

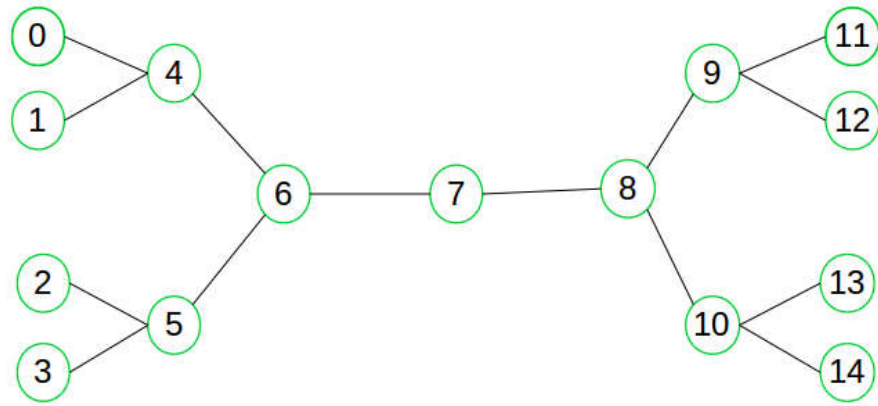
Assignment Group – 60

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Q4. Explain your strategy in bi-directional search.

Ans:

1. Bidirectional search is a graph search algorithm that finds a shortest path from an initial vertex to a goal vertex in a directed graph. It runs two simultaneous searches: one forward from the initial state, and one backward from the goal, stopping when the two meet. The reason for this approach is that in many cases it is faster: for instance, in a simplified model of search problem complexity in which both searches expand a tree with branching factor b , and the distance from start to goal is d , each of the two searches has complexity $O(bd/2)$ (in Big O notation), and the sum of these two search times is much less than the $O(bd)$ complexity that would result from a single search from the beginning to the goal.
2. We can consider bidirectional approach when- Both initial and goal states are unique and completely defined. And the branching factor is exactly the same in both directions.
3. Bidirectional search is complete if BFS is used in both searches. Also, it is optimal if BFS is used for search and paths have uniform cost. Time and space complexity is $O(bd/2)$.
4. For below figure, Suppose we want to find if there exists a path from vertex 0 to vertex 14. Here we can execute two searches, one from vertex 0 and other from vertex 14. When both forward and backward search meet at vertex 7, we know that we have found a path from node 0 to 14 and search can be terminated now. We can clearly see that we have successfully avoided unnecessary exploration.



5. Pseudo Code:

BIDIRECTIONAL_SEARCH

```
1   $Q_I.Insert(x_I)$  and mark  $x_I$  as visited
2   $Q_G.Insert(x_G)$  and mark  $x_G$  as visited
3  while  $Q_I$  not empty and  $Q_G$  not empty do
4      if  $Q_I$  not empty
5           $x \leftarrow Q_I.GetFirst()$ 
6          if  $x = x_G$  or  $x \in Q_G$ 
7              return SUCCESS
8          forall  $u \in U(x)$ 
9               $x' \leftarrow f(x, u)$ 
10             if  $x'$  not visited
11                 Mark  $x'$  as visited
12                  $Q_I.Insert(x')$ 
13             else
14                 Resolve duplicate  $x'$ 
15     if  $Q_G$  not empty
16          $x' \leftarrow Q_G.GetFirst()$ 
17         if  $x' = x_I$  or  $x' \in Q_I$ 
18             return SUCCESS
19         forall  $u^{-1} \in U^{-1}(x')$ 
20              $x \leftarrow f^{-1}(x', u^{-1})$ 
21             if  $x$  not visited
22                 Mark  $x$  as visited
23                  $Q_G.Insert(x)$ 
24             else
25                 Resolve duplicate  $x$ 
26 return FAILURE
```

6. Conceptual implementation:

```
# Python3 program for Bidirectional BFS
# Search to check path between two vertices
```

```
# Class definition for node to
# be added to graph
class AdjacentNode:
```

```
    def __init__(self, vertex):
```

```
self.vertex = vertex
self.next = None
```

```
# BidirectionalSearch implementation
class BidirectionalSearch:
```

```
def __init__(self, vertices):
```

```
    # Initialize vertices and
    # graph with vertices
    self.vertices = vertices
    self.graph = [None] * self.vertices
```

```
    # Initializing queue for forward
    # and backward search
    self.src_queue = list()
    self.dest_queue = list()
```

```
    # Initializing source and
    # destination visited nodes as False
    self.src_visited = [False] * self.vertices
    self.dest_visited = [False] * self.vertices
```

```
    # Initializing source and destination
    # parent nodes
    self.src_parent = [None] * self.vertices
    self.dest_parent = [None] * self.vertices
```

```
# Function for adding undirected edge
def add_edge(self, src, dest):
```

```
    # Add edges to graph
```

```
    # Add source to destination
    node = AdjacentNode(dest)
    node.next = self.graph[src]
    self.graph[src] = node
```

```
    # Since graph is undirected add
    # destination to source
    node = AdjacentNode(src)
    node.next = self.graph[dest]
```

```
self.graph[dest] = node
```

```
# Function for Breadth First Search
```

```
def bfs(self, direction = 'forward'):
```

```
    if direction == 'forward':
```

```
        # BFS in forward direction
```

```
        current = self.src_queue.pop(0)
```

```
        connected_node = self.graph[current]
```

```
        while connected_node:
```

```
            vertex = connected_node.vertex
```

```
            if not self.src_visited[vertex]:
```

```
                self.src_queue.append(vertex)
```

```
                self.src_visited[vertex] = True
```

```
                self.src_parent[vertex] = current
```

```
            connected_node = connected_node.next
```

```
    else:
```

```
        # BFS in backward direction
```

```
        current = self.dest_queue.pop(0)
```

```
        connected_node = self.graph[current]
```

```
        while connected_node:
```

```
            vertex = connected_node.vertex
```

```
            if not self.dest_visited[vertex]:
```

```
                self.dest_queue.append(vertex)
```

```
                self.dest_visited[vertex] = True
```

```
                self.dest_parent[vertex] = current
```

```
            connected_node = connected_node.next
```

```
# Check for intersecting vertex
```

```
def is_intersecting(self):
```

```
    # Returns intersecting node
```

```
    # if present else -1
```

```
    for i in range(self.vertices):
```

```

        if (self.src_visited[i] and
            self.dest_visited[i]):
            return i

    return -1

# Print the path from source to target
def print_path(self, intersecting_node,
               src, dest):

    # Print final path from
    # source to destination
    path = list()
    path.append(intersecting_node)
    i = intersecting_node

    while i != src:
        path.append(self.src_parent[i])
        i = self.src_parent[i]

    path = path[::-1]
    i = intersecting_node

    while i != dest:
        path.append(self.dest_parent[i])
        i = self.dest_parent[i]

    print("*****Path*****")
    path = list(map(str, path))

    print(' '.join(path))

# Function for bidirectional searching
def bidirectional_search(self, src, dest):

    # Add source to queue and mark
    # visited as True and add its
    # parent as -1
    self.src_queue.append(src)
    self.src_visited[src] = True
    self.src_parent[src] = -1

```

```

        # Add destination to queue and
        # mark visited as True and add
        # its parent as -1
        self.dest_queue.append(dest)
        self.dest_visited[dest] = True
        self.dest_parent[dest] = -1

    while self.src_queue and self.dest_queue:

        # BFS in forward direction from
        # Source Vertex
        self.bfs(direction = 'forward')

        # BFS in reverse direction
        # from Destination Vertex
        self.bfs(direction = 'backward')

        # Check for intersecting vertex
        intersecting_node = self.is_intersecting()

        # If intersecting vertex exists
        # then path from source to
        # destination exists
        if intersecting_node != -1:
            print(f"Path exists between {src} and {dest}")
            print(f"Intersection at : {intersecting_node}")
            self.print_path(intersecting_node,
                             src, dest)
            exit(0)

    return -1

# Driver code
if __name__ == '__main__':

    # Number of Vertices in graph
    n = 15

    # Source Vertex
    src = 0

    # Destination Vertex
    dest = 14

```

```
# Create a graph
graph = BidirectionalSearch(n)
graph.add_edge(0, 4)
graph.add_edge(1, 4)
graph.add_edge(2, 5)
graph.add_edge(3, 5)
graph.add_edge(4, 6)
graph.add_edge(5, 6)
graph.add_edge(6, 7)
graph.add_edge(7, 8)
graph.add_edge(8, 9)
graph.add_edge(8, 10)
graph.add_edge(9, 11)
graph.add_edge(9, 12)
graph.add_edge(10, 13)
graph.add_edge(10, 14)

out = graph.bidirectional_search(src, dest)

if out == -1:
    print(f"Path does not exist between {src} and {dest}")
```

7. Output: