

# Homework 28

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## 51

Let  $f$  be the function passed as input to Simon's algorithm. When Simon's algorithm returns  $a = 0$  it is claiming that the function from  $\{0, 1\}^n \rightarrow \{0, 1\}^n$  is a permutation. During the measurement of the first  $n$  bits in Simon's algorithm, you get a uniformly distributed  $y$  at random such that  $y * a = 0$ . Since  $a = 0$  in this case, you get a uniformly distributed measurement of  $y$ . If  $f$  is a permutation, then there is a uniform distribution that  $y$  in the range of  $f$  is chosen from input  $x$ , so Simon's algorithm correctly handles the case where  $a = 0$ .

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**a**

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

**b**

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

**c**

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

**d**

$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} a + b + c + d \\ a - b + c - d \\ a + b - c - d \\ a - b - c + d \end{bmatrix}$$

**e**

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \sqrt{a^2 + b^2} \\ \sqrt{c^2 + d^2} \end{bmatrix} = \begin{bmatrix} \sqrt{a^2 + b^2} + \sqrt{c^2 + d^2} \\ \sqrt{a^2 + b^2} - \sqrt{c^2 + d^2} \end{bmatrix}$$

**f**

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \sqrt{a^2 + b^2} \\ \sqrt{c^2 + d^2} \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \sqrt{a^2 + c^2} \\ \sqrt{b^2 + d^2} \end{bmatrix} = \begin{bmatrix} \sqrt{a^2 + b^2} + \sqrt{c^2 + d^2} \\ \sqrt{a^2 + b^2} - \sqrt{c^2 + d^2} \end{bmatrix} \begin{bmatrix} \sqrt{a^2 + c^2} + \sqrt{b^2 + d^2} \\ \sqrt{a^2 + c^2} - \sqrt{b^2 + d^2} \end{bmatrix} =$$