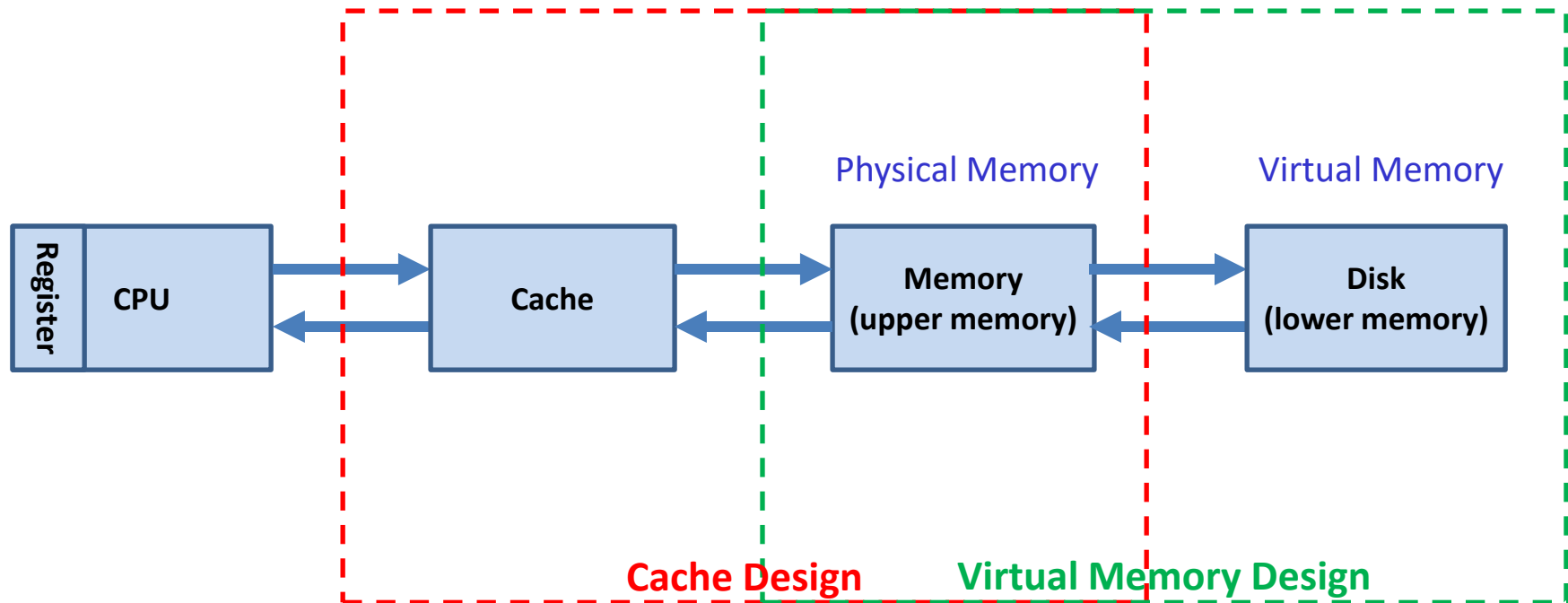


# LRU Algorithm

Professor: Yang Peng

The slides are re-produced by the courtesy of  
Dr. Arnie Berger, Dr. Ross Ortega and Dr. Wooyoung Kim

# Accessing Memories in a Computer System



# Replacement Policy

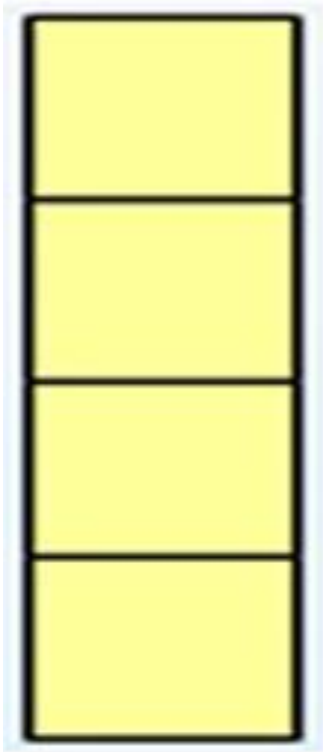
- When all the blocks in cache are used, we need to find a “**victim**” block to refill, where we need a ***Replacement Policy***
- *Optimal replacement policy*: impossible to implement as it should predict all the future cache references completely

# Three Most Common Replacement Policies

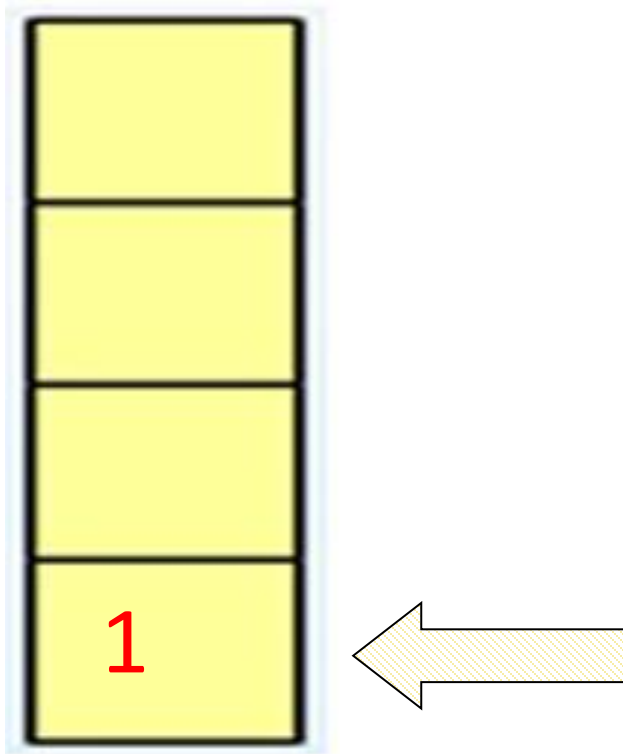
- ***First-In, First-Out (FIFO)***
  - Throw away the frame that has been in the cache the longest, regardless of when it was last used
- ***Random***
  - Picks a frame at random and replaces it with a new one
  - Disadvantage: Can certainly evict a frame that will be needed often or needed soon
- ***Least Recently Used (LRU)***
  - Evicts the frame that has been unused for the longest period of time
  - Disadvantage: Complex, as it has to maintain an access history for each block, which ultimately slows down the cache.

# Implementing an LRU Stack

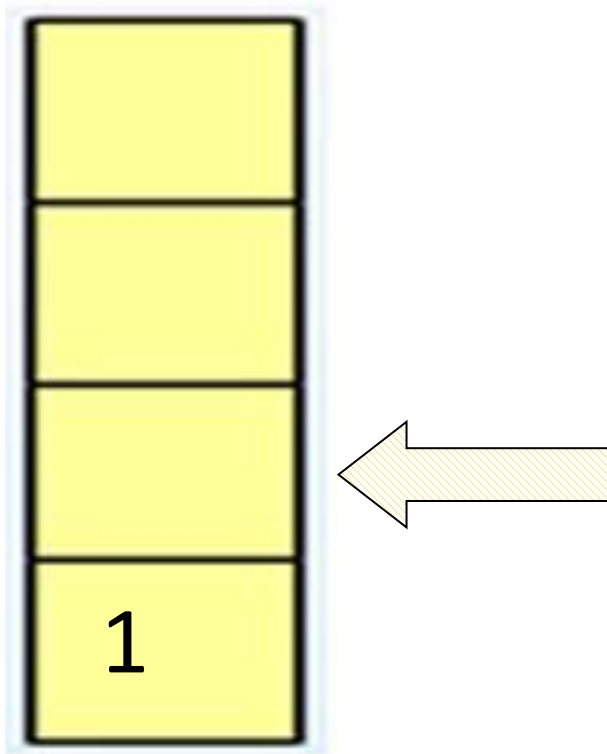
REF string: 1 5 3 1 6 2 3



REF string: 1 5 3 1 6 2 3

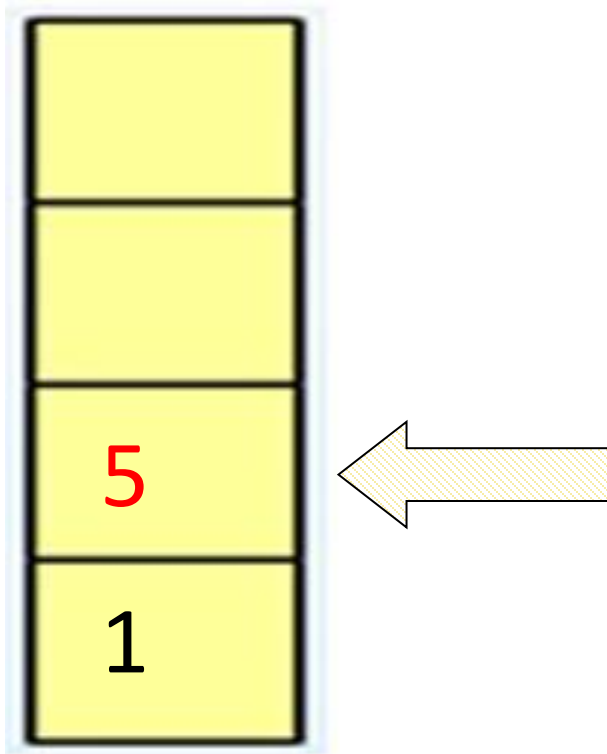


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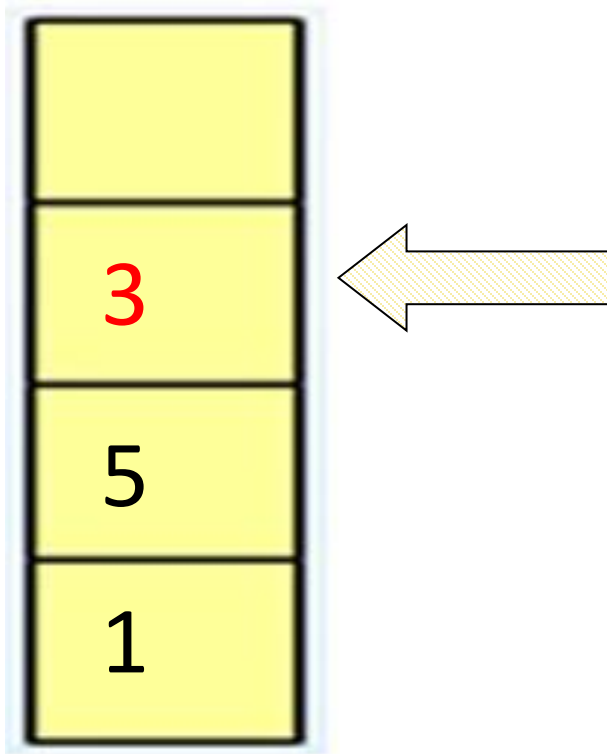




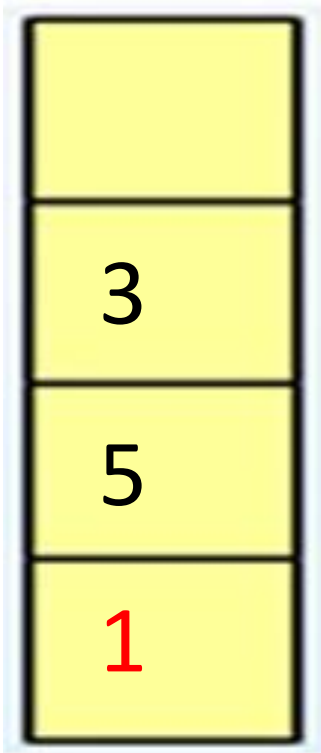
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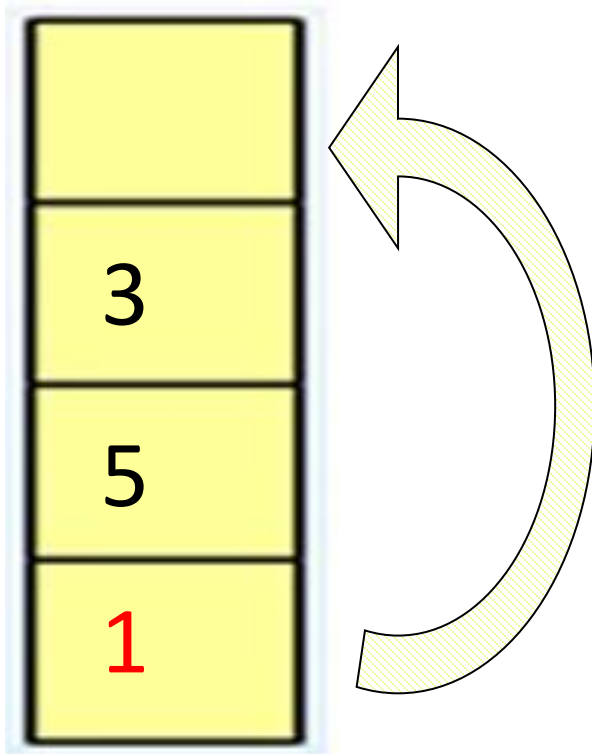
REF string: 1 5 3 1 6 2 3



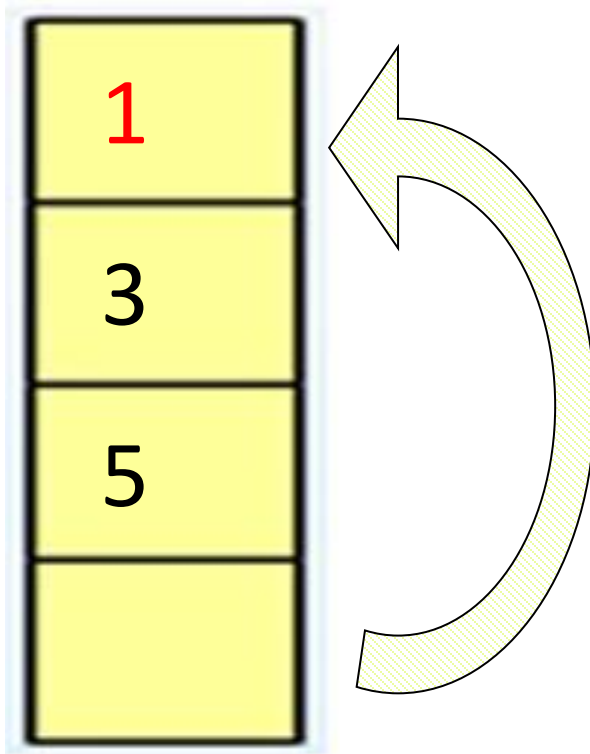
REF string: 1 5 3 **1** 6 2 3



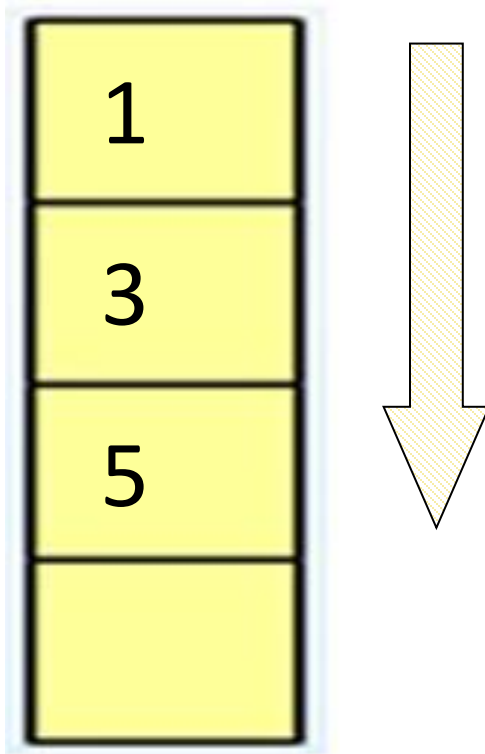
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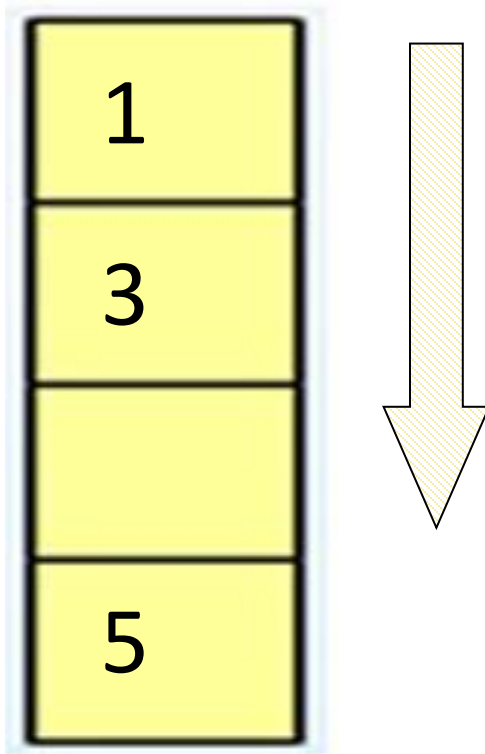
REF string: 1 5 3 **1** 6 2 3



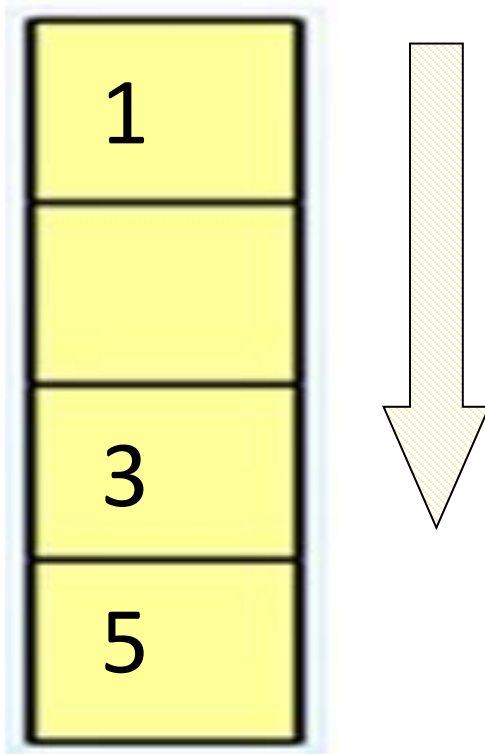
REF string: 1 5 3 **1** 6 2 3



REF string: 1 5 3 **1** 6 2 3

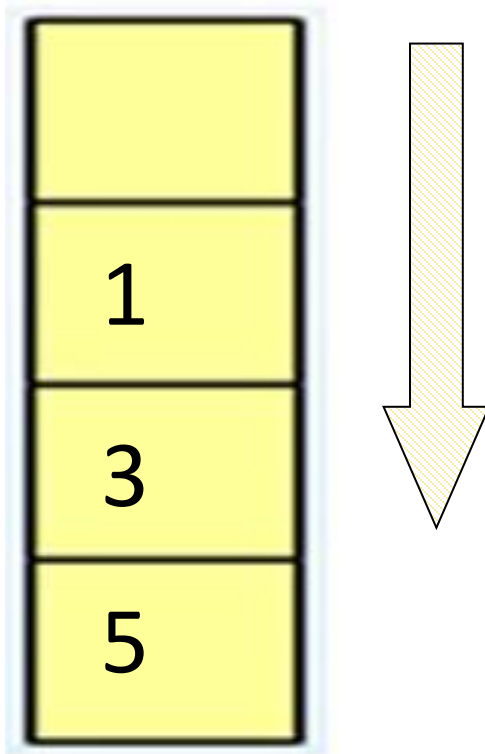


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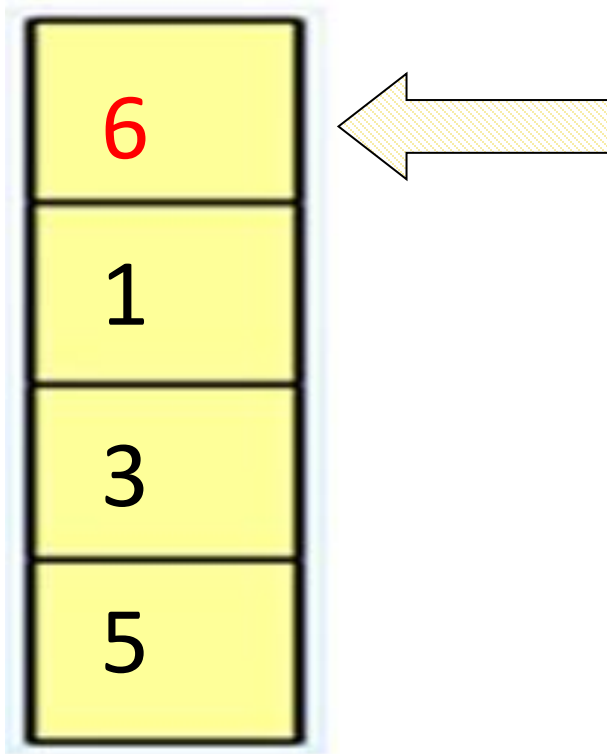




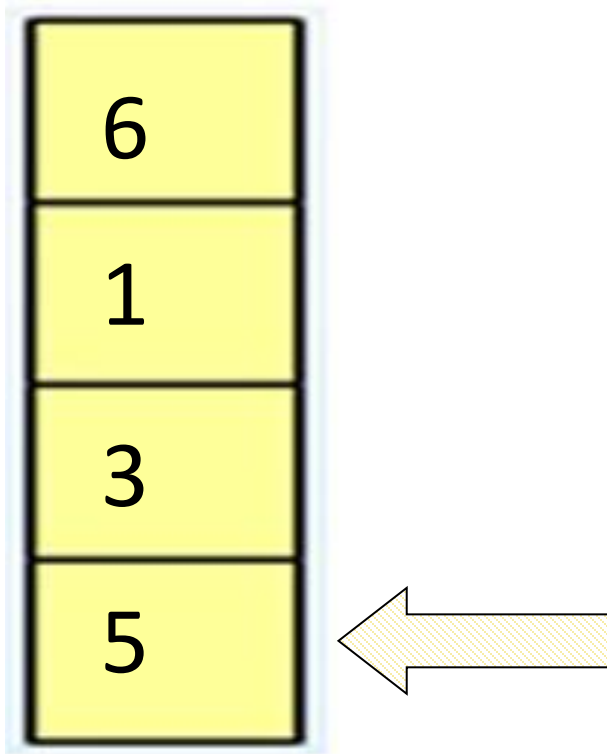
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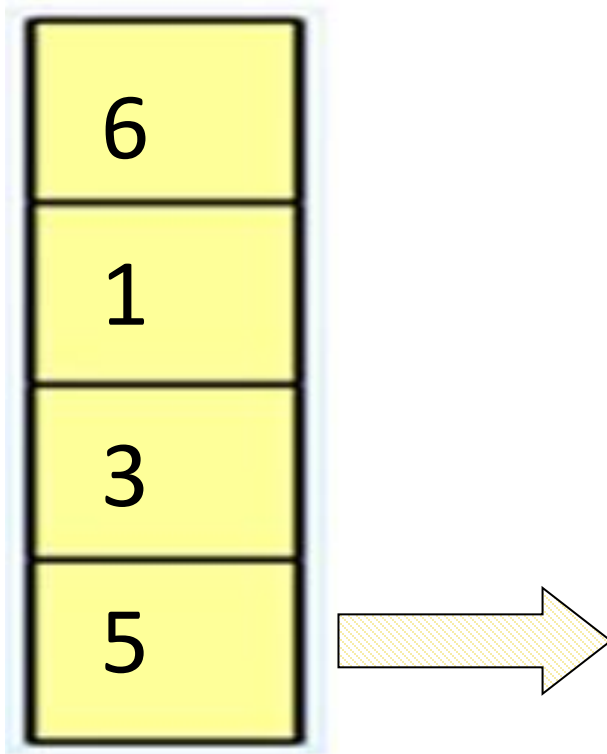
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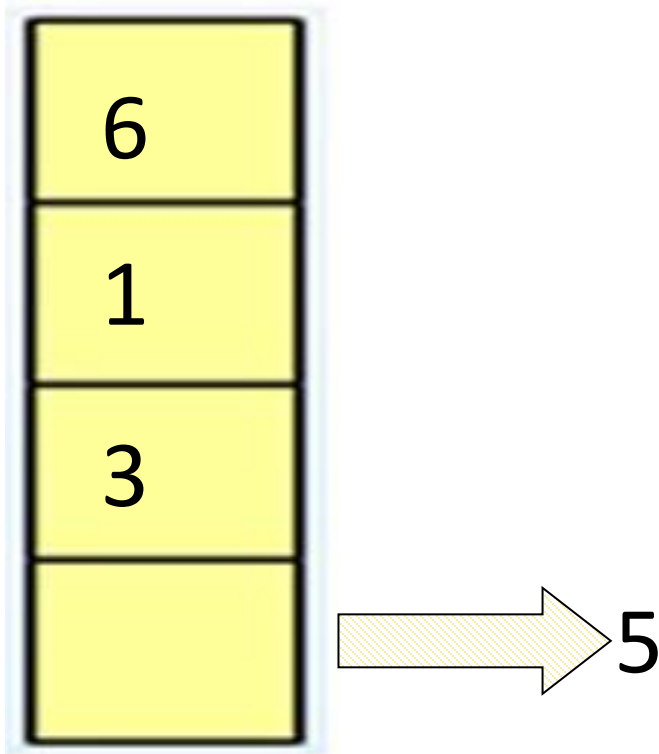
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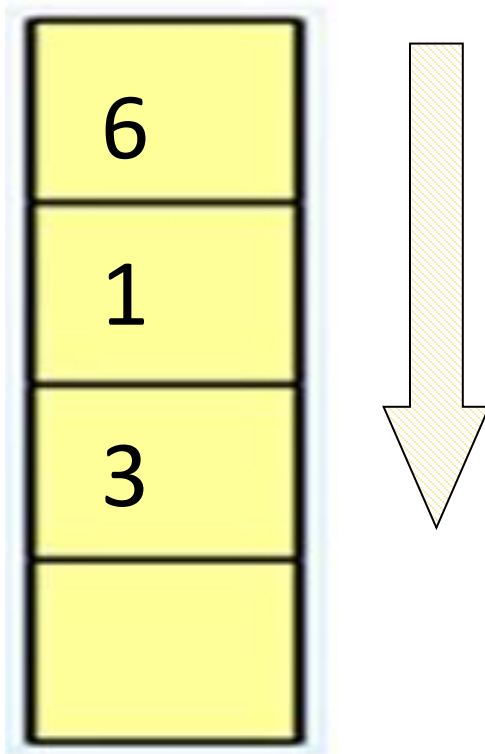
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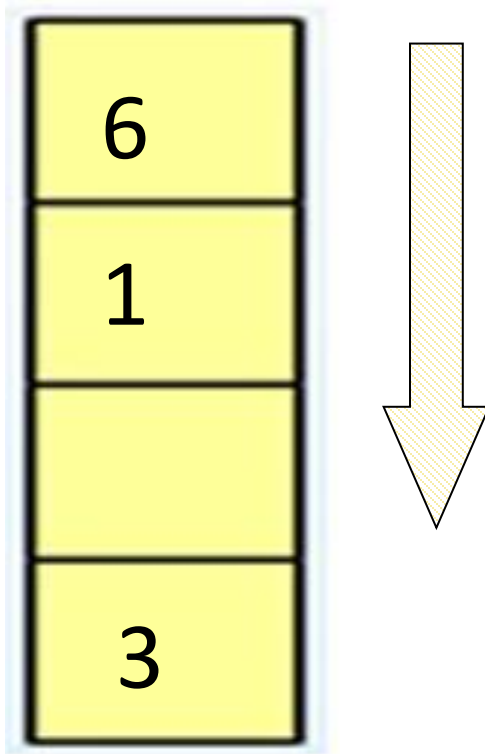
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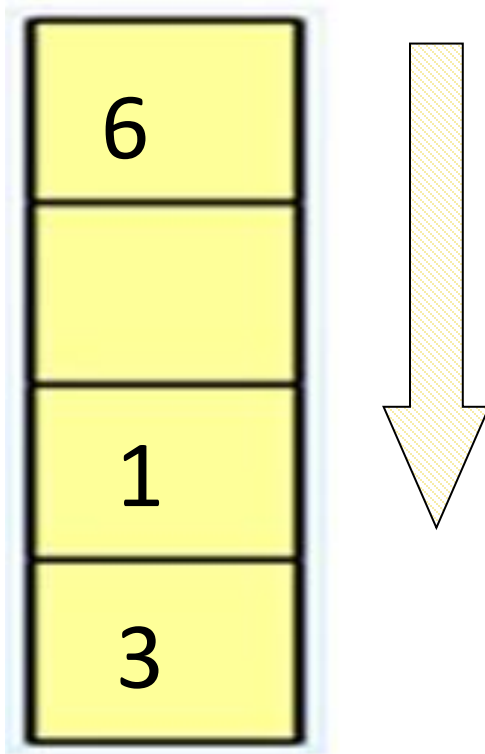
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REF string: 1 5 3 1 6 **2** 3

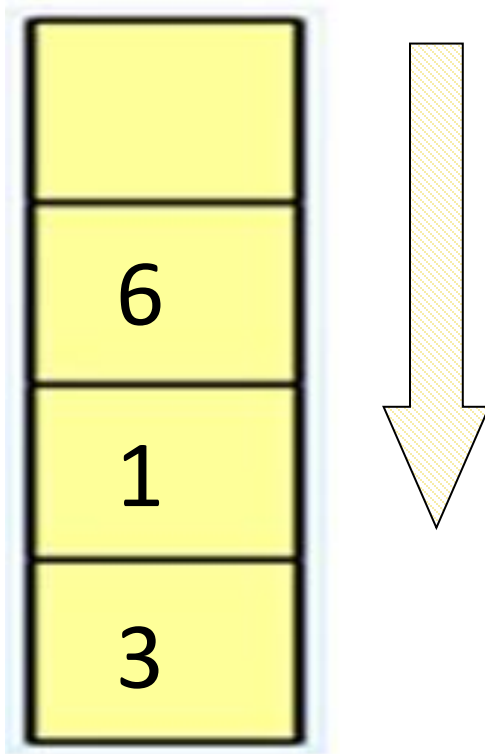


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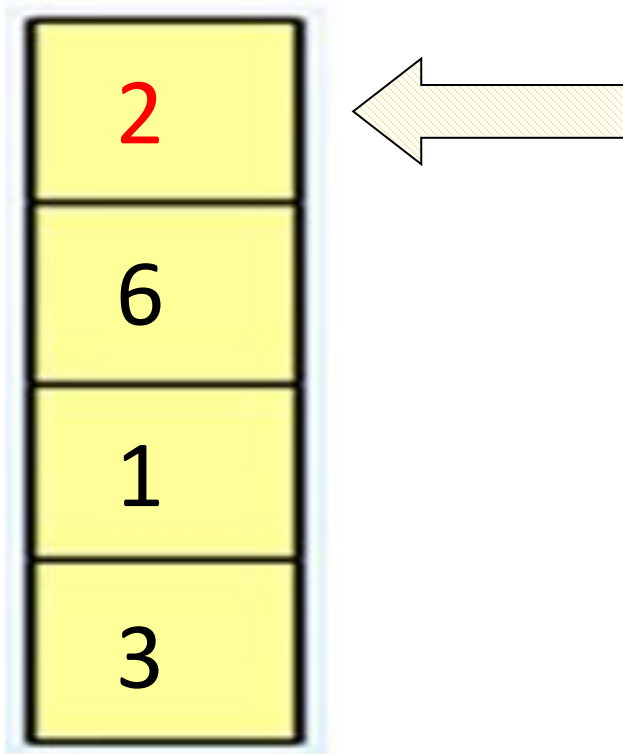




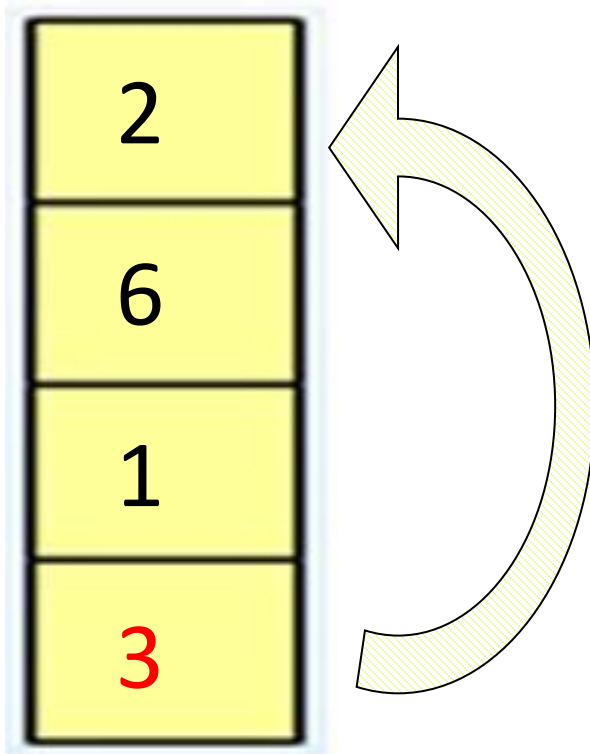
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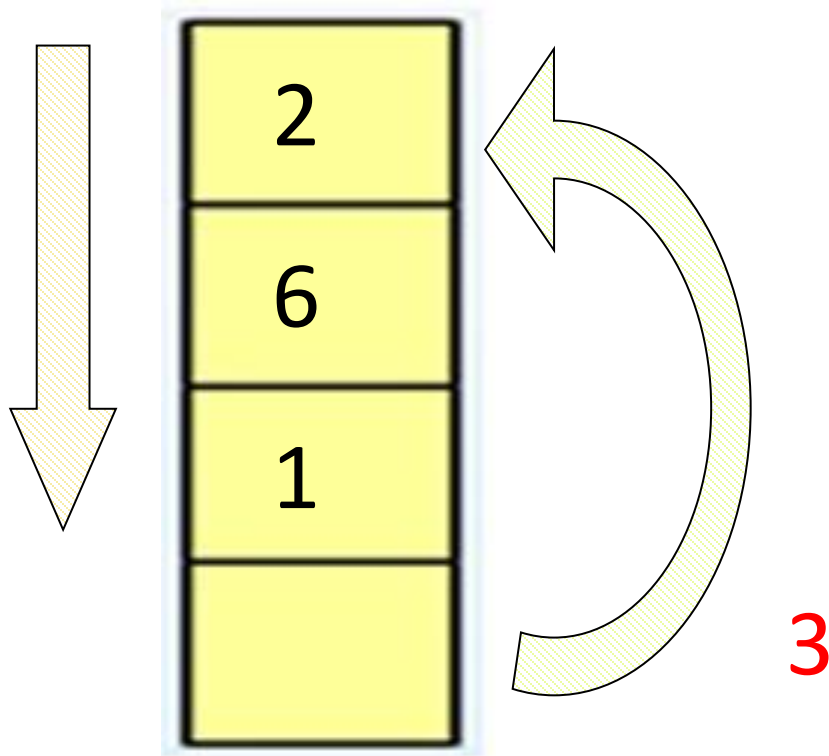
REF string: 1 5 3 1 6 **2** 3



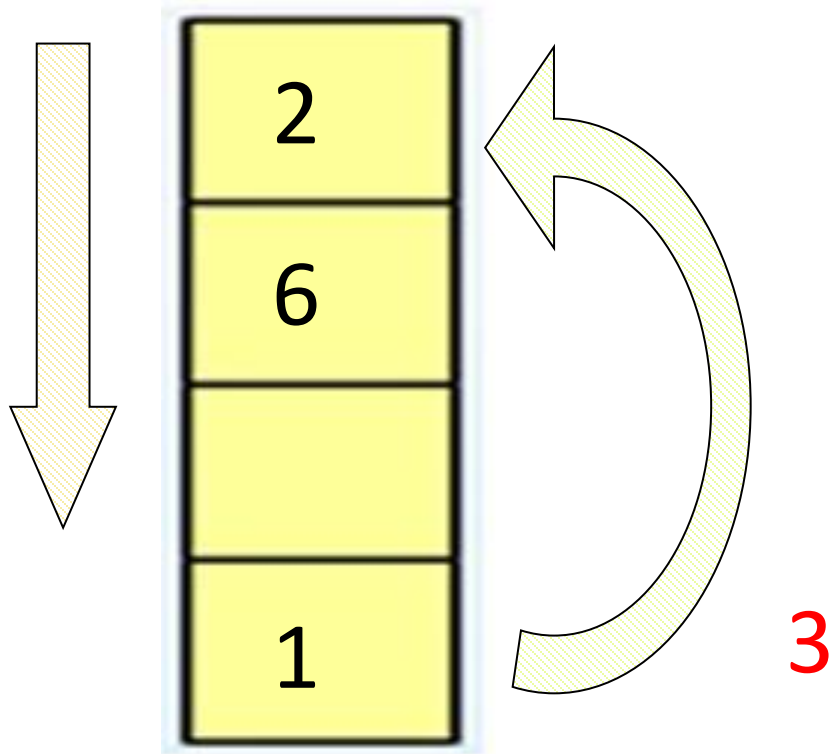
REF string: 1 5 3 1 6 2 **3**



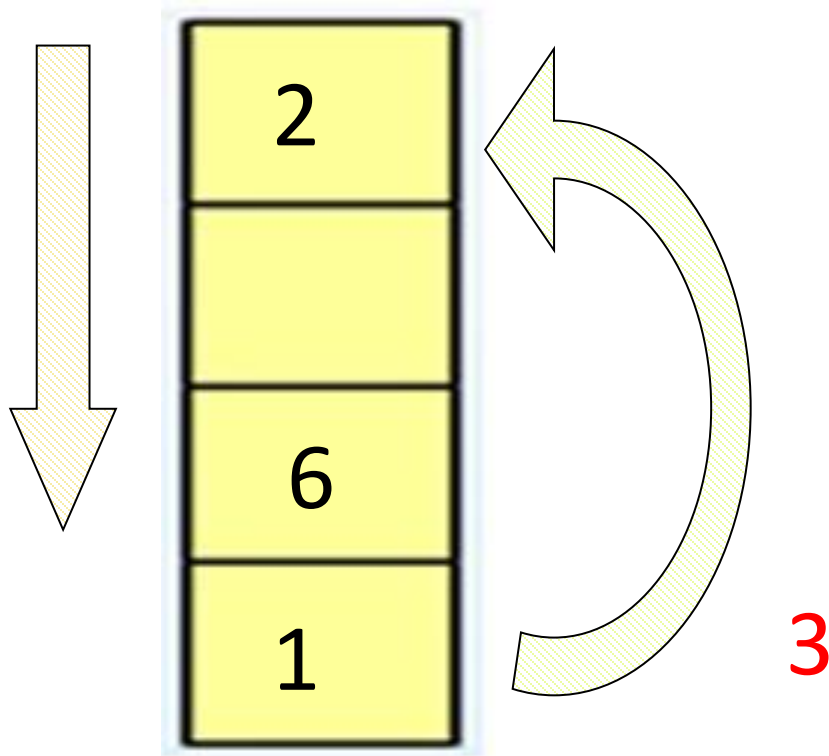
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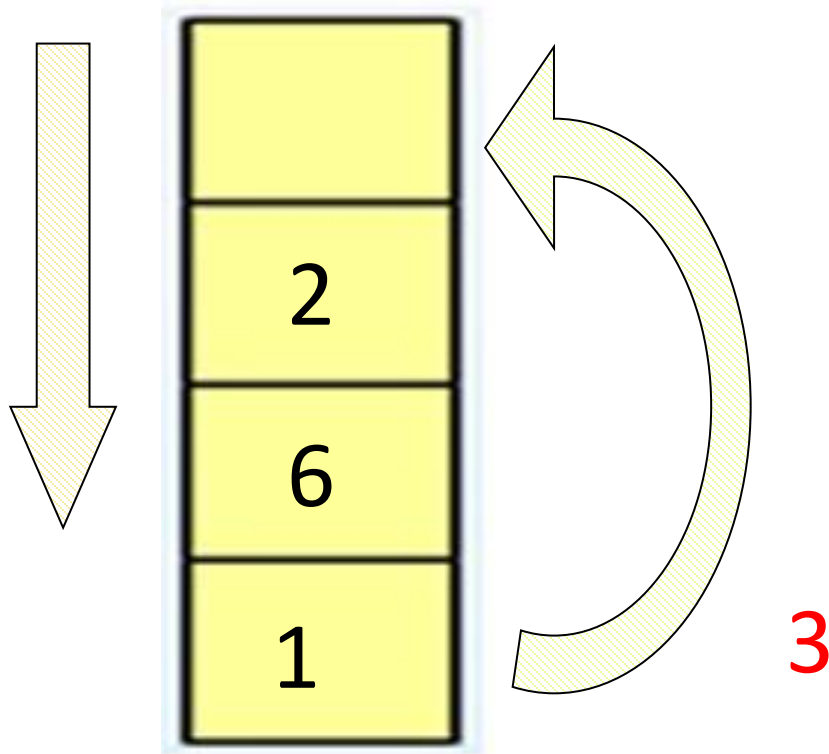
REF string: 1 5 3 1 6 2 **3**



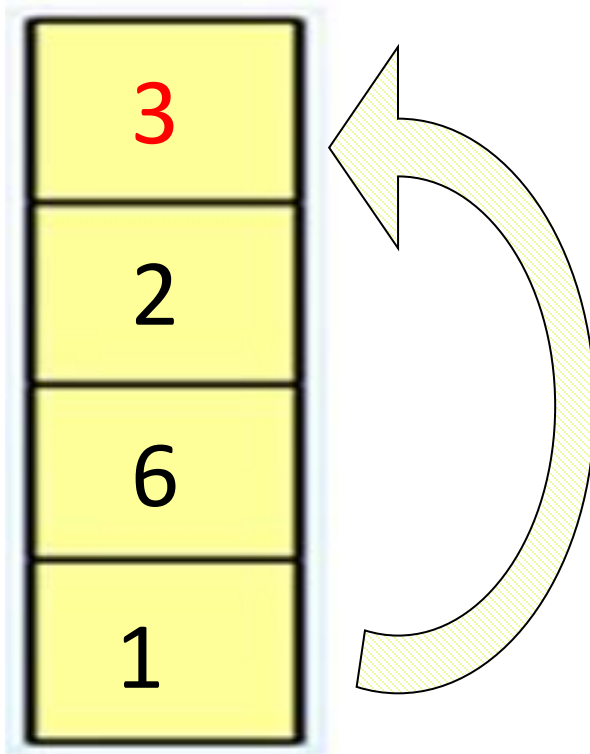
REF string: 1 5 3 1 6 2 **3**



REF string: 1 5 3 1 6 2 **3**



REF string: 1 5 3 1 6 2 **3**





# Cache LRU Stack

- Cache LRU stack – example for **associative cache**
  - When Cache is full, the victim block is the block at the bottom of the Cache LRU stack
  - The victim block is removed from the stack and the newly used one goes on top of the stack. The rest are shifted to down.

Cache LRU Stack

5
1
7
4
3
2
0
6

Address with tag value 18  
is referenced

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	2	*
7	12	*

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Cache LRU Stack

5
1
7
4
3
2
0
6

Address with tag value 18  
is referenced

**Cache miss!**  
**Block 6 is the victim!**

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	2	*
7	12	*

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Cache LRU Stack

6
5
1
7
4
3
2
0

Address with tag value 18  
is referenced

**Cache miss!**  
**Block 6 is the victim!**

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	18	*
7	12	*

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  - When Cache is full, the victim block is the block at the bottom of the Cache LRU stack
  - The victim block is removed from the stack and the newly used one goes on top of the stack. The rest are shifted to down.

Cache LRU Stack

6
5
1
7
4
3
2
0

Address with tag value 7  
is referenced.

**Cache hit!**  
**Block 2's position in LRU**  
**stack is updated.**

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	18	*
7	12	*

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- Cache LRU stack – example for **associative cache**
  - When Cache is full, the victim block is the block at the bottom of the Cache LRU stack
  - The victim block is removed from the stack and the newly used one goes on top of the stack. The rest are shifted to down.

Cache LRU Stack

2
6
5
1
7
4
3
0

Address with tag value 7  
is referenced

**Cache hit!**  
**Block 2's position in LRU**  
**stack is updated.**

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	18	*
7	12	*

# Cache LRU Stack

- Cache LRU stack – example for ***N-way set-associative*** cache
  - When ***a set in Cache is full***, the victim block is the block at the bottom of ***the set's LRU stack***
  - The victim block is removed from the stack and the newly used one goes on top of the stack. The rest are shifted to down.

LRU Stack for set 0

2
0
1
3

LRU Stack for set 1

5
6
7
4

Address with set value 0 and tag value 21 is referenced

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	2	*
7	12	*

# Cache LRU Stack

- Cache LRU stack – example for ***N-way set-associative*** cache
  - When ***a set in Cache is full***, the victim block is the block at the bottom of ***the set's LRU stack***
  - The victim block is removed from the stack and the newly used one goes on top of the stack. The rest are shifted to down.

LRU Stack for set 0

2
0
1
3

LRU Stack for set 1

5
6
7
4

Address with set value 0 and tag value 21 is referenced

**Cache miss!**

**Block 3 in set 0 is the victim!**

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	9	*
4	3	*
5	15	*
6	2	*
7	12	*

# Cache LRU Stack

- Cache LRU stack – example for ***N-way set-associative*** cache
  - When ***a set in Cache is full***, the victim block is the block at the bottom of ***the set's LRU stack***
  - The victim block is removed from the stack and the newly used one goes on top of the stack. The rest are shifted to down.

LRU Stack for set 0

3
2
0
1

LRU Stack for set 1

5
6
7
4

Address with set value 0 and tag value 21 is referenced

**Cache miss!**

**Block 3 in set 0 is the victim!**

Cache

Block ID	Tag Value	Data
0	10	*
1	0	*
2	7	*
3	21	*
4	3	*
5	15	*
6	2	*
7	12	*