CSS 422 Hardware and Computer Organization

Memory Hierarchy and Cache

Professor: Yang Peng

The slides are re-produced by the courtesy of Dr. Arnie Berger, Dr. Ross Ortega and Dr. Wooyoung Kim



Topics

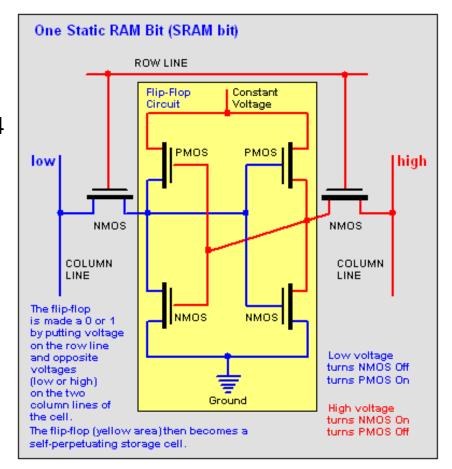
- Memory hierarchy
- Cache memory management
- Cache and performance
- Chapter 6 by Null
- Chapter 14 by Berger(Available online)



Memories: SRAM

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- Static Random-Access Memory
 - Value is stored using a pair of inverting gates
 - Fast, but takes up more space (4 to 6 transistors) than DRAM
 - Expensive



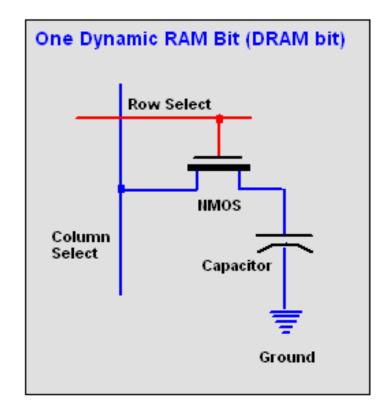


Memories: DRAM

- Dynamic Random-Access Memory
 - Value is stored as a charge on capacitor (must be refreshed)
 - Very small but slower than SRAM (factor of 5 to 10)
 - Cheap

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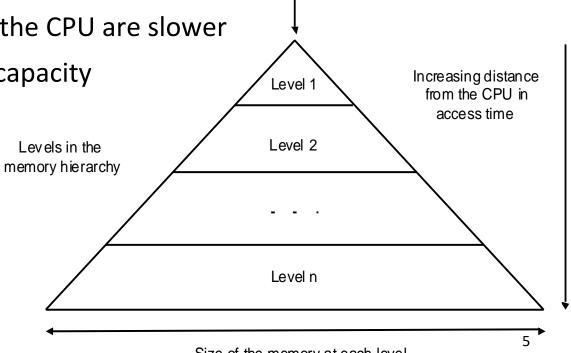
Memory Hierarchy

- Memory Hierarchy
 - Levels closer to the CPU are faster
 - Relatively small capacity
 - SRAM

Levels further from the CPU are slower

Relatively large capacity

DRAM



CPU



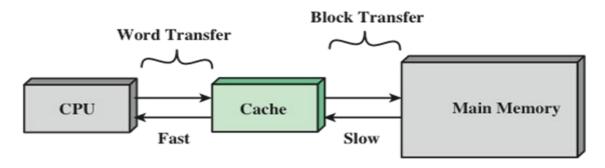
Locality

- If an item is referenced (read or write)
 - Temporal locality says
 - It will tend to be referenced again soon
 - Spatial locality says,
 - Nearby items will tend to be referenced again soon
- Our initial focus: two-level hierarchy (upper and lower)
 - Upper level is cache memory, lower level is main memory
 - Definitions
 - Block: the minimum unit of data
 - Hit: data requested is in the cache (upper level)
 - Miss: data requested is not in the cache (upper level)

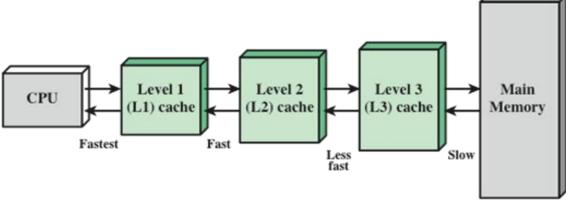


Cache and Main Memory

 A computer might have one or more caches between CPU and main memory

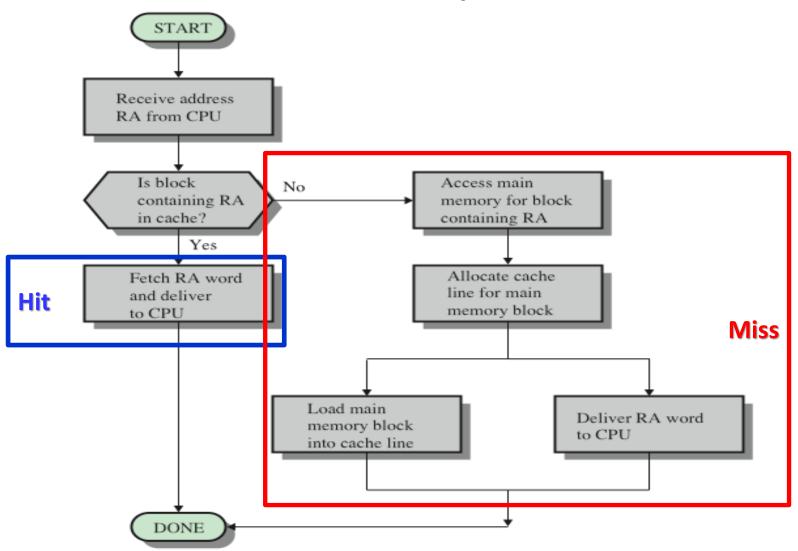


- L1 cache usually means "On-chip" cache
- L2/L3 caches between the CPU and a main memory





Cache Read Operation





Effective Execution Time (EET)

- Block: unit of data transfer (called refill line as well)
- Hit Rate: percentage of accesses found in cache
- Miss Rate: percentage of accesses not in cache (1 hit rate)
- Hit Time: time to access cache
- Miss Penalty: time to replace a block in cache with appropriate data in main memory (replace a whole block, not a single byte)
- Effective Execution Time (EET):
 - hit rate * hit time + miss rate * miss penalty
 - The goal is to achieve the minimum EET!
 - Decreasing the miss rate (simultaneously increasing hit rate) is an important method



Class Exercise

- 1. A certain processor has an on-chip cache with the following specifications:
 - Cache hit rate for the L1 cache is 98%
 - Instructions that are located in-cache execute in 1 clock cycle
 - Instructions that are not found in the on-chip cache will cause the processor to stop program execution and refill a portion of the cache. This operation takes 100 clock cycles to execute.
- **Q)** What is the effective execution time in nanoseconds for this processor if the clock frequency is 100 MHz?



Class Exercise

- 1. A certain processor has an on-chip cache with the following specifications:
 - Cache hit rate for the L1 cache is 98%
 - Instructions that are located in-cache execute in 1 clock cycle
 - Instructions that are not found in the on-chip cache will cause the processor to stop program execution and refill a portion of the cache. This operation takes 100 clock cycles to execute.
- **Q)** What is the effective execution time in nanoseconds for this processor if the clock frequency is 100 MHz?

Answer:

Clock cycle time = 1/100MHz = 10ns

EET = hit rate X hit time + miss rate X miss penalty

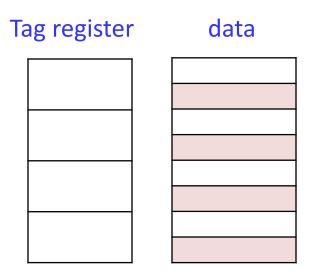
= 0.98 X 1 (clock cycle) X 10ns + 0.02 X 100 (clock cycle) X 10 ns

= 9.8 ns + 20 ns = 29.8 ns



Cache Organization

- Cache memory consists of a number of cache entries
 - Tag register: Holds the memory address and determines if there is a match to a CPU request
 - Data: Copies of the contents (instructions/data) of main memory



Cache Memory



Cache Design

- Goal: Increase the performance of using Caches
- Issues:
 - How to map the data in memory to the data in cache? How do we know if a data item is in the cache? If it is, how do we find it? (*Mapping Function*)
 - What happens if we change a data value in cache? (Write Policy)
 - What to replace when the cache is full? (Replacement Algorithm)
 - Is it a physical cache, or virtual cache? (Cache Address)
 - How big should be the Cache? (Cache Size)
 - How many adjacent data should come together in a cache? (*Line/Block Size*)
 - What is the optimal number of caches? (Number of Caches)

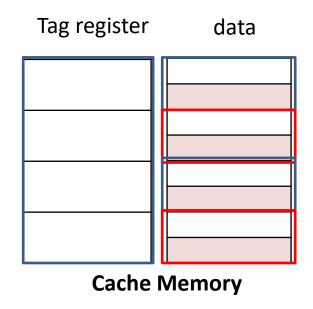


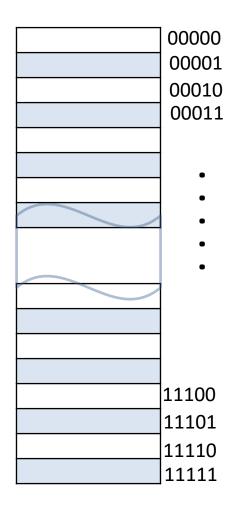
Mapping Function

- Processor can access the data/instruction by its address in main memory
- But, data in cache DOES NOT have an address!
- How to map the address of memory to some data in cache?
- Mapping Schemes
 - 1. Direct Mapping
 - 2. Associative Mapping
 - 3. Set-Associative Mapping



- Suppose a main memory system has 32-byte capacity
- The system is byte-addressable
- A direct-mapped cache has 8-byte capacity
- A block (refill line) has 2 bytes

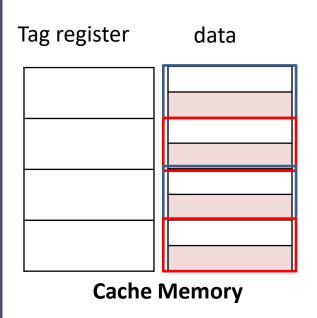


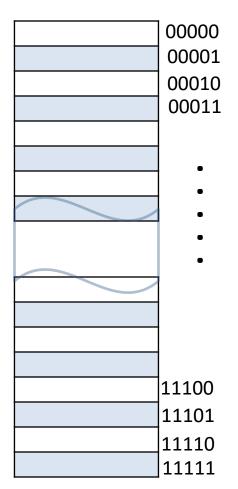


Main Memory



- Rearrange main memory as a number of columns (pages) so that each column (page) has the same size as the cache
- How many columns you can have when memory size is 32 bytes, cache is 8 bytes?







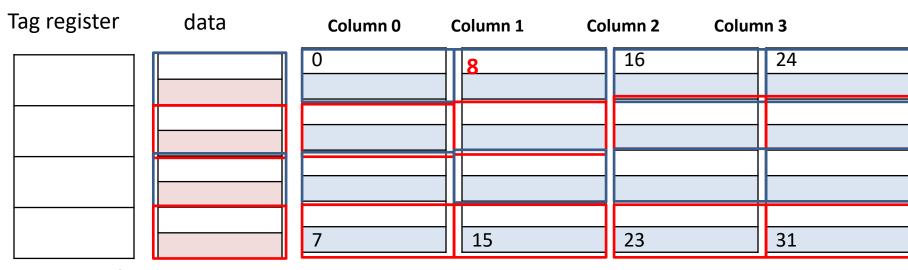
- Rearrange main memory as a number of columns (pages) so that each column (page) has the same size as the cache
- Main memory and caches are divided into equally sized blocks (refill lines)
 - Block (Line) size: Typically between 4 and 64 bytes long (must be power of 2)

Tag register	data	Column 0	Column 1 Co	lumn 2 Colum	ın 3
		0	8	16	24
		7	15	23	31

Cache Memory



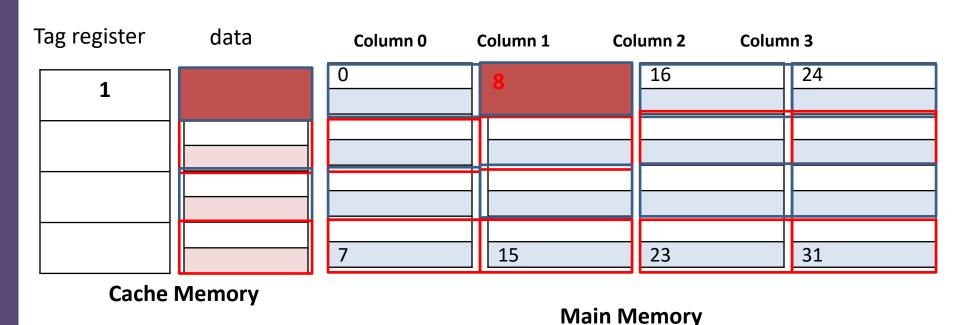
- Want to read data at address 8 (01000₂) in main memory into cache
- Map the Oth block (line) in main memory in any column (page) to the Oth block in cache



Cache Memory

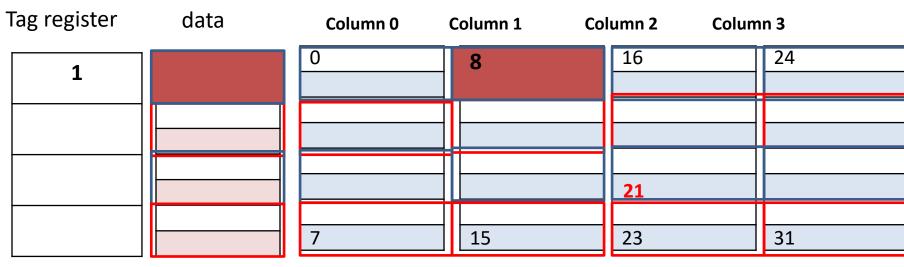


- Want to read data at an address 8 (01000₂) in main memory into cache
- Map the Oth block (line) in main memory in any column (page) to the Oth block in cache and update tag





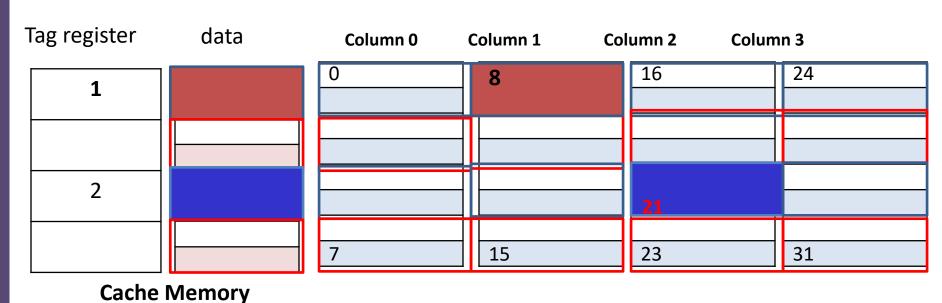
- Want to read data at an address 21 (10101₂) in main memory into cache
- Map the 2nd block (line) in main memory in any column (page) to the 2nd block in cache



Cache Memory



- Want to read data at an address 21 (10101₂) in main memory into cache
- Map the 2nd block (line) in main memory in any column (page) to the 2nd block in cache and update tag





- Mapping → map to the same block location
- What value is in the tag register?

The column (page) number

- How to calculate the tag value from an address?
- Address 8 → tag 1 and Address 21 → tag 2

Tag register	data	Column 0	Column 1 Co	lumn 2 Colum	ın 3
1		0	8	16	24
2				21	
		7	15	23	31

Cache Memory



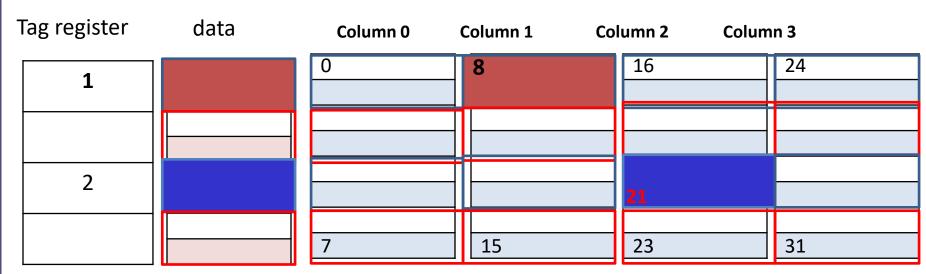
- Out of a 5-bit address, how many bits are for column number?
- The first two bits (since there are 4 pages)
 - 8 = $01000 \rightarrow \text{tag is } 01_2$
 - $21 = 10101_2 \rightarrow \text{tag is } 10_2$
- What are the other bits?

Tag register	data	Column 0	Column 1 Co	lumn 2 Colum	ın 3
1		0	8	16	24
2				21	
		7	15	23	31

Cache Memory



- Out of a 5-bit address, the first two bits (since there are 4 pages)
- What are the other bits?
- 8 = $01\ 00\ 0_2$ \rightarrow column 1, 0^{th} block, 0^{th} in the block
- $21 = 10 \ 10 \ 1_2 \rightarrow column \ 2$, $2^{nd} \ block$, $1^{st} \ in \ the \ block$



Cache Memory



Divide the address into tag, row and offset bits

- Memory size: L bytes
- Direct-mapped Cache size: M bytes
- The Cache block size: **K** bytes
- \rightarrow # Columns in a main memory: L/M \rightarrow # tag bit is $\log_2(L/M)$
- \rightarrow # Blocks in a cache memory: $M/K \rightarrow$ # row number bit is $log_2(M/K)$
- \rightarrow block size in a main memory: $K \rightarrow$ offset bit is $\log_2 K$

Tag Row/line	Offset
--------------	--------

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Direct Mapping - Example

Divide the address into tag, row and offset bits

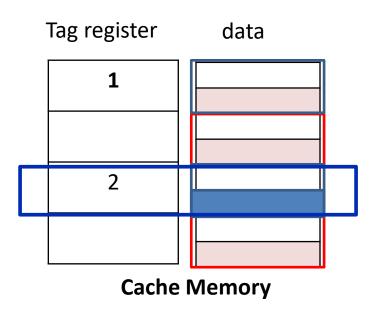
- Memory size: **32** bytes
- Direct-mapped Cache size: 8 bytes
- The Cache block size: **2** bytes
- \rightarrow # Columns in a main memory: 32/8 = 4 \rightarrow # tag bit is ?
- \rightarrow # Blocks in a main memory: 8/2 = 4 \rightarrow # row number bit is ?
- → block size in a main memory: 2 → offset bit is?

Tag (2)	Row/line (2)	Offset (1)
---------	--------------	------------



Find Hit/Miss in a Direct-Mapped Cache

- 1. Given an address $(21 = 10101_2)$
 - 1. get tag/block (10_2) , row (10_2) and offset (1_2)
- 2. Go to the same row (block: 10_2) in a cache, check the valid tag value in the tag register.
- 3. If the valid tag matches, then hit; otherwise miss.
- 4. When hit, then find the content in that offset location (1_2) in that block





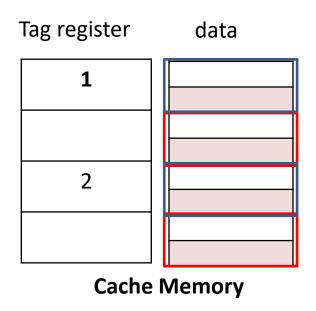
Find Hit/Miss in a Direct-Mapped Cache

Suppose that the length of address is 5 bits:

2-bit tag, 2-bit row, and 1-bit offset

From the following cache image, see if the followings are hit or miss

- 1) Address 9
- 2) Address 17
- 3) Address 29





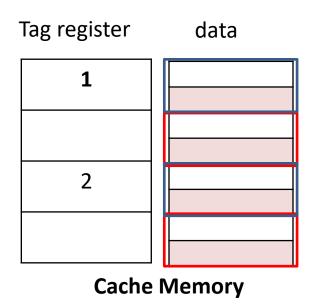
Find Hit/Miss in a Direct-Mapped Cache

Suppose that the length of address is 5 bits:

2-bit tag, 2-bit row, and 1-bit offset

From the following cache image, see if the followings are hit or miss

- 1) Address 9 = 01 00 1: block is 0, tag is 1 (hit)
- 2) Address 17 = 10 00 1: block is 0, tag is 2 (miss: not matches 1)
- 3) Address 29 = 11 10 1: block is 2, tag is 3 (miss: not matches 2)





Class Exercise: Direct-Mapped Cache

- Main memory: 2¹⁴ bytes
- Cache: direct-mapped
 - 16 blocks (refill lines)
 - Each block has 8 bytes

Q1) What is the size of cache?

Now we will divide the address bits:

Q2) How many bits for the offset (where is the data within a block)?

Q3) How many bits for line number (what is the block number)?

Q4) How many bits for tag (What is the number of pages in a main memory)?

Class Exercise: Direct-Mapped Cache

- Main memory: 2¹⁴ bytes
- Cache: direct-mapped
 - 16 blocks (refill lines)
 - Each block has 8 bytes
- Q1) What is the size of cache?
- 16 blocks X 8 bytes = 2^7 bytes
- Q2) How many bits for the offset?

 Each block has 8 bytes. So, 3 bits for the offset.
- Q3) How many bits for block (row/line) number?

Each page has 16 blocks (same as the cache). So, 4 bits for the block number. (Or the row/line number)

Q4) How many bits for tag (What is the number of pages in a main memory)? Each page should be the same size with cache. 14 - 3 - 4 = 7 bits for tag





Limitation of Direct-Mapped Cache

- What if you repeatedly access the data of the same block but from different pages? (swapping the blocks causes lots of miss penalty)
- Example

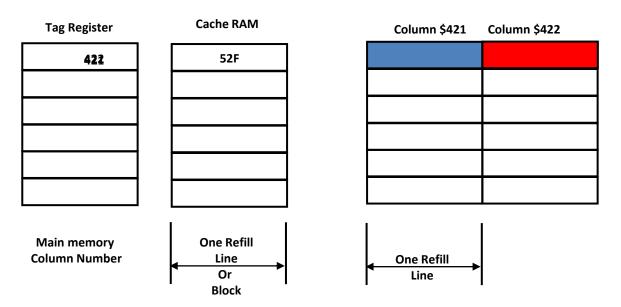
```
Loop: JSR subroutine ($10854BCA)
{...}
BNE loop
Subroutine: {...} ($10894BC0)
RTS
```

- \$10854BCA
 - Offset: 0xx0A, **Row = 0x52F**, Column (page) = 0x0421
- \$ 10894BC0
 - Offset: 0xx00, **Row = 0x52F**, Column (page) = 0x0422



Limitation of Direct-Mapped Cache

- \$10854BCA
 - Offset: 0xx0A, **Row = 0x52F**, Column (page) = 0x0421
- \$ 10894BC0
 - Offset: 0xx00, **Row = 0x52F**, Column (page) = 0x0422



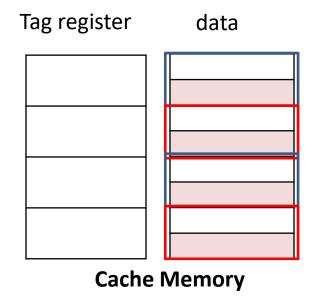


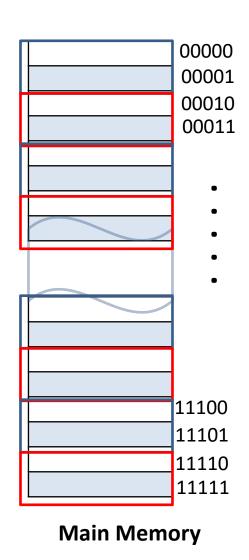
Associative Cache



Associative Cache

- Rearrange the main memory based on the size of a block (refill line size)
- number of columns = number of blocks

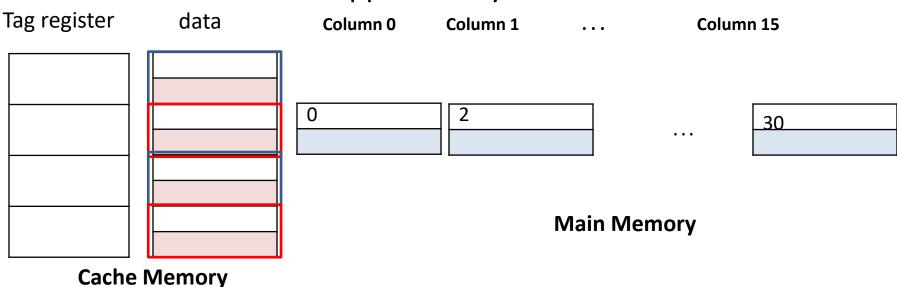






Associative Cache

- Rearrange the main memory based on the size of a block (refill line size)
- Each column is one block
 - number of columns = number of blocks
- Each block can be mapped to any available block



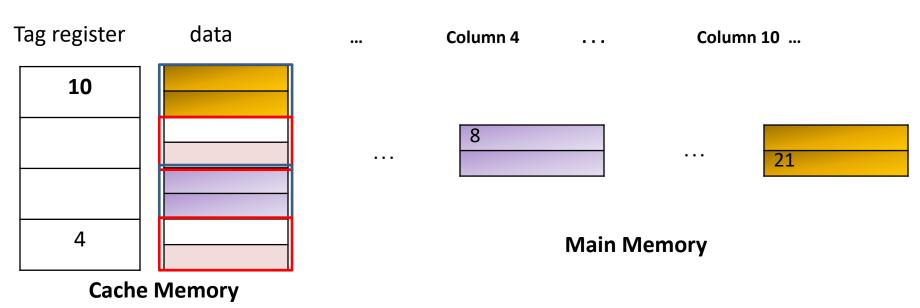


Associative Cache

- Data at address 8 will be at the column 4: $8 = 0100 \, O_2$
- Data at address 21 will be at the column 10: $21 = 1010 1_2$



Map any main memory block to any available cache block





Associative Cache

Divide the address into tag and offset (No ROW number!!)

- Memory size: L bytes
- Associative Cache size: M bytes
- Cache block size: K bytes
- \rightarrow # Columns in a main memory: L/K \rightarrow # tag bit is $\log_2(L/K)$
- \rightarrow Block size in a main memory: $K \rightarrow$ offset bit is $\log_2(K)$

Tag Offset



Associative Cache - Example

Divide the address into tag and offset (No ROW number!!)

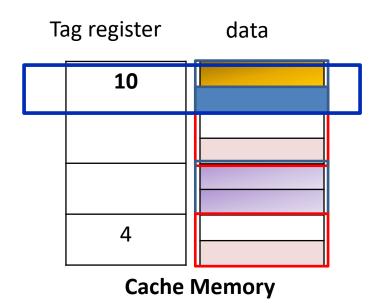
- Memory size: 32 bytes
- Associative Cache size: 8 bytes
- Cache block size: 2 byte
- \rightarrow # Columns in a main memory: 32/2 = 16 \rightarrow # tag bit is ?
- → block size in a main memory: 2 → offset bit is?

Tag (4)	Offset (1)
---------	------------



Find Hit/Miss in an Associative Cache

- 1. Given a memory address (21), get tag (1010_2 =10) and offset (1)
- 2. Search the Tag register to find the block whose tag matches $(1010_2=10)$
- 3. If found the matching tag, then hit; otherwise miss.
- 4. When hit, then find the content in the cache block which is at the offset location





Class Exercise: Associative Cache

- Main memory: 2¹⁴ bytes
- Cache: associative cache
 - 16 blocks (refill lines)
 - Each block has 8 bytes
- Q1) What is the size of cache?
- Q2) How many bits for the offset? (where the data within in a block)
- Q3) How many bits for block (line) number?

Q4) How many bits for tag (What is the number of pages in a main memory)?



Class Exercise: Associative Cache

- Main memory: 2¹⁴ bytes
- Cache: associative cache
 - 16 blocks (refill lines)
 - Each block has 8 bytes
- Q1) What is the size of cache?
- 16 blocks X 8 bytes = 2^7 bytes
- Q2) How many bits for the offset? (where the data within in a block)
- Each block has 8 bytes. So, 3 bits for the offset
- Q3) How many bits for block (line) number?
- No block number. Any main memory block can be mapped to any cache block.
- Q4) How many bits for tag (What is the number of pages in a main memory)?
- bits for tag = 14 3 = 11 bits.
- Conceptually, each block can be a page.



Limitation of Associative Cache

- 1. Should search all the blocks (rows) in a cache to find the matching tag (no block number information embedded in the address)
 - Complex hardware is needed for address comparisons if main memory is large

- 2. When cache is full, what should be removed (victim block) when a new block should be loaded into cache?
 - Need replacement algorithm (will cover later)



Set-Associative Cache

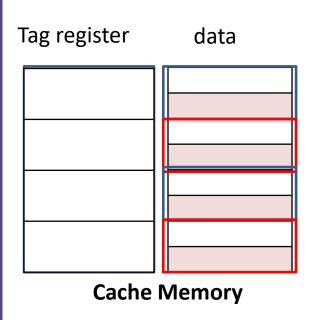


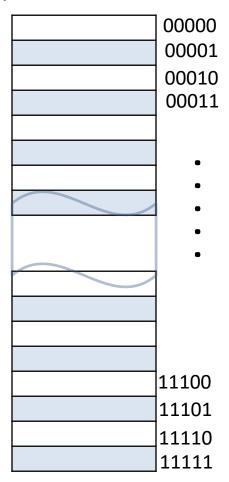
Set-Associative Cache

- Also called N-way set-associative cache
- Combines the properties of the direct-mapped and associative cache into one system
 - Direct-mapped Cache is very restrictive
 - Associative Cache is very expensive in terms of search
 - So, combine those two → Set-Associative Cache
 - Most commonly used in modern processors (4-way set-associative cache)
- N-way set-associative
 - Divide the cache into multiple sets
 - N is the number of blocks in a set
 - !!! N is not the number of sets !!!



- Suppose a byte-addressable main memory system is 32-byte capacity
- A 2-way set-associative cache has 8-byte capacity
- A block has 2 bytes

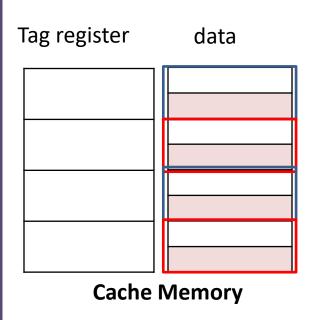


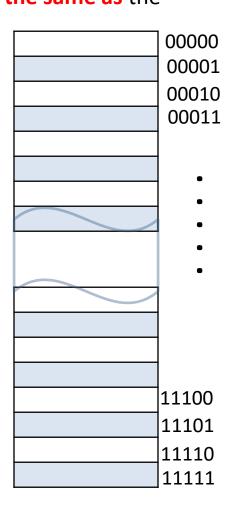




 Rearrange main memory as a number of columns (pages) so that the number of blocks in each column (page) is the same as the

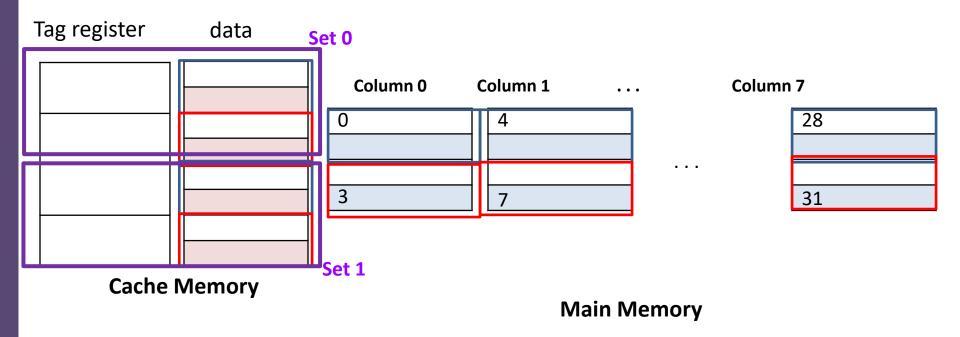
number of cache sets





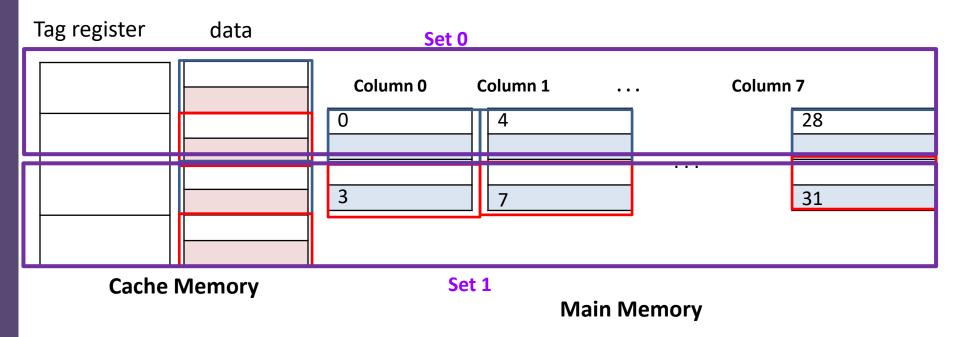


- Rearrange main memory so that 2 blocks in a cache map to each block in a column
- Two blocks in the cache is in the same set



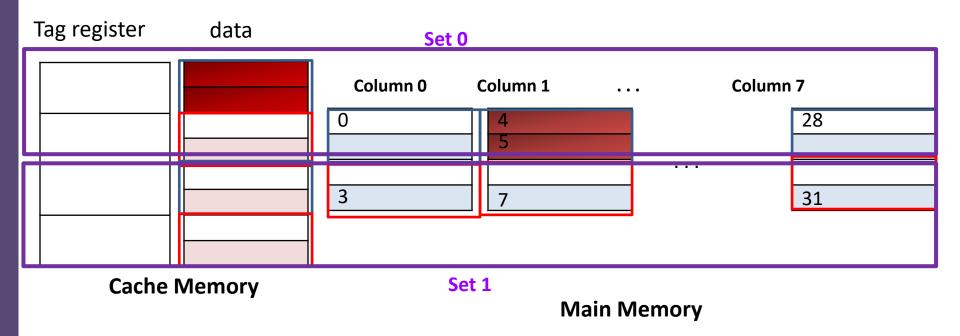


Want to read data at address 5(001012) in main memory into a cache



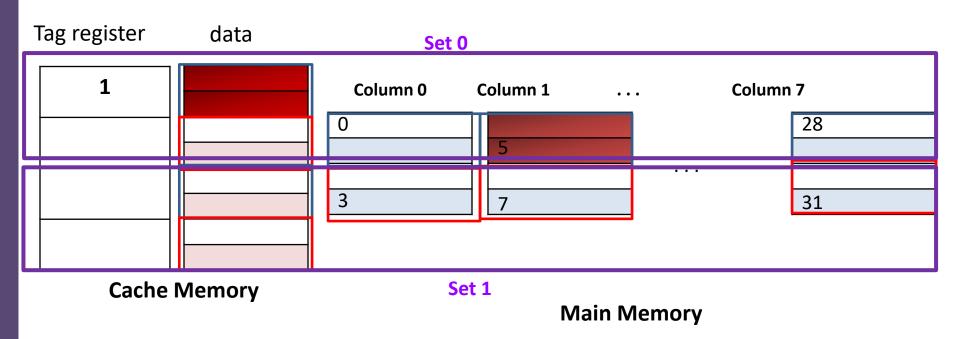


- Want to read data at address 5 (00101₂) in main memory into a cache
- Map the 0th block in main memory to any available block in the 0th set of cache





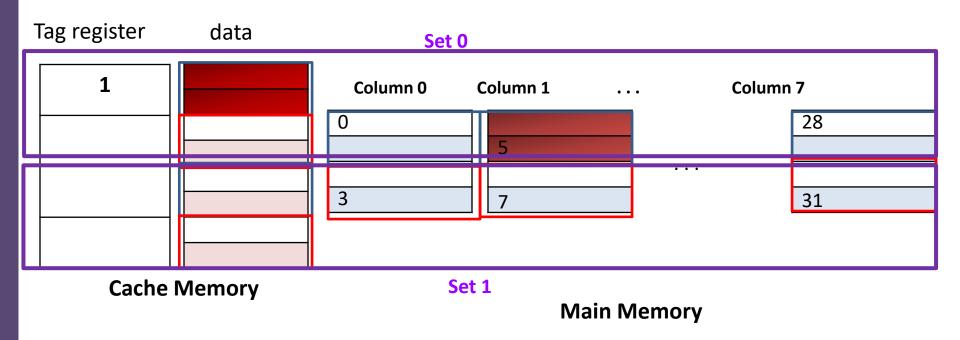
- Want to read data at address 5(00101₂) in main memory into a cache
- Map the Oth block in main memory to any available block in the Oth set of cache and update tag register



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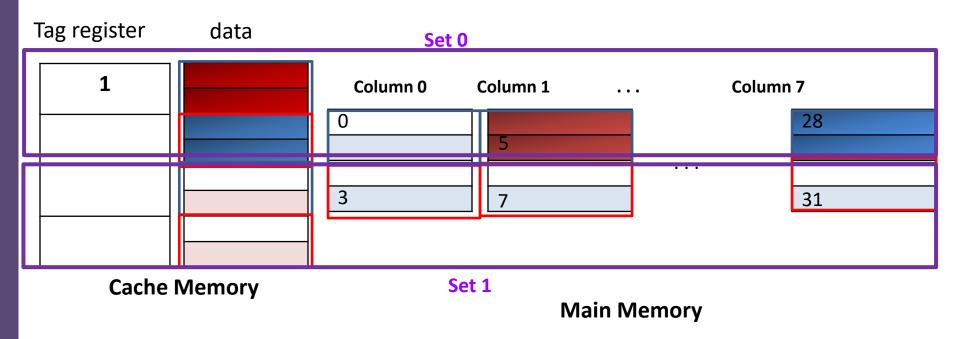


• Want to read data at address 28 (11100₂) in main memory into a cache



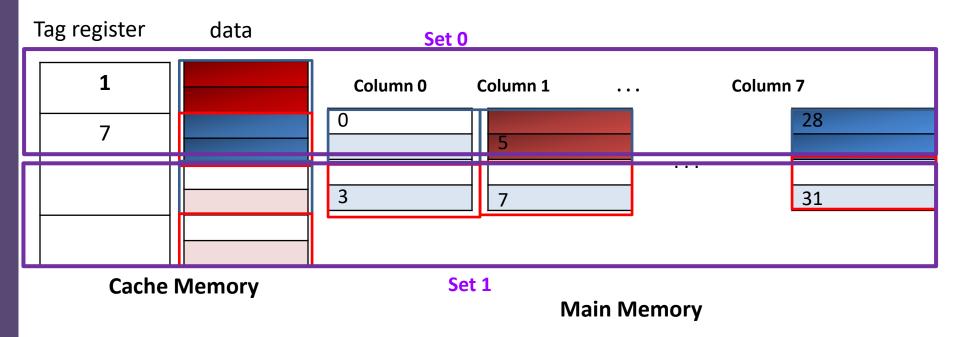


- Want to read data at address 28 (11100₂) in main memory into a cache
- Map the 0th block in main memory to any available block in the 0th set of cache



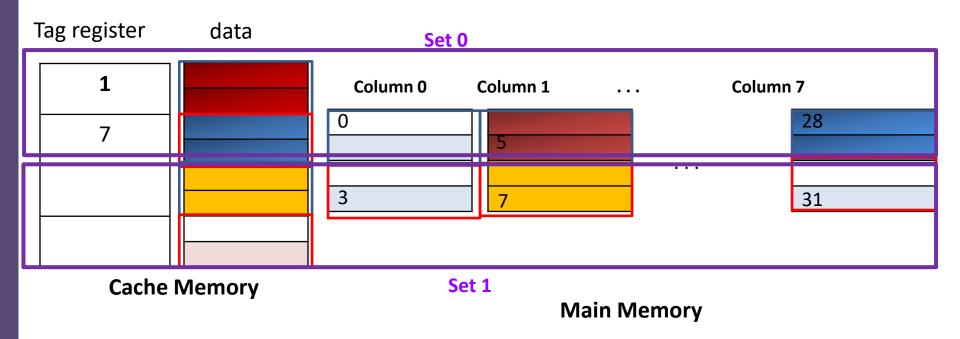


Want to read data at address 7 (00111₂) in main memory into a cache



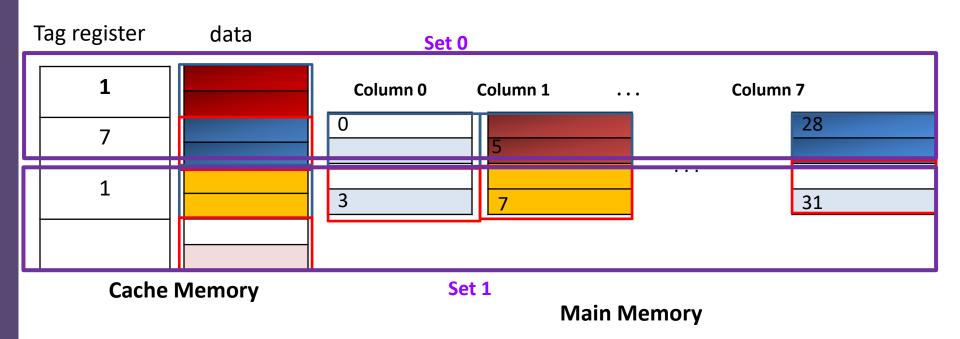


- Want to read data at address **7** (00111₂) in main memory into a cache
- Map the 1st block in main memory to any available block in the 1st set of cache





- Want to read data at address 7 (00111₂) in main memory into a cache
- Map the 1st block in main memory in to any available block in the 1st set of cache and update tag register



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Divide the address into tag, set and offset bits

- Memory size: L bytes
- N-Way Set-Associative Cache size: M bytes
- The Cache block size: K bytes
- \rightarrow Block size in a main memory: $K \rightarrow$ offset bit is $log_2(K)$
- \rightarrow # of sets in a cache: # blocks/N = (M/K)/N \rightarrow # set bit is $\log_2((M/K)/N)$
- → # Columns (Tag) in a main memory: L/((M/K)/N * K) = L/(M/N)

 \rightarrow # tag bit is $\log_2(L/(M/N))$

Tag	Set	Offset



N-way Set-Associative Cache - Example

Divide the address into tag, set and offset bits

- Memory size: 32 bytes (total address 5 bits)
- 2-way set-associative Cache size: 8 bytes
- The Cache block size: 2 bytes
- → Block size in a main memory: 2 → offset bit is?
- \rightarrow # of sets in a cache = # blocks/N = 4/2 \rightarrow # set bit is ?
- \rightarrow # Columns in a main memory: 32/(8/2) \rightarrow # tag bit is ?

Tag (3) Set (1	Offset (1)
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Set-Associative Cache

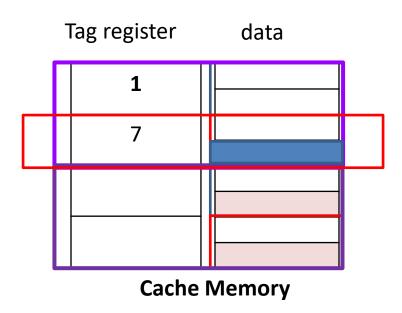
- Equivalent to a multiple column direct mapping
 - Example: 2-way set-associative cache has two blocks in a set

- The main memory address is partitioned into three pieces
 - Tag, **Set**, Offset



Find Hit/Miss in a Set-Associative Cache

- 1. Given a memory address (29 = 11101_2), get tag (111_2), set (0) and offset (1)
- 2. Go to the set (set 0) in a cache, search for a block in a set whose tag is matched $(111_2 = 7)$
- 3. If the tag matches, then hit; otherwise miss.
- 4. When hit, then find the content in the cache block which is at the offset location





Class Exercise: Set-Associative Cache

- Main memory: 2¹⁴bytes
- Cache: 2-way set-associative cache
 - 16 blocks (refill lines)
 - Each block has 8 bytes
- Q1) What is the size of cache?
- Q2) How many bits for the offset? (where the data within in a block)
- Q3) How many bits for set?
- Q4) How many bits for the tag (What is the number of pages in a main memory)?

Class Exercise: Set-Associative Cache

- Main memory: 2¹⁴bytes
- Cache: 2-way set-associative cache
 - 16 blocks (refill lines)
 - Each block has 8 bytes

Q1) What is the size of cache?

16 blocks X 8 bytes = 2^7 bytes

Q2) How many bits for the offset?

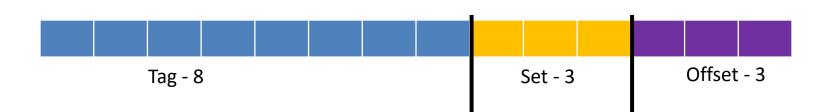
Each block has 8 bytes. So, 3 bits for the offset.

Q3) How many bits for set?

There are total 16 blocks, and each set has 2 blocks. So there are total 8 sets. So, 3-bits.

Q4) How many bits for the tag (What is the number of pages in a main memory)?

bits for tag = 14 - 3 - 3 = 8 bits.





Cache Mapping Function – Summary

Directed mapping

- The main memory address is divided into Tag, Row and Offset bits
- Tag bit matches the log of the number of columns in a main memory
- Each column has the same size with the cache
- One to one mapping between blocks in memory and cache restrictive

(Fully) Associative mapping

- The main memory address is divided into Tag and Offset bits
- Conceptually each block is one column
- Any block from main memory can be mapped any available cache block
- Expensive as search is needed to find matching tag

N-way set-associative mapping

- The main memory address is divided into Tag, Set and Offset bits
- Blocks are mapped within a set



Class Exercise

A certain processor has an on-chip cache with the following specifications:

- 32-bit wide address and data busses
- On-chip instruction cache is 64K bytes, organized as a 4-way set-associative
- Cache block size (refill line) = 64 bytes
- Average cache hit rate = 95%
- Instructions located in cache execute in 1 clock cycle
- For this memory design burst accesses from main memory requires
 - an address set-up time of 5 clock cycles
 - then each subsequent burst fetch from main memory requires 2 clock cycles per memory fetch
- **Q)** What is the effective execution time (EET) in nanoseconds for this processor if the clock frequency is 100 MHz?



Class Exercise

From the lecture notes we recall that:

- 1 clock cycle = 1/100MHz = 10 ns
- Effective execution time = hit rate * hit time + miss rate * miss penalty
- Hit rate: 0.95: Miss rate: 0.05
- Hit time = 1 clock cycle * 10 ns
- Miss time = (burst memory access + read all 64 bytes (in a block))*10ns = (5 + 2*(64/4))*10 ns = 370 ns

Note: If we have a cache miss, then the processor must refill one block in the cache. Since this is a 32-bit processor, we can read a maximum of 4 bytes at once. Thus, we must read main memory 64/4 or 16 times.

Since each external memory fetch requires 2 cycles, the memory read requires 16x2 = 32 clock cycles. However, we also have the overhead of setting up the address. This takes 5 clock cycles. Each clock cycle is 10 ns, so the miss penalty causes a total time delay of 370 ns:

Effective Execution Time = 0.95*10 + 0.05*370 = 9.5 + 18.5 = 28 ns



Cache Write Strategies

- Cache behavior is relatively straight-forward until new data must be stored
 - If data is updated and stored in the cache:
 - Cache image and memory image are no longer the same (coherent)
- Cache activity with respect to data writes can be of two types:
 - Write-through cache:
 - Data is written to the cache AND main memory at the same time
 - Write-back (post-write)cache:
 - Data is **held until** bus activity allows the data to be written without interrupting other operations
 - May also wait until it has an entire block of data to be written
- A memory cell that has an updated value still in cache is called a dirty cell



Cache Write Strategies (2)

- If the data image is not in cache
 - Write-around cache: Non-cached data is immediately written to memory (do not go through cache)
 - Or, if there is a cache block available with no corresponding dirty memory cells, it may store the data in that cache first,
 - Then do a write-through, or post-write, depending upon the design



Hits vs. Misses

- Read hits
 - this is what we want
- Read misses
 - stall the CPU, fetch block from memory, deliver to cache, restart
- Write hits
 - can replace data in cache and memory (write-through)
 - write the data only into the cache (write-back the cache later)
- Write misses
 - write-around cache, or
 - read the entire block into the cache, then write the data



Simplified Model

```
execution time = (execution cycles + stall cycles) \times cycle time stall cycles = # of instructions \times miss ratio \times miss penalty
```

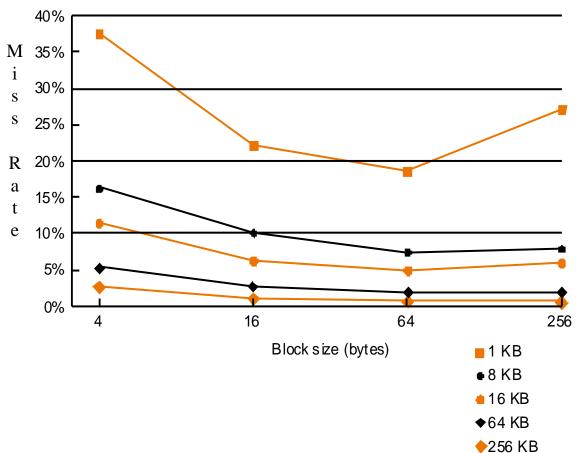
- Two ways of improving performance
 - decreasing the miss ratio
 - Increase the block size
 - What will happen if the block size is too large?

Larger miss penalty!

decreasing the miss penalty



- Optimal block size?
- Increasing the block size (refill line) tends to decrease miss rate:



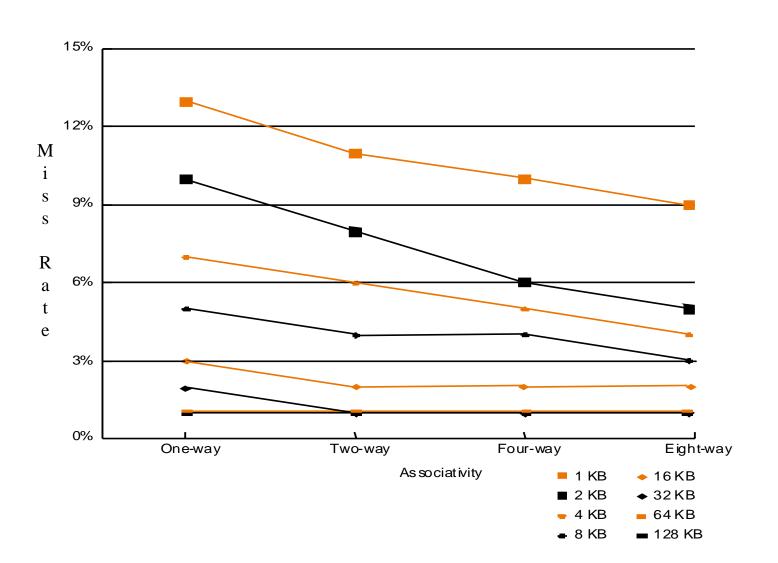


- How to improve the performance further?
- Use split caches because there is more spatial locality in code
 - Data cache (D-cache)
 - Instruction cache (I-cache)
- Cache performance can be impacted by the nature of the software running on the computer
 - By association, the performance of the cache may be influenced by the compiler used to create the code image
- Cache behavior can dramatically improve or diminish software performance

Program	Block size in words	Instruction miss rate	Data miss rate	Effective combined miss rate
gcc	1	6.1%	2.1%	5.4%
	4	2.0%	1.7%	1.9%
spice	1	1.2%	1.3%	1.2%
-	4	0.3%	0.6%	0.4%



Optimal set number?





Decreasing Miss Penalty with Multilevel Caches

- Add a second level (level two) cache:
 - Often primary cache is on the same chip as the processor
 - Use SRAMs to add another cache above primary memory (DRAM)
 - Miss penalty goes down if data is in 2nd level cache
- Using multilevel caches:
 - Try and optimize the hit time on the 1st level cache
 - Try and optimize the miss rate on the 2nd level cache



Elements of Cache Design

- Mapping function
 - Direct
 - Associative
 - Set-Associative
- Write Policy
 - Write through
 - Write back
- Replacement Algorithm
 - First in first out (FIFP)
 - Random
 - Least frequently used (LFU)
 - Least recently used (LRU)

- Cache Address
 - Logical
 - Physical
- Cache Size
- Line Size
- Number of Caches
 - Single or two level
 - Unified or split