

P2.

15.1.3

Cut-rod-modified ( $P, n, c$ )

if  $n=0$

return 0

$q = -\infty$

for  $i=1$  to  $n$

$q = \max(q, P[i] - c + \text{cut-rod}(P, n-i))$

$q = q - c$

return  $q$ .

15.2.4

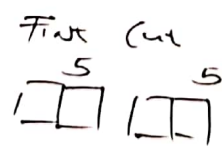
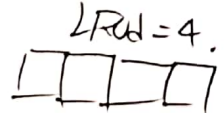
vertices:  $1 + (n-1) + (n-2) + \dots + 1 = \frac{(n+1) \cdot n}{2}$

Edges: It has  $\sum_{i=1}^n \sum_{j=1}^i (j-i) = \sum_{i=1}^n \sum_{k=0}^{i-1} k$

$$= \sum_{i=1}^n \frac{i(i-1)}{2} = \frac{n(n-1)}{2}$$

15.2.5

For example, take figure 15.2 as example.



Revenue =  $5 + 5 = 10$ , which is maximised.

~~So we can tell that it is impossible because we can only have 1 length, at our first cut. So the previous optimal subproblem doesn't hold.~~

If we have rod = 4, we can produce 4 pieces of rods. the original one new to cut it into two. which is different from now. So the original solution doesn't hold anymore



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15-3

(To be honest again I searched this on google to get hints, It's beyond my ability)

If this is in test I would directly drop dead,

we can equally make this problem into: A and B start from the leftmost point. And travel two different paths And reach the rightmost point

Let  $f[i][j]$  stand for the shortest path that A goes to  $i$

And B goes to  $j$ .

when  $i = j$

$$f[i][j] = \min_{1 \leq k \leq j-1} (f[k][i] + \text{dis}[k][i])$$

$i < j-1$

$$f[i][j] = f[i][j-1] + \text{dis}[j-1][j]$$

for ( $j=3$  ;  $j \leq n$  ;  $j++$ ) {

for ( $i=1$  ;  $i < j-1$  ;  $i++$ ) {

$$f[i][j] = f[i][j-1] + \text{dis}[j-1][j]$$

}

for ( $k=1$  ;  $k \leq j-2$  ;  $k++$

$$f[j-1][j] = \min(f[j-1][j], f[k][j-1] + \text{dis}[k][j]),$$

for (int  $k=1$  ;  $k \leq j-1$  ;  $k++$ )

$$f[j][j] = \min(f[j][j], f[k][j] + \text{dis}[k][j])$$

return  $f[n][n]$ .

