

a. Because  $z$  is the ancestor of  $v$

b.  $z$  is the descendant of  $v$ . So  $z$  is a back edge in DFS.

c. It's shows that  $v$  is visited before  $z$ . Since both  $v.d$  and  $v.f$  are smaller than attributes of  $z$ .

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(1) If it's back edge, this indicates the two vertex connected with this edge is the descendant of the other edge. But BFS doesn't contain the process of "moving up". And for forward edges, it indicates one vertex of this edge connected has already processed, this is impossible too.

Since all processed vertices must connect with the vertex with out going through another.

(2) If only when the edge goes to the vertex that has been processed but can't be tree edge. So it's path to root is at least the current vertex + 1.

(3) Depth of vertex edge in cross edge would be more than 1. ~~Depth of vertex is cross edge would be~~

b. (1) ~~forward edges mean a path from the root to the current~~

(2) BFS only consider shorter path first, but in forward edge, we need to already processed a vertex using more than one edge, that's not the shortest path.



(2) Because it's tree edge that means  $v$  is the direct descendant of  $u$ .  
 so  $v.d = u.d + 1$

(3) It's cross edge means that from the root to  $v$ ,  $z.d + 1$   
 $z.d + 1$  serves as the upper bound for updating  $v.d$  to  $z.v$ .  
 (Inspired by DFS)

(4) there's some path from  $v$  to  $z$ , there are all tree edges.  
 (since it's back edge)  $v, v_1, v_2, \dots, v_k, z$   
 in this path.  $z$  is

$$z.d = v_k.d + 1 = v_{k-1}.d + 2 = \dots = v.d + k + 1. \text{ so } z.d > v.d.$$

And  $v.d > 0$ .

