2008-2009 第二学期期中试题(B卷)解答

2.
$$\sqrt{3}$$
, $5\sqrt{3}$ (2 $\%$, 2 $\%$)

3.
$$\{-3,3\}$$
, $3\sqrt{2}$ (2分,2分)

4.
$$1+x+\frac{1}{2}(x^2+2y^2)+o(\rho^2)$$
 (一次项 1 分, 二次项 2 分, 余项 1 分)

5.
$$yf_1' + e^x f_2'$$
, $f_1' + xyf_{11}'' + (y + xe^x)f_{12}'' + e^x f_{22}''$ (2 $\%$, 2 $\%$)

6.
$$\{1, -\frac{3}{5}, -\frac{2}{5}\}$$

7.
$$\frac{y^2}{2}\arcsin x - \ln|\cos x| + \frac{y^2}{2}$$

$$= 2xyz + x^2y\frac{\partial z}{\partial x} = f' \cdot (-\frac{\partial z}{\partial x})$$
(4 \(\frac{\pi}{2}\))

$$\frac{\partial z}{\partial x} = \frac{-2xyz}{f' + x^2y} \tag{5 \text{ }\%}$$

$$x^{2}z + x^{2}y \frac{\partial z}{\partial y} = f' \cdot (1 - \frac{\partial z}{\partial y}) \qquad (9 \%)$$

$$\frac{\partial z}{\partial x} = \frac{f' - x^2 z}{f' + x^2 y} \tag{10 }$$

$$\equiv . I = 2 \int_0^{\frac{\pi}{2}} d\theta \int_0^{2R\cos\theta} \rho \sqrt{4R^2 - \rho^2} d\rho(4 \%)$$

$$= -\frac{16}{3}R^{3} \int_{0}^{\frac{\pi}{2}} (\sin^{3}\theta - 1) d\theta \qquad(8 \, \%)$$

$$= -\frac{8(4-3\pi)}{9}R^3 \qquad(10 \, \%)$$

由于 $\frac{\partial f}{\partial \vec{e}}$ 在曲线上确有最大值和最小值,故 M_1, M_2 为所求,且

$$\max_{M} \{ \frac{\partial f}{\partial \vec{e}} \} = \frac{10}{\sqrt{3}} \qquad \min_{M} \{ \frac{\partial f}{\partial \vec{e}} \} = -\frac{10}{\sqrt{3}} \qquad \dots (12 \ \%)$$