

CS1699: Blockchain Technology and Cryptocurrency

7. Proof of Work and Mining

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Recall Our Naive Consensus Protocol

- * "Pick a node at random, allow them to add their transactions in their transaction pool to blockchain"
- * Problems:
 - * How to pick a random node?
 - Assumes honest nodes easy to subvert
 - * Nothing at stake, no reason to be honest

Incentives

- * We can't punish dishonest nodes but...
- * What if there was an incentive to be an honest node?
- * How about... bitcoins?

Incentives in Bitcoin

- * Two incentive mechanisms:
 - * Block reward
 - * Transaction fees

Block Reward

- * The creator of a valid block gets a reward (currently 12.5 bitcoin halves every 210,000 blocks, will drop to 6.25 around May 2020) http://www.thehalvening.com/
- * Block reward only valid if it's on long-term consensus branch, which means other nodes must accept it
- * If longest-valid-branch, will incentivize to work off of longest branch and be honest
- * Creating blocks is hard work (as we will see) don't want to waste it!

The Future of the Block Reward

- * No other way to generate bitcoins besides block reward
- * Block rewards will end around the year 2140 (they keep halving approximately four years, for much longer than that they will be so small as to be insignificant)
- * So... nobody will mine from 2140 on, right?

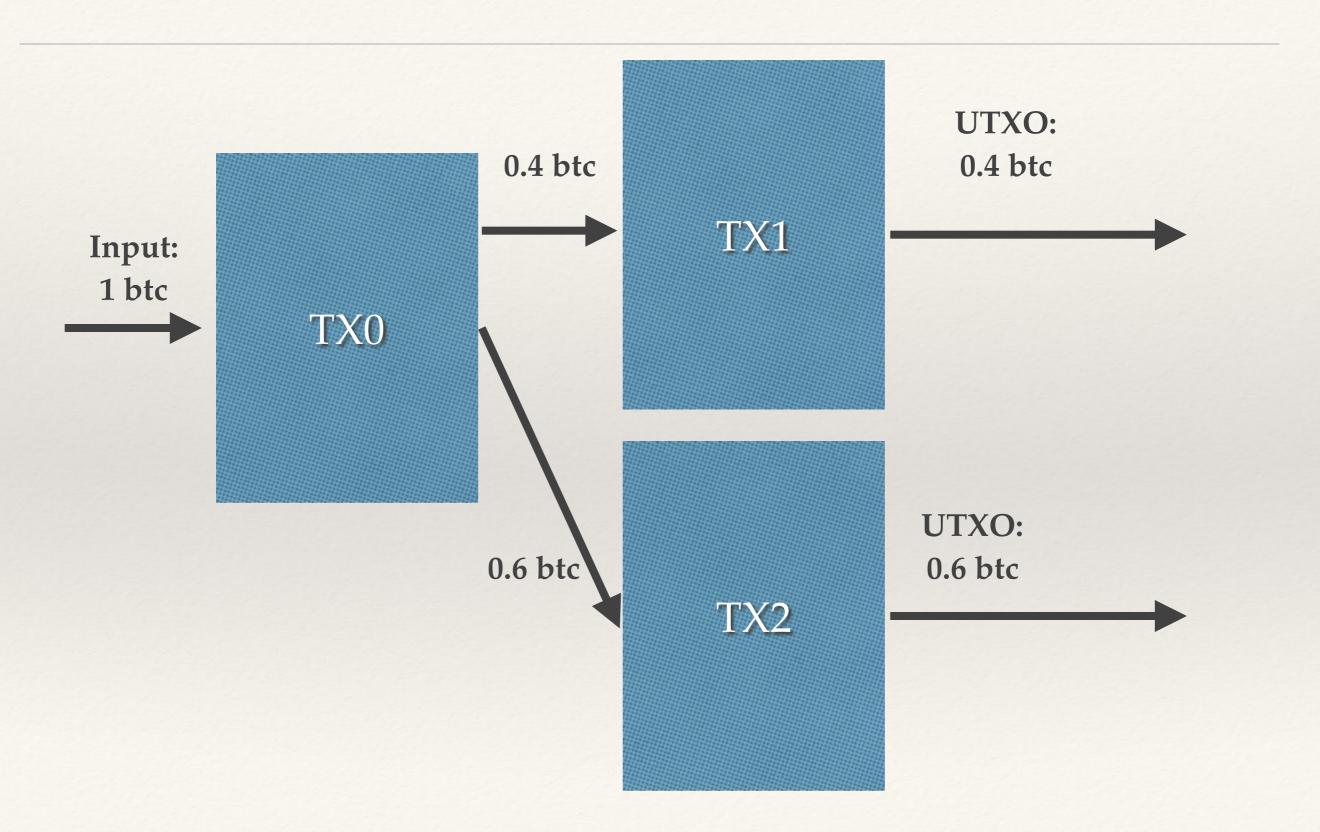
Transaction Fees

- * The other incentive mechanism is transaction fees
- * The creator of a transaction can decide to give themselves back less in "change" than necessary
- * This "missing bitcoin" can be claimed by the miner of a block

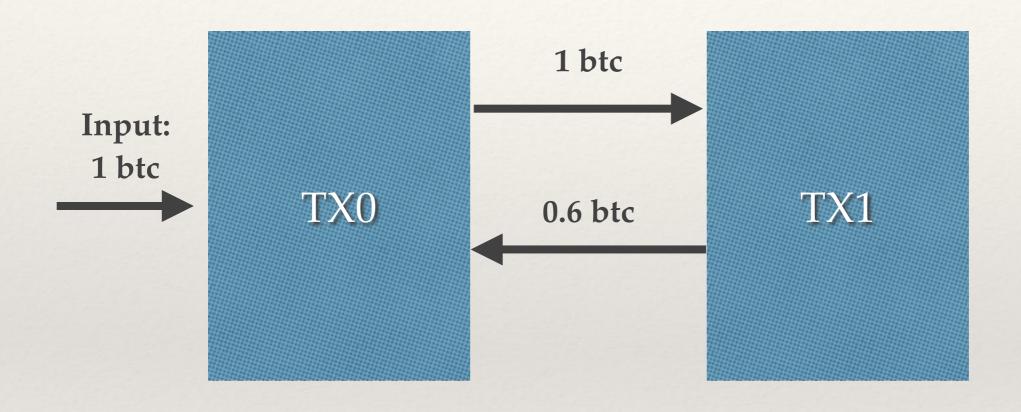
Side Note: UTXOs

- * Although we think of Bitcoin as a distributed ledger where address X has 4 bitcoin and address Y has 2.5 bitcoin, really each has a collection of *unspent transaction outputs*, that is, transactions that been input to an address but not yet output
- * We can tally up these outputs and determine the full amount of bitcoin that a particular address has, but behind the scenes they are actually a collection of these outputs

Transactions Behind the Scenes

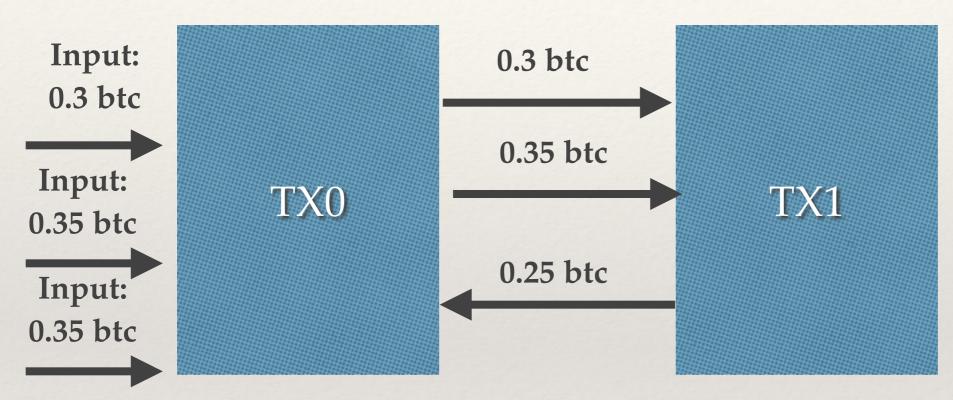


Splitting TXs - Sending 0.4 btc



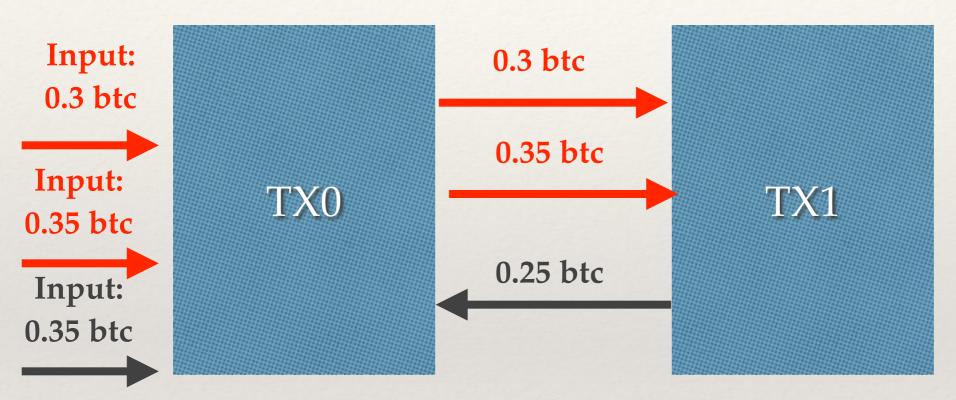
Multiple TX Input/Output

Sending 0.4 btc



Spent vs Unspent Tx's

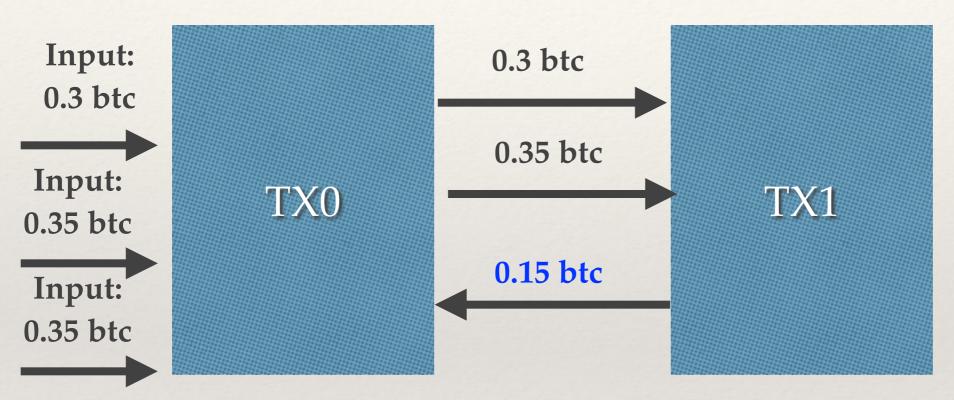
Sending 0.4 btc



Generator of TX0 now has two UTXOs: 0.35 btc and 0.25 btc Most bitcoin wallets will just show you 0.35 + 0.25 = 0.6 btc 1 btc - 0.4 btc = 0.6 btc

Multiple TX Input/Output

Sending 0.4 btc



What if we only asked for 0.15 btc back instead of 0.25?

Extra money is the *transaction fee* - whoever mines a block with this transaction can claim it!

Transaction Fees

- * Ceteris paribus, miners prefer to include transactions with higher fees
 - * There are reasons not to do so, however, which we will discuss later...
- * Think of it as bidding for space or express mail if you want your transaction in a block quickly, you gotta pay
- https://bitcoinfees.info/

Proof of Work

* So what's to stop you from going out there and making a block yourself and gathering some transaction fees?



* ... As Long You Can Provide a Valid Nonce

- * To create a block is going to require work (a tax on identity avoids Sybil attacks, or at least cheap ones)
- * Bitcoin uses SHA-256 hash puzzles, i.e., find a nonce (number used once) such that a hash of concatenation of the nonce, the hash of the previous block, and all transactions in the block is less than some target
- * $H(nonce \mid prev_hash \mid tx_1 \mid tx_2 \mid \dots tx_n) < target$

Recall Puzzle-Friendliness of SHA-256 Hash

- * No solving strategy for $H(id \mid \mid x) \in Y$ better than trying possible values of id
- * In other words, assuming a non-trivial target, we are going to have to try some very large number of nonces (with no shortcuts) before we find a nonce such that $H(nonce \mid \mid rest_of_block) < target$
- * And trying different values is the ONLY way to do so no shortcut, one-way function

Hash Puzzle Properties

- 1. Difficult to compute
- 2. Parameterizable (i.e. adjustable) cost
- 3. Trivial to verify

1. Difficult to Compute

- We want people to prove that they have worked for this (to avoid Sybil attacks / nothing-at-stake problem)
- * As of the creation of this slide, miners around the world are trying ~ 50,419,619,703,000,000,000 (> 50 quintillion) possible nonces every second, and they generally don't find a solution until after about ten minutes of this!
- * This number of attempts per second is called the *hash* rate or *hashpower* of the Bitcoin network

2. Paramaterizable Cost

- * January 12, 2009 hash rate was (best estimate) ~ 4,500,000 (orders of magnitude lower than today)
- * But blocks still were generated at a rate of about one every ten minutes
- Target re-adjusts itself every 2016 blocks based on (self-reported!)
 block times
 - * If blocks are taking longer than 10 minutes, difficulty adjusts down (target increases, making it easier to find nonce)
 - * If blocks are taking less than 10 minutes, difficulty adjusts up (target decreases, making it harder to find nonce)

Impact of Puzzle-Friendliness

- * Solving hash values is probabilistic some blocks are produced within seconds (or even "negative" time remember dealing with time in a distributed system!), others can take hours
- * Average is ~ 10 minutes
- https://data.bitcoinity.org/bitcoin/block_time/all? f=m10&t=l

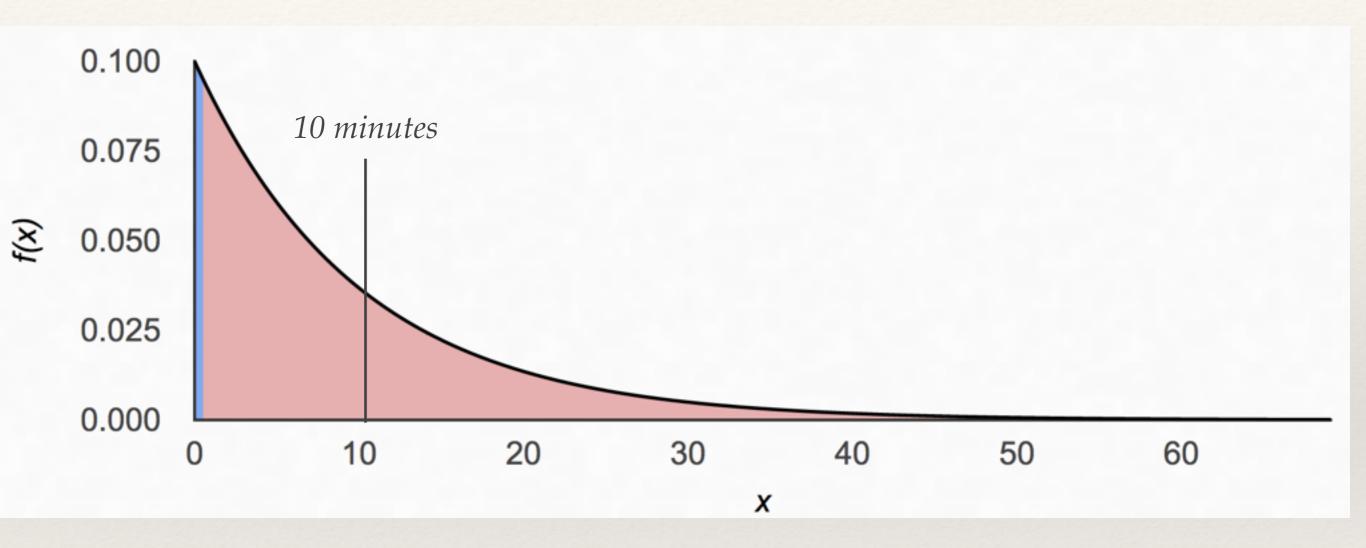
Bernoulli Trials

- * A Bernoulli trial is a process with two possible outcomes (success and failure), and the probability of being successful (and by implication, failure) is fixed between trials
- * Examples: coin flip, dice, roulette
- * Mining: Success H(nonce | | rest_of_block) < target
 Failure H(nonce | | rest_of_block) >= target

Poisson Process

- * Iterated Bernoulli trials (at large enough numbers so that we can basically act as if the result is continuous instead of discrete) represent a *Poisson process*
 - * A continous probabilistic process where events occur independently at a constant *average* rate
 - Likelihood of a block occurring follows an exponential distribution

Exponential Distribution



Note graph is positively skewed - median < mean.

Poisson Process - Mining Bitcoin

- * No nonces have been tried what is the mean time until $H(nonce \mid \mid rest_of_block) < target?$
- * 500 quintillion nonces have been tried what is the mean time until *H*(*nonce* | | *rest_of_block*) < *target*?

Poisson Process - Dice

- * I just rolled 1. How many rolls on average until I roll a 6?
- * I just rolled 4, 3, 1, 5, 2, 3, 3, 3, 2, 5, 4. How many rolls on average until I roll a 6?

Poisson Process - Next Successful Event?

- * For dice: on average (mean), 6 rolls
- * For Bitcoin blocks: on average (mean), 10 minutes
- * ALWAYS, at any point in time Bernoulli trials have no "memory", thus they are always "on average", i.e. mean 10 minutes away no matter how much time has already elapsed since the previous block.
- * It's been 45 minutes since the last block? On average, you *still* have 10 more minutes to wait! Poor you.

How Long for a Given Miner To Find a Block?

* I don't care about the network as a whole, I care about me!

mean time to my next block =

10 minutes

fraction of hashpower I control

3. Trivial to Verify

- * It should be very difficult to MINE a block, but easy for others to verify that it is valid
- * Computationally simple
 - * Run SHA-256 hash function against block with miner-calculated nonce
 - * If *H(nonce* | | rest_of_block) < target, block is valid

Mining Overview

```
// Should I mine Bitcoin?
mining_reward = block_reward + tx_fees
mining_cost = hardware_cost + operating_costs
if (mining_reward > mining_cost)
  return true
else
  return false
```

51% Attack

- * Recall that a key tenet of Bitcoin is decentralization
- * Mining allows us to perform distributed consensus and avoid a ScroogeCoin-like (or a Scrooge hiding behind an army of Sybils) centralization
- * But what if more than half of the hashpower is owned by a single entity? Is this a new Scrooge?

What Can Our Pseudo-Scrooge Do?

- * *Steal coins?* **No**. The ONLY way to move coins is knowing the secret key of the owner (public key).
- * Suppress transactions? **Yes**. Just like Scrooge, they can ignore transactions and refuse to put them in blocks but users will see transactions in mempool and realize this attack is occurring.
- * Change the block reward? **No**. They cannot change the rules of consensus valid nodes will ignore the blocks.
- * *Double-spend?* **Yes**. They can decide to build off a blockchain which does not include the block which includes a sent transaction.
- * *Hurt confidence in Bitcoin?* **Yes**. A key benefit of Bitcoin lies in its decentralized nature; destroying this may start an exodus to alternatives.

A Pale Yet Dangerous Shadow

- * Scrooge could change the block reward, suppress transactions without others realizing, or even change the rules of consensus none of which our Pseudo-Scrooge can do.
- Decentralization has benefits even when it's been centralized!