HW1 Collaborative: Propositional Logic

CS40 Fall'21

Due: Thursday, Oct 7, 2021 at 10:00PM on Gradescope

In this assignment,

You will practice reading and applying definitions to get comfortable working with mathematical language and propositional logic

For all Collaborative HW assignments:

Collaborative homeworks may be done individually or in groups of up to 4 students. You may switch HW partners for different HW assignments. Please ensure your name(s) and PID(s) are clearly visible on the first page of your homework submission.

All submitted homework for this class must be typed. Diagrams may be hand-drawn and scanned and included in the typed document. You can use a word processing editor if you like (Microsoft Word, Open Office, Notepad, Vim, Google Docs, etc.) but you might find it useful to take this opportunity to learn LaTeX. LaTeX is a markup language used widely in computer science and mathematics. The homework assignments are typed using LaTeX and you can use the source files as templates for typesetting your solutions[1] .

Integrity reminders

- Problems should be solved together, not divided up between the partners. The homework is designed to give you practice with the main concepts and techniques of the course, while getting to know and learn from your classmates.

- You may not collaborate on homework with anyone other than your group members. You may ask questions about the homework in office hours (of the instructor, TAs, and/or tutors) and on Piazza. You *cannot* use any online resources about the course content other than the text book and class material from this quarter – this is primarily to ensure that we all use consistent notation and definitions we will use this quarter.

- Do not share written solutions or partial solutions for homework with other students in the class who are not in your group. Doing so would dilute their learning experience and detract from their success in the class.

You will submit this assignment via Gradescope (https://www.gradescope.com) in the assignment called "HW1-Collaborative".

---

[1]To use this template, you will need to copy both the source file (extension `.tex`) you'll be editing and the file containing all the "shortcut" commands we've defined for this class)

Assigned Questions

1. Determine whether each of the following sentences is a proposition. If the sentence is a proposition, then write its negation.

   (a) Have a nice day.

   (b) The soup is cold.

2. Express each English statement using the logical operations $\vee$, $\wedge$, $\neg$ and the propositional variables t, n, and m defined below. The use of the word "or" means inclusive or.

   - t: The patient took the medication.
   - n: The patient had nausea.
   - m: The patient had migraines.

   (a) The patient had nausea and migraines

   (b) The patient took the medication, but still had migraines.

   (c) Despite the fact that the patient took the medication, the patient had nausea.

   (d) There is no way that the patient took the medication.

3. In this question practice expressing a set of conditions using logical operations.

   Consider the following pieces of identification a person might have in order to apply for a credit card:

   - b: Applicant presents a birth certificate.
   - d: Applicant presents a driver's license.
   - m: Applicant presents a marriage license.

   Write a logical expression for the requirements under the following conditions:[2]

   (a) The applicant must present either a birth certificate, a driver's license, or a marriage license.

   (b) The applicant must present at least two of the following forms of identification: birth certificate, driver's license, marriage license.

   (c) Applicant must present either a birth certificate or both a driver's license and a marriage license

4. Practice finding the truth values for conditional statements in English. Which of the following conditional statements are true and why?

   (a) If February has 30 days, then 7 is an odd number.

   (b) If January has 31 days, then 7 is an even number.

---

[2]Inclusive or is assumed unless explicitly stated otherwise.

5. Give an English sentence in the form "If...then...." that is equivalent to each sentence.

   (a) Maintaining a B average is sufficient for Joe to be eligible for the honors program.

   (b) Maintaining a B average is necessary for Joe to be eligible for the honors program.

   (c) Rajiv can go on the roller coaster only if he is at least four feet tall.

   (d) Rajiv can go on the roller coaster if he is at least four feet tall.

6. Show using truth tables or laws of propositional logic whether each logical expression is a tautology, contradiction or neither. Note: When writing the truth table follow the row sequence used in lecture and the book (i.e. TT, TF, FT, FF)

   (a) $(p \vee q) \vee (q \rightarrow p)$

   (b) $(p \rightarrow q) \leftrightarrow (p \wedge \neg q)$

7. There are three kinds of people on an island: knights who always tell the truth, knaves who always lie, and spies who can either lie or tell the truth. You encounter three people, A, B, and C. You know one of these people is a knight, one is a knave, and one is a spy. Each of the three people knows the type of person each of other two is. A says "C is the knave," B says "A is the knight," and C says "I am the spy.". If possible, determine whether there is a unique solution and determine who the knave, knight, and spy are. When there is no unique solution, list all possible solutions or state that there are no solutions.

8. Use the Disjunctive Normal form to construct a proposition Q whose truth table is as below:

p	q	r	Q
T	T	T	T
T	T	F	F
T	F	T	F
T	F	F	T
F	T	T	T
F	T	F	F
F	F	T	T
F	F	F	F

Attributions