## Discriminant Analysis (DA)

## Supervised vs Unsupervised Learning\*

#### Supervised Learning

- Predict some feature of interest (e.g., disease type, cell type, disease prognosis, species of an organism) by using one or more other variables (the predictors)
- Typically we construct prediction rule from training data
- We want to predict new cases and have some criteria to assess the quality of prediction rule

#### Unsupervised learning

- Here all variables are on an equal footing.
- Techniques include
  - Principal Components Analysis, PCA
  - Multidimensional Scaling, MDS, nMDS
  - Hierarchical and non-Hierarchical Clustering (todo)
- We want to
  - Discover patterns, ordinations
  - Reduce dimensions produce low- dimensional maps to display data and data patterns

## Supervised vs Unsupervised Learning\*

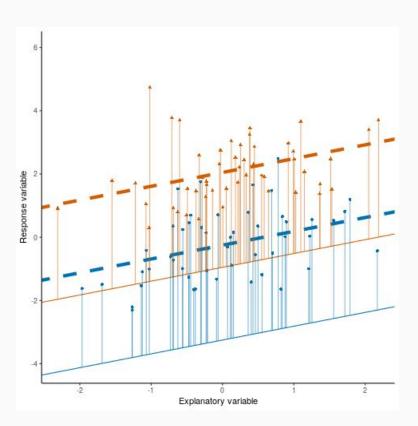
#### Supervised Learning

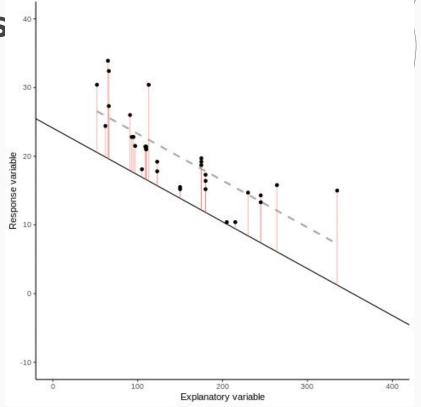
- Find a prediction rule to predict value of one feature, objective or response from the other features
- Response can be continuous or categorical
  - Continuous response: regression
  - Categorical response: classification

#### Unsupervised learning

 Find similarities or distances between cases based on their feature values, e.g. clustering, ordination

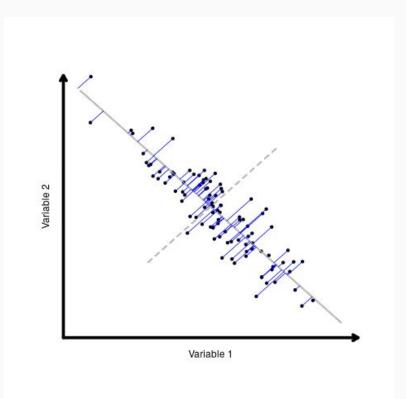
# Linear discriminant analysis all about y = mx + c ...



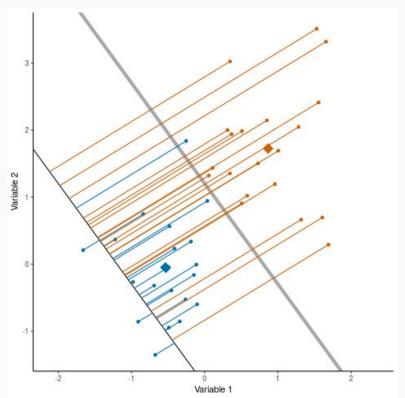


## PCA still has the straight lines

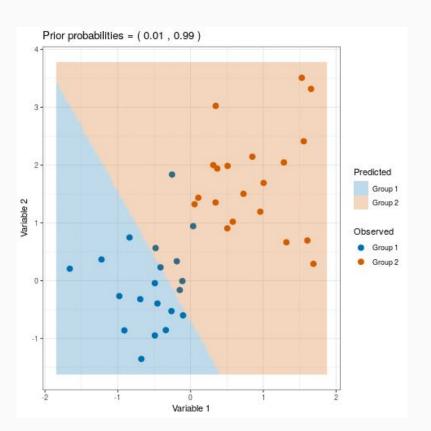
Note the slight difference in how we calculate distance (point to line, rather than point to point)



## So, what if we want to separate/discriminate groups?



### So, what if we want to separate/discriminate groups?

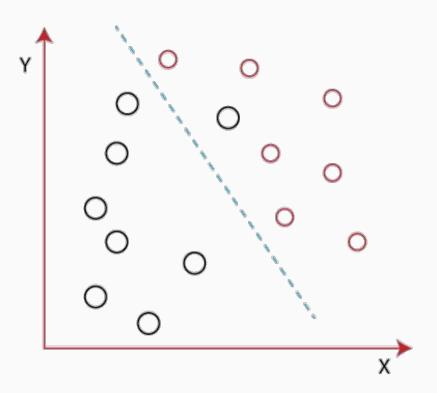


#### LDA

- Goal is to predict some feature of interest using one or more variables
- Like regression but predicting groups: think ANOVA meets PCA
- Finding a linear combination of features that classifies observations into groups

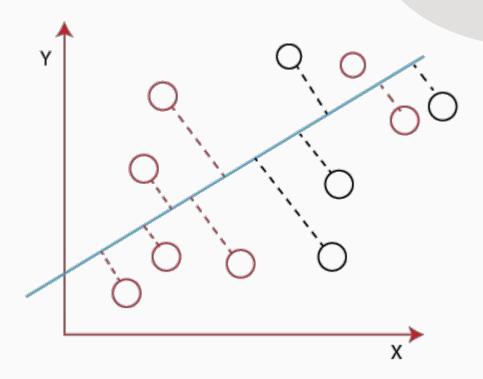
#### **LDA**

- It is impossible to draw a straight line in a 2-d plane that can separate these data points efficiently
- However, using linear discriminant analysis; we can dimensionally reduce the 2-D plane into the 1-D plane.
- Using this technique, we can also maximize the separability between multiple classes.



## LDA...

- Maximizes the distance between means of two classes, whilst
- Minimizing the variance within the individual class.



#### What we should be aware of

- The structure of our training data
  - Remember talking about algorithmic bias in Module 1
  - How many observations are in each group ("prior probabilities") will affect inference
  - It's your choice to assess if the defaults are correct or not.

#### To look out for

- The proportion of trace
  - Gives the percentage separation achieved by each discriminant function (think of eigenvalues /stress measures from PCA and MDS)
- The **discriminant functions** themselves
  - Give the linear combination of variables giving best separation between groups (think of reconstructing our principal components in PCA)
- The confusion (misclassification) matrix
  - The misclassification rate tells us the proportion of cases we miss classified:)
- Prediction of new cases! Using inbuilt functions we see
  - The predicted class (group) of the observations, and
  - The **posterior probabilities** for each observation belonging to each group

#### Glass Identification



#### [code along, activity 3]

