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# Basics of Neural Network

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## Programming Vectorization

# What is vectorization?

$$z = \underbrace{\omega^T x}_{\text{Non-vectorized}} + b$$

Non-vectorized:

$$z = 0$$

```
for i in range(n - x):  
    z += w[i] * x[i]
```

$$z += b$$

$$\omega = \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix} \quad x = \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix}$$

$$\omega \in \mathbb{R}^{n_x} \quad x \in \mathbb{R}^{n_x}$$

Vectorized

$$z = \underbrace{\text{np.dot}(\omega, x)}_{w^T x} + b$$

$\rightarrow$  GPU } SIMD - single instruction  
 $\rightarrow$  CPU } multiple data.



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## Programming

### More vectorization examples

# Neural network programming guideline

Whenever possible, avoid explicit for-loops.

# Neural network programming guideline

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$$u = Av$$

$$u_i = \sum_j A_{ij} v_j$$

$u = np.zeros((n,))$

for i ...

    for j ...

$u[i] += A[:, i] * v[j]$

$$u = np.dot(A, v)$$

# Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_2} \\ \vdots \\ e^{v_n} \end{bmatrix}$$

$\rightarrow u = np.zeros((n,1))$   
 ~~$\rightarrow$  for i in range(n):~~  $\rightarrow u[i] = \text{math.exp}(v[i])$

import numpy as np  
u = np.exp(v) ←  
→  
np.log(v)  
np.abs(v)  
np.maximum(v, 0)  
v\*\*2  
v/v

# Logistic regression derivatives

$$J = 0, \cancel{dw_1 = 0}, \cancel{dw_2 = 0}, db = 0$$

for  $i = 1$  to  $n$ :

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log (1 - \hat{y}^{(i)})]$$

$$\cancel{dw_j} \leftarrow \cancel{0}$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$\begin{cases} dw_1 \leftarrow x_1^{(i)} dz^{(i)} \\ dw_2 \leftarrow x_2^{(i)} dz^{(i)} \\ db \leftarrow dz^{(i)} \end{cases}$$

$$n_x = 2$$

$$dw \leftarrow x^{(i)} dz^{(i)}$$

$$J = J/m, \cancel{dw_1 = dw_1/m}, \cancel{dw_2 = dw_2/m}, db = db/m$$

$$dw \leftarrow m \cdot$$

$$dw = np.zeros((n_x, 1))$$



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# Basics of Neural Network Programming Broadcasting in Python

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# Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

	Apples	Beef	Eggs	Potatoes	
Carb	56.0	0.0	4.4	68.0	
Protein	1.2	104.0	52.0	8.0	= A (3,4)
Fat	1.8	135.0	99.0	0.9	

59 cal

$$\frac{56}{59} \approx 94.9\%$$



Calculate % of calories from Carb, Protein, Fat. Can you do this without explicit for-loop?

cal = A.sum(axis = 0)

percentage = 100\*A/(cal.reshape(1,4))

↑(3,4) / (1,4)

# Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \\ 100 \end{bmatrix} \xrightarrow{100}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix} \xleftarrow{(m,n) \quad (2,3)} \xrightarrow{(1,n) \rightsquigarrow (m,n) \quad (2,3)}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 & 200 \end{bmatrix} = \xleftarrow{(m,1)} \xleftarrow{(m,n)}$$

# General Principle

$$\begin{array}{ccc} (m, n) & \xrightarrow{\quad \pm \quad} & (1, n) \rightsquigarrow (m, n) \\ \underline{\text{matrix}} & \xrightarrow{\quad \times \quad} & (m, 1) \rightsquigarrow (m, n) \end{array}$$

$$\begin{array}{ccccc} (m, 1) & + & \mathbb{R} & & \\ \left[ \begin{smallmatrix} 1 \\ 2 \\ 3 \end{smallmatrix} \right] & + & 100 & = & \left[ \begin{smallmatrix} 101 \\ 102 \\ 103 \end{smallmatrix} \right] \\ [1 2 3] & + & 100 & = & [101 \quad 102 \quad 103] \end{array}$$

Matlab/Octave: bsxfun



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## Programming

A note on python/  
numpy vectors

# Python Demo

# Python / numpy vectors

```
import numpy as np  
  
a = np.random.randn(5)  
  
a = np.random.randn((5,1))  
  
a = np.random.randn((1,5))  
  
assert(a.shape = (5,1))
```