1	myope	none	9	myope	none	17	myope	none
2	myope	soft	10	myope	soft	18	myope	none
3	myope	none	11	myope	none	19	myope	none
4	myope	hard	12	myope	hard	20	myope	hard
5	hypermetrope	none	13	hypermetrope	none	21	hypermetrope	none
6	hypermetrope	soft	14	hypermetrope	soft	22	hypermetrope	soft
7	hypermetrope	none	15	hypermetrope	none	23	hypermetrope	none
8	hypermetrope	hard	16	hypermetrope	none	24	hypermetrope	none

 $\#(\mathbf{spectacle\text{-}prescrip} = hypermetrope \land \mathbf{contact\text{-}lenses} = hard) = 1$

	soft	hard	none
myope	2	3	7
hypermetrope	3	1	

1	myope	none	9	myope	none	17	myope	none
2	myope	soft	10	myope	soft	18	myope	none
3	myope	none	11	myope	none	19	myope	none
4	myope	hard	12	myope	hard	20	myope	hard
5	hypermetrope	none	13	hypermetrope	none	21	hypermetrope	none
6	hypermetrope	soft	14	hypermetrope	soft	22	hypermetrope	soft
7	hypermetrope	none	15	hypermetrope	none	23	hypermetrope	none
8	hypermetrope	hard	16	hypermetrope	none	24	hypermetrope	none

 $\#(\mathbf{spectacle\text{-}prescrip} = hypermetrope \land \mathbf{contact\text{-}lenses} = none) = 8$

	soft	hard	none
myope	2	3	7
hypermetrope	3	1	8

1	no	none	9	no	none	17	no	none
2	no	soft	10	no	\mathbf{soft}	18	no	none
3	yes	none	11	yes	none	19	yes	none
4	yes	hard	12	yes	hard	20	yes	hard
5	no	none	13	no	none	21	no	none
6	no	soft	14	no	soft	22	no	soft
7	yes	none	15	yes	none	23	yes	none
8	yes	hard	16	yes	none	24	yes	none

 $\#(astigmatism = no \land contact-lenses = soft) = 5$

	soft	hard	none
no	5		
yes			

1	no	none	9	no	none	17	no	none
2	no	soft	10	no	soft	18	no	none
3	yes	none	11	yes	none	19	yes	none
4	yes	hard	12	yes	hard	20	yes	hard
5	no	none	13	no	none	21	no	none
6	no	soft	14	no	soft	22	no	soft
7	yes	none	15	yes	none	23	yes	none
8	yes	hard	16	yes	none	24	yes	none

 $\#(astigmatism=no \land contact-lenses=hard)=0$

	soft	hard	none
no	5	0	
yes			

1	no	none	9	no	none	17	no	none
2	no	soft	10	no	soft	18	no	none
3	yes	none	11	yes	none	19	yes	none
4	yes	hard	12	yes	hard	20	yes	hard
5	no	none	13	no	none	21	no	none
6	no	soft	14	no	soft	22	no	soft
7	yes	none	15	yes	none	23	yes	none
8	yes	hard	16	yes	none	24	yes	none

 $\#(astigmatism = no \land contact-lenses = none) = 7$

	soft	hard	none
no	5	0	7
yes			

1	no	none	9	no	none	17	no	none
2	no	soft	10	no	soft	18	no	none
3	yes	none	11	yes	none	19	yes	none
4	yes	hard	12	yes	hard	20	yes	hard
5	no	none	13	no	none	21	no	none
6	no	soft	14	no	soft	22	no	soft
7	yes	none	15	yes	none	23	yes	none
8	yes	hard	16	yes	none	24	yes	none

 $\#(astigmatism = yes \land contact-lenses = soft) = 0$

	soft	hard	none
no	5	0	7
yes	0		

1	no	none	9	no	none	17	no	none
2	no	soft	10	no	soft	18	no	none
3	yes	none	11	yes	none	19	yes	none
4	yes	hard	12	yes	hard	20	yes	hard
5	no	none	13	no	none	21	no	none
6	no	soft	14	no	soft	22	no	soft
7	yes	none	15	yes	none	23	yes	none
8	yes	hard	16	yes	none	24	yes	none

 $\#(astigmatism = yes \land contact-lenses = hard) = 4$

	soft	hard	none
no	5	0	7
yes	0	4	

1	no	none	9	no	none	17	no	none
2	no	soft	10	no	soft	18	no	none
3	yes	none	11	yes	none	19	yes	none
4	yes	hard	12	yes	hard	20	yes	hard
5	no	none	13	no	none	21	no	none
6	no	soft	14	no	soft	22	no	soft
7	yes	none	15	yes	none	23	yes	none
8	yes	hard	16	yes	none	24	yes	none

 $\#(\mathbf{astigmatism} = yes \land \mathbf{contact} - \mathbf{lenses} = none) = 8$

	soft	hard	none
no	5	0	7
yes	0	4	8

1	reduced	none	9	reduced	none	17	reduced	none
2	normal	soft	10	normal	soft	18	normal	none
3	reduced	none	11	reduced	none	19	reduced	none
4	normal	hard	12	normal	hard	20	normal	hard
5	reduced	none	13	reduced	none	21	reduced	none
6	normal	soft	14	normal	soft	22	normal	soft
7	reduced	none	15	reduced	none	23	reduced	none
8	normal	hard	16	normal	none	24	normal	none

 $\#(\mathbf{tear\text{-}prod\text{-}rate} = \mathit{reduced} \land \mathbf{contact\text{-}lenses} = \mathit{soft}) = 0$

	soft	hard	none
reduced	0		
normal			

1	reduced	none	9	reduced	none	17	reduced	none
2	normal	soft	10	normal	soft	18	normal	none
3	reduced	none	11	reduced	none	19	reduced	none
4	normal	hard	12	normal	hard	20	normal	hard
5	reduced	none	13	reduced	none	21	reduced	none
6	normal	soft	14	normal	soft	22	normal	soft
7	reduced	none	15	reduced	none	23	reduced	none
8	normal	hard	16	normal	none	24	normal	none

 $\#(\mathbf{tear\text{-}prod\text{-}rate} = reduced \land \mathbf{contact\text{-}lenses} = hard) = 0$

	soft	hard	none
reduced	0	0	
normal			

1	reduced	none	9	reduced	none	17	reduced	none
2	normal	soft	10	normal	soft	18	normal	none
3	reduced	none	11	reduced	none	19	reduced	none
4	normal	hard	12	normal	hard	20	normal	hard
5	reduced	none	13	reduced	none	21	reduced	none
6	normal	soft	14	normal	soft	22	normal	soft
7	reduced	none	15	reduced	none	23	reduced	none
8	normal	hard	16	normal	none	24	normal	none

 $\#(\mathbf{tear\text{-}prod\text{-}rate} = reduced \land \mathbf{contact\text{-}lenses} = none) = 12$

	soft	hard	none
reduced	0	0	12
normal			

1	reduced	none	9	reduced	none	17	reduced	none
2	normal	soft	10	normal	soft	18	normal	none
3	reduced	none	11	reduced	none	19	reduced	none
4	normal	hard	12	normal	hard	20	normal	hard
5	reduced	none	13	reduced	none	21	reduced	none
6	normal	soft	14	normal	soft	22	normal	\mathbf{soft}
7	reduced	none	15	reduced	none	23	reduced	none
8	normal	hard	16	normal	none	24	normal	none

 $\#(\mathbf{tear\text{-}prod\text{-}rate} = normal \land \mathbf{contact\text{-}lenses} = soft) = 5$

	soft	hard	none
reduced	0	0	12
normal	5		

1	reduced	none	9	reduced	none	17	reduced	none
2	normal	soft	10	normal	soft	18	normal	none
3	reduced	none	11	reduced	none	19	reduced	none
4	normal	hard	12	normal	hard	20	normal	hard
5	reduced	none	13	reduced	none	21	reduced	none
6	normal	soft	14	normal	soft	22	normal	soft
7	reduced	none	15	reduced	none	23	reduced	none
8	normal	hard	16	normal	none	24	normal	none

$\#(\mathbf{tear\text{-}prod\text{-}rate} = normal \land \mathbf{contact\text{-}lenses} = hard) = 4$

	soft	hard	none
reduced	0	0	12
normal	5	4	

1	reduced	none	9	reduced	none	17	reduced	none
2	normal	soft	10	normal	soft	18	normal	none
3	reduced	none	11	reduced	none	19	reduced	none
4	normal	hard	12	normal	hard	20	normal	hard
5	reduced	none	13	reduced	none	21	reduced	none
6	normal	soft	14	normal	soft	22	normal	soft
7	reduced	none	15	reduced	none	23	reduced	none
8	normal	hard	16	normal	none	24	normal	none

 $\#(\mathbf{tear\text{-}prod\text{-}rate} = normal \land \mathbf{contact\text{-}lenses} = none) = 3$

	soft	hard	none
reduced	0	0	12
normal	5	4	3