

Define problem $U_{xx} + f = 0$
 $U(0) = g = 1$
 $-U_x(1) = h = 0$

↓
Set up the mesh
polynomial degree pp ;

$$N_{el} = pp+1, \quad N_{el}, \quad N_{np} = N_{el} \times pp + 1$$

$$N_{eq} = N_{np} - 1$$

$$hh = \frac{1}{N_{np}-1} \quad \text{space between 2 nodes}$$

$$x \text{ coordinate} = 0 : hh : 1$$

↓
Create IEN array

for $ee = 1 : N_{el}$ element

for $aa = 1 : N_{en}$ element node

$$\text{IEN}(ee, aa) = \underbrace{(ee-1) \times pp + aa}_{ac}$$

| | | | | |
|----|---|---|---|-----|
| ee | 1 | 2 | 3 | ... |
| | 2 | 3 | 4 | ... |
| | 3 | 4 | 5 | ... |
| | , | | | |

↓
Set up 1D array

ID = 1 : Nnp ID(end) = 0

1 2 3 4 ... 0

↓
Set up quadrature rule

Gauss function N=10
get ξ and weights

↓
Create K and F

K = spalloc (Neq, Neq, (2*p+1)*Nel)
sparse matrix

F = zeros(Neq, 1)

↓
Assembly of K and F

ee = 1 : Nel each element

Kele : Nen x Nen element matrix

fele : Nen x 1

Xele : Xcoor x (IEN(ee, :))

determine x_1 , $\frac{dx}{d\xi}$, $\frac{d^3}{dx^3}$, fele - Kele

for qua = 1 : int

for aa = 1 : Nen

$$X_L = X_L + X_{ele}(aa) \times \text{polyshape}(\text{pp}, aa, x_{ipw})$$

:

↓

Assembly of k_{ele} to K, f_{ele} to F

for aa = 1 : Nen

$$P = ID(IEN(ee, aa))$$

If P > 0

$$F(P) = F(P) + f_{ele}(aa)$$

for bb = 1 : Nen

$$Q = ID(IEN(ee, bb))$$

If Q > 0

$$K(P, Q) = K(P, Q) + k_{ele}(aa, bb)$$

else

$$\underline{F(P) = F(P) - k_{ele}(aa, bb)}$$

$$\downarrow B.C - k_{ele}(aa, bb) = h$$

$$F(ID(IEN(1, 1))) = F(ID(IEN(1, 1))) + h$$

$$d_{\text{temp}} = K \setminus F \quad \text{solve } d$$

↓

$$d_{\text{disp}} = [d_{\text{temp}}; g]$$

↓

post - proceeding

show u^h and u by sample points