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Basics of Neural Network Programming Vectorization

What is vectorization?

$$z = \underbrace{w^T x} + b$$

$$w = \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix} \quad x = \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix}$$

$$w \in \mathbb{R}^{n_x}$$

$$x \in \mathbb{R}^{n_x}$$

Non-vectorized:

$$z = 0$$

for i in $\text{range}(n-x)$:

$$z += w[i] * x[i]$$

$$z += b$$

Vectorized

$$z = \underbrace{\text{np.dot}(w, x)}_{w^T x} + b$$

\Rightarrow GPU } SIMD - single instruction
 \Rightarrow CPU } multiple data.



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Basics of Neural Network Programming

More vectorization examples

Neural network programming guideline

Whenever possible, avoid explicit for-loops.

Neural network programming guideline

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$$u = Av$$

$$u_i = \sum_j A_{ij} v_j$$

$$u = \text{np.zeros}(n, 1)$$

for i ... ←

for j ... ←

$$u[i] += A[i][j] * v[j]$$

$$u = \text{np.dot}(A, v)$$

Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_2} \\ \vdots \\ e^{v_n} \end{bmatrix}$$

→ `u = np.zeros((n,1))`

→ `for i in range(n):` ←
 → `u[i]=math.exp(v[i])`

`import numpy as np`
`u = np.exp(v)` ←

`np.log(v)`

`np.abs(v)`

`np.maximum(v, 0)` ↓

`v**2`

`v/v`

Logistic regression derivatives

$$J = 0, \text{ ~~dw1 = 0, dw2 = 0, db = 0~~ }$$

$$dw = np.zeros((n-x, 1))$$

→ for i = 1 to n:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log (1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$\text{~~dw}_1 += x_1^{(i)} dz^{(i)}~~$$

$$\text{~~dw}_2 += x_2^{(i)} dz^{(i)}~~$$

$$db += dz^{(i)}$$

$$n_x = 2$$

$$dw += x^{(i)} dz^{(i)}$$

$$J = J/m, \text{ ~~dw}_1 = dw_1/m, dw_2 = dw_2/m, db = db/m~~$$

$$dw /= m.$$



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Basics of Neural Network Programming Broadcasting in Python

Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

	Apples	Beef	Eggs	Potatoes
Carb	56.0	0.0	4.4	68.0
Protein	1.2	104.0	52.0	8.0
Fat	1.8	135.0	99.0	0.9

= A
(3,4)



59 cal

$$\frac{56}{59} \approx 94.9\%$$

Calculate % of calories from Carb, Protein, Fat. Can you do this without explicit for-loop?

cal = A.sum(axis = 0)

percentage = 100*A/(cal.reshape(1,4))

↑(3,4) / (1,4)

Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \\ 100 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}_{(m,n)} + \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 & 200 \end{bmatrix}_{\substack{(m,1) \\ \vdots \\ (m,n)}} =$$

General Principle

$$\begin{array}{ccc} (m, n) & + & (1, n) \\ \text{matrix} & \times & \rightsquigarrow (m, n) \\ \hline & / & \end{array}$$
$$(m, 1) \rightsquigarrow (m, n)$$

$$\begin{array}{ccc} (m, 1) & + & \mathbb{R} \\ \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} & + & 100 \\ [1 \ 2 \ 3] & + & 100 \end{array} = \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix}$$
$$= [101 \quad 102 \quad 103]$$

Matlab/Octave: bsxfun



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Basics of Neural Network

Programming

A note on python/
numpy vectors

Python Demo

Python / numpy vectors

```
import numpy as np
```

```
a = np.random.randn(5)
```

```
a = np.random.randn((5,1))
```

```
a = np.random.randn((1,5))
```

```
assert(a.shape == (5,1))
```