# **CP468 Assignment1 Missionaries and Cannibals**

## By Group 4 ZZ-TW-ML-YC

#### **Abstraction**

For convenience, in the remainder, each abbreviation has its own meaning:

Abbreviation	Meanning
M	missionary
C	cannibal
N	number of ${f M}$ or ${f C}$ (the same)
В	number of seats in boat
ml	number of ${f M}$ on left side
mb	number of ${f M}$ in boat
mr	number of ${f M}$ on right side
cl	number of ${f C}$ on left side
cb	number of ${f C}$ in boat
cr	number of ${f C}$ on right side
pos	position of boat, left side: 1, right side: 0
(ml, cl, pos)	one state when the boat is empty and on side pos, $ml\mathbf{M}$ and $cl\mathbf{C}$ are on the left side
L(mb, cb)	carry $mb\mathbf{M}$ and $cb\mathbf{C}$ to left side
R(mb, cb)	carry $mb\mathbf{M}$ and $cb\mathbf{C}$ to right side

## **Reality constraints**

Each number must be non-negative and less than the total number:

$$0 \le ml, mb, mr, cl, cb, cr \le N$$
$$0 \le mb, cb \le B$$
$$ml + mb + mr == cl + cb + cr == N$$

The boat can not across the river without someone in it:

$$0 < mb + cb \le B$$

## **Security constraints**

Whether on left, right or in boat, the number of  ${\bf M}$  should not less than that of  ${\bf C}$ :

$$ml == 0 || ml >= cl$$

$$mb == 0 || mb >= cb$$

#### **Initial State**

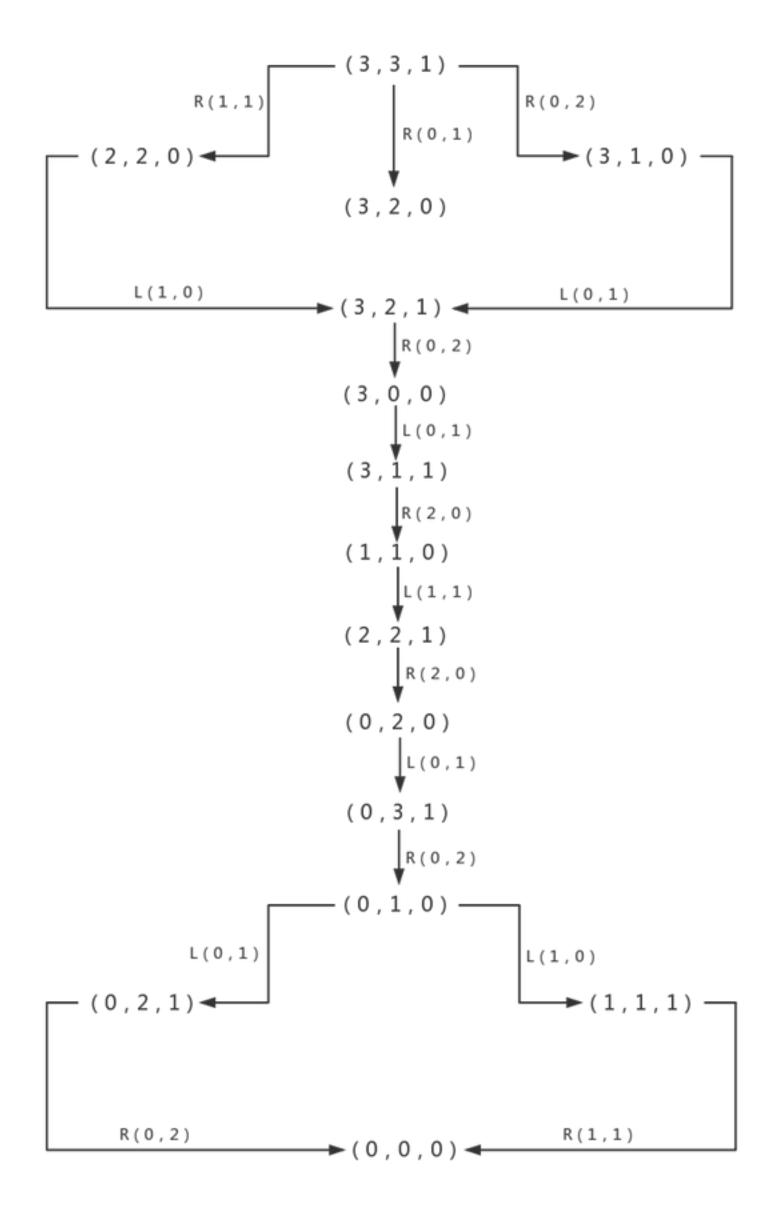
 $N\mathbf{M}$  and  $N\mathbf{C}$  are on one side, let's say left side, with a boat at the same side, described as (N, N, 1).

#### **Goal State**

 $N\mathbf{M}$ ,  $N\mathbf{C}$  and the boat are on the right side, described as (0, 0, 0).

#### **State Space**

Take N == 3, B == 2 as an example, below is the complete state space graph:



There are 10 states and 16 \* 2 = 32 transitions in total. For short we just show half of transitions:

**Transitions** 

Result((3,3,1), R(1,1)) = (2,2,0)
Result((3,3,1), R(0,1)) = (3,2,0)
Result((3,3,1), R(0,2)) = (3,1,0)
Result((2, 2, 0), L(1, 0)) = (3, 2, 1)
Result((3, 1, 0), L(0, 1)) = (3, 2, 1)
Result((3, 2, 1), R(0, 2)) = (3, 0, 0)
Result((3,0,0), L(0,1)) = (3,1,1)
Result((3, 1, 1), R(2, 0)) = (1, 1, 0)
Result((1, 1, 0), L(1, 1)) = (2, 2, 1)
Result((2, 2, 1), R(2, 0)) = (0, 2, 0)
Result((0, 2, 0), L(0, 1)) = (0, 3, 1)
Result((0,3,1), R(0,2)) = (0,1,0)
Result((0, 1, 0), L(0, 1)) = (0, 2, 1)
Result((0, 1, 0), L(1, 0)) = (1, 1, 1)
Result((0, 2, 1), R(0, 2)) = (0, 0, 0)
Result((1, 1, 1), R(1, 1)) = (0, 0, 0)

#### **Path Cost**

Path cost increased by one each time when the boat cross the river.

### **Algorithm Analysis**

We considered two algorithms for this problem:

iterative deenpening depth-first search(IDS) and iterative deepening a\* search(IDA\*).

	IDS	IDA*
complete	Υ	Υ
optimal	Υ	Υ
time	$O(b^d)$	$O(b^d)$
space	O(bd)	O(bd)

IDS and IDA\* are both complete in that they will continue searching until find a solution or exhaust all states. They are optimal in that the cost is increasing during iteration, in other words, the first solution found must cost least.

IDS and IDA\* are also the same in structure: outside is a iteration of limit and inside is a recursion of search function.

But IDS uses g(n) (cost from start state to current state n) as limit, IDA\* uses f(n) = g(n) + h(n) (global estimated cost) instead.

Moreover, IDS does DFS within the limit from one child state; while IDA\* will expand at the child state with the minimum value of f(n).

Another thing worth talking is the selection of hueristic function of IDA\*.

#### Implementation in Java

Source code can be find here: https://github.com/BIOTONIC/MissionariesAndCannibals

Test.java	State.java	Action.java	IDS.java	IDAStar.java
call two algorithms	store state's info & provide functions related to state	use two lists to store all valid arrangements of $M$ and $C$ on boat	IDS algorithm	IDA* algorithm

Below is the output of two algorithms when N == 3 and B == 2. Solutions of two algorithms are the same because they traverse all actions of a given state by the same sequence provided by Action.java. One difference is that IDA\*'s limit starts directly from 4.

```
iterative deepening depth-first search
try depth limit 1
try depth limit 2
try depth limit 3
try depth limit 4
try depth limit 5
try depth limit 6
try depth limit 7
try depth limit 8
try depth limit 9
try depth limit 10
try depth limit 11
optimal solution found
step 1: (3,3,1) \Rightarrow (0,2)
step 2: (3,1,0) \ll (0,1)
step 3: (3,2,1) \Rightarrow (0,2)
step 4: (3,0,0) \ll (0,1)
step 5: (3,1,1) \Rightarrow (2,0)
step 6: (1,1,0) \ll (1,1)
step 7: (2,2,1) \Rightarrow (2,0)
step 8: (0,2,0) \ll (0,1)
step 9: (0,3,1) \Rightarrow (0,2)
step 10: (0,1,0) \ll (0,1)
step 11: (0,2,1) \Rightarrow (0,2)
iterative deepening a star search
try depth limit 4
try depth limit 5
try depth limit 6
try depth limit 7
try depth limit 8
try depth limit 9
try depth limit 10
try depth limit 11
optimal solution found
step 1: (3,3,1) \Rightarrow (0,2)
step 2: (3,1,0) \ll (0,1)
step 3: (3,2,1) \Rightarrow (0,2)
step 4: (3,0,0) \ll (0,1)
step 5: (3,1,1) \Rightarrow (2,0)
step 6: (1,1,0) \ll (1,1)
step 7: (2,2,1) \Rightarrow (2,0)
step 8: (0,2,0) \ll (0,1)
step 9: (0,3,1) \Rightarrow (0,2)
step 10: (0,1,0) \ll (0,1)
step 11: (0,2,1) \Rightarrow (0,2)
```

Both algorithms are able to solve N missionaries, N cannibals and B seats problems. Below is the output when N == 7 and B == 4:

```
step 1: (7,7,1) \Rightarrow (0,4)

step 2: (7,3,0) \Leftarrow (0,2)

step 3: (7,5,1) \Rightarrow (0,4)

step 4: (7,1,0) \Leftarrow (0,2)

step 5: (7,3,1) \Rightarrow (4,0)

step 6: (3,3,0) \Leftarrow (1,1)

step 7: (4,4,1) \Rightarrow (2,2)

step 8: (2,2,0) \Leftarrow (1,1)

step 9: (3,3,1) \Rightarrow (2,2)

step 10: (1,1,0) \Leftarrow (1,1)

step 11: (2,2,1) \Rightarrow (2,2)
```

#### //TODO 何时有解无解

The remainder is the source code. Download it from github if you want to run and test it.

```
// Test.java
// call two algorithms

public class Test {
    public static void main(String[] args) {
        new IDS(7, 4, 1000); // N=7 B=4 upperLimit=1000
        new IDAStar(3, 2, 1000); // N=3 B=2 upperLimit=1000
    }
}
```

```
// State.java
// store state's info & provide functions related to state
class State {
    int n; // numbers of missionaries or cannibals
    int ml; // numbers of missionaries on the left
    int cl; // numbers of cannibals on the left
    int pos; // current position of the boat, 0: on the right, 1: on the left
    // start state: ml=N, cl=N, pos=1
    // goal state: ml=0, cl=0, pos=0
    State(int n) {
        this.n = n;
        this.ml = n;
        this.cl = n;
        this.pos = 1;
    }
    State(int n, int ml, int cl, int pos) {
        this.n = n;
        this.ml = ml;
        this.cl = cl;
        this.pos = pos;
    }
    State doAction(int mb, int cb) {
        if (pos == 0) {
            // current at right, to left
            // 0<=ml+mb<=N
```

```
// && 0<=cl+cb<=N
        // \&\& (ml+mb==0||ml+mb==N||ml+mb==cl+cb)
        if (ml + mb >= 0 \&\& ml + mb <= n
                && cl + cb >= 0 && cl + cb <= n
                && (ml + mb == 0 \mid \mid ml + mb == n \mid \mid ml + mb == cl + cb)) {
            return new State(n, ml + mb, cl + cb, 1);
        } else {
            return null;
        }
    } else {
        // current at left, to right
        // 0<=ml-mb<=N
        // && 0<=cl-cb<=N
        // && (ml==mb||ml+mb==N||ml-mb==cl-cb)
        if (ml - mb \ge 0 \&\& ml - mb \le n)
                && cl - cb >= 0 && cl - cb <= n
                && (ml == mb \mid | ml + mb == n \mid | ml - mb == cl - cb)) {
            return new State(n, ml - mb, cl - cb, 0);
        } else {
            return null;
        }
}
@Override
public boolean equals(Object other) {
    if (this == other) {
        return true;
    }
    if (other == null) {
        return false;
    }
    if (getClass() != other.getClass()) {
        return false;
    }
    State otherState = (State) other;
    if (otherState.n == this.n && otherState.ml == this.ml
            && otherState.cl == this.cl && otherState.pos == this.pos) {
        return true;
    } else {
        return false;
    }
}
@Override
public String toString() {
    return "(" + this.ml + "," + this.cl + "," + this.pos + ")";
}
public String toPath(int mb, int cb) {
    return toString() + " " + (pos == 1 ? "=> " : "<= ") + "(" + mb + "," + cb + ")";
}
public String toPath(State child) {
    return toString() + " " + (pos == 1 ? "=> " : "<= ") + "("
            + Math.abs(child.ml - ml) + "," + Math.abs(child.cl - cl) + ")";
}
boolean isGoal() {
    if (ml == 0 && cl == 0 && pos == 0) {
        return true;
    } else {
        return false;
```

```
}
// Action.java
// use two lists to store all valid arrangements of m and c on boat
import java.util.ArrayList;
public class Action {
    public static ArrayList<Integer> mbs; // list of numbers of missionaries on boat
    public static ArrayList<Integer> cbs; // list of numbers of cannibals on boat
    Action(int N, int B) {
        mbs = new ArrayList<>();
        cbs = new ArrayList<>();
        for (int b = B; b > 0; b--) {
            for (int mb = 0; mb <= N; mb++) {
                if (mb \le b \& \& b - mb \ge 0 \& \& b - mb \le N \& \& (mb == 0 | | 2 * mb >= b)) {
                    mbs.add(mb);
                    cbs.add(b - mb);
            }
        }
    }
}
```

}

```
// IDS.java
import java.util.ArrayList;
import java.util.Stack;
public class IDS {
    int N; // numbers of missionaries and cannibals are both N
    int B; // number of seats on boat
    Action action;
    ArrayList<State> explored;
    Stack<String> records; // records of every optimal step
    static final int SUCCESS = 0;
    static final int FAILURE = -1;
    static final int CUTOFF = -2;
    public IDS(int N, int B, int upperLimit) {
        System.out.println("iterative deepening depth-first search");
        this.N = N;
        this.B = B;
        action = new Action(N,B);
        int limit = 0;
        int result;
        State state;
        do {
            // iterate limit
            limit++;
            System.out.println("try depth limit " + limit);
            // init state and explored list before every iteration
            state = new State(N);
            explored = new ArrayList<>();
            records = new Stack<>();
            result = search(state, limit);
```

```
if (result == SUCCESS) {
            break;
        } else if (result >= upperLimit) {
            result = FAILURE;
            break;
        }
    } while (search(state, limit) != SUCCESS);
    // print result
    if (result == SUCCESS) {
        int i = 1;
        while (!records.empty()) {
            System.out.println("step " + i + ": " + records.pop());
            i++;
        }
    } else {
        System.out.println("no solution when upper limit is " + limit);
    }
}
int search(State state, int limit) {
    explored.add(state);
    if (state.isGoal()) {
        explored.remove(state);
        System.out.println("optimal solution found");
        return SUCCESS;
    }
    if (limit == 0) {
        explored.remove(state);
        //System.out.println("cut off");
        return CUTOFF;
    }
    boolean isCutoff = false;
    // traversal all actions
    for (int i = 0; i < action.mbs.size(); i++) {
        State child = state.doAction(action.mbs.get(i), action.cbs.get(i));
        // graph search
        // only expand valid and non-repetitive states
        if (child != null && !explored.contains(child)) {
            //System.out.println(child);
            // recursion, decreasing limit
            int result = search(child, limit - 1);
            if (result == CUTOFF) {
                // once result from child is cutoff (child state limit == 0)
                // current state is cutoff too
                // need to increase depth limit
                // so just jump out of the for loop immediately
                isCutoff = true;
                break;
            } else if (result != FAILURE) {
                // find a step
                records.push(state.toPath(action.mbs.get(i), action.cbs.get(i)));
                explored.remove(state);
                return result;
            }
        }
    }
    explored.remove(state);
    if (isCutoff) {
        return CUTOFF;
    } else {
        System.out.println("no solution");
        return FAILURE;
```

```
}
// IDAStar.java
import java.util.Stack;
public class IDAStar {
    int N; // numbers of missionaries and cannibals are both N
    int B; // number of seats on boat
    Action action;
    Stack<State> path;
    Stack<String> records; // records of every optimal step
    static final int SUCCESS = 0;
    static final int FAILURE = -1;
    public IDAStar(int N, int B, int upperLimit) {
        System.out.println("iterative deepening a star search");
        this.N = N;
        this.B = B;
        action = new Action(N,B);
        records = new Stack<>();
        State state = new State(N);
        path = new Stack<>();
        path.push(state);
        int limit = h(state);
        int result;
        do {
            System.out.println("try depth limit " + limit);
            result = search(0, limit);
            if (result == SUCCESS) {
                break;
            } else if (result >= upperLimit) {
                result = FAILURE;
                break;
            limit = result;
        } while (result != SUCCESS);
        // print result
        if (result == SUCCESS) {
            State child = path.pop();
            while (!path.empty()) {
                records.push(path.peek().toPath(child));
                child = path.pop();
            }
            int i = 1;
            while (!records.empty()) {
                System.out.println("step " + i + ": " + records.pop());
            }
        } else {
            System.out.println("no solution when upper limit is " + limit);
        }
    }
```

}

}

```
int h(State state) {
        return state.ml + state.cl - 2 * state.pos;
    }
    int search(int g, int limit) {
        State state = path.peek();
        int f = g + h(state);
        if (f > limit) {
            return f;
        } else if (state.isGoal()) {
            System.out.println("optimal solution found");
            return SUCCESS;
        }
        int min = Integer.MAX_VALUE;
        // traversal all actions
        for (int i = 0; i < action.mbs.size(); i++) {
            State child = state.doAction(action.mbs.get(i), action.cbs.get(i));
            // graph search
            // only expand valid and non-repetitive states
            if (child != null && !path.contains(child)) {
                //System.out.println(child);
                path.push(child);
                int result = search(g + 1, limit);
                if (result == SUCCESS) {
                    return SUCCESS;
                }
                if (result < min) {</pre>
                    min = result;
                path.pop();
            }
        return min;
    }
}
```