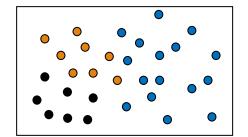


Clustering Tendency: Whether the Data Contains Inherent Grouping Structure

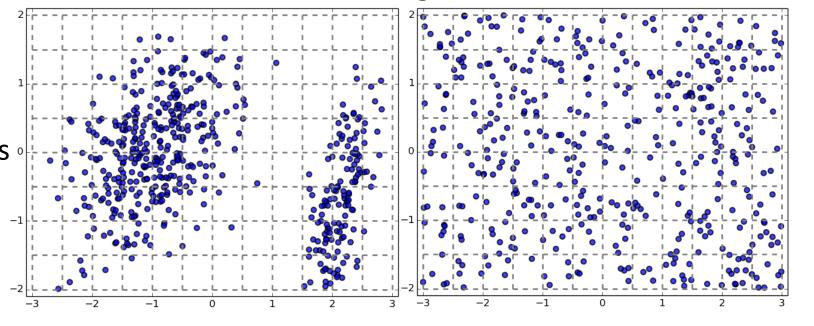
- Assessing the suitability of clustering
 - ☐ (i.e., whether the data has any inherent grouping structure)
- Determining clustering tendency or clusterability



- □ A hard task because there are so many different definitions of clusters
 - □ E.g., partitioning, hierarchical, density-based, graph-based, etc.
- Even fixing cluster type, still hard to define an appropriate null model for a data set
- □ Still, there are some **clusterability assessment methods**, such as
 - Spatial histogram: Contrast the histogram of the data with that generated from random samples
 To be covered here
 - Distance distribution: Compare the pairwise point distance from the data with those from the randomly generated samples
 - Hopkins Statistic: A sparse sampling test for spatial randomness

Testing Clustering Tendency: A Spatial Histogram Approach

- □ **Spatial Histogram Approach:** Contrast the *d*-dimensional histogram of the input dataset *D* with the histogram generated from random samples
 - □ Dataset D is clusterable if the distributions of two histograms are rather different
- Method outline
 - Divide each dimension into equi-width bins, count how many points lie in each cells, and obtain the empirical joint probability mass function (EPMF)



- Do the same for the randomly sampled data
- □ Compute how much they differ using the Kullback-Leibler (KL) divergence value

Recommended Readings

- M. J. Zaki and W. Meira, Jr. Data Mining and Analysis: Fundamental Concepts and Algorithms. Cambridge University Press, 2014
- L. Hubert and P. Arabie. Comparing Partitions. *Journal of Classification*, 2:193–218, 1985
- □ A. K. Jain and R. C. Dubes. Algorithms for Clustering Data. Printice Hall, 1988
- M. Halkidi, Y. Batistakis, and M. Vazirgiannis. On Clustering Validation Techniques. Journal of Intelligent Info. Systems, 17(2-3):107–145, 2001
- □ J. Han, M. Kamber, and J. Pei. Data Mining: Concepts and Techniques. Morgan Kaufmann, 3rd ed., 2011
- □ H. Xiong and Z. Li. Clustering Validation Measures. in (Chapter 23) C. Aggarwal and C. K. Reddy (eds.), Data Clustering: Algorithms and Applications. CRC Press, 2014