Statistical Inference - course project

10/25/2014

The exponential distribution can be simulated in R with rexp(n, lambda) where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also also 1/lambda.

1. Show where the distribution is centered at and compare it to the theoretical center of the distribution.

When we calculate sample and theorithical mean, we see that both lie close together.

```
mean(averages)

## [1] 4.99

1/lambda

## [1] 5
```

2. Show how variable it is and compare it to the theoretical variance of the distribution.

From the CLT we know that X^{α} approximately follows $N(mu, sigma^{\alpha}/2n)$. We know sigma to be 1/lambda. As such it follows that the theoretical standard deviation is:

```
(1/lambda)/sqrt(40) # Theoretical standard deviation

## [1] 0.7906

sd(averages) # actual standard deviation

## [1] 0.7817

# And the variances
((1/lambda)/sqrt(40))^2

## [1] 0.625
```

```
sd(averages)^2
```

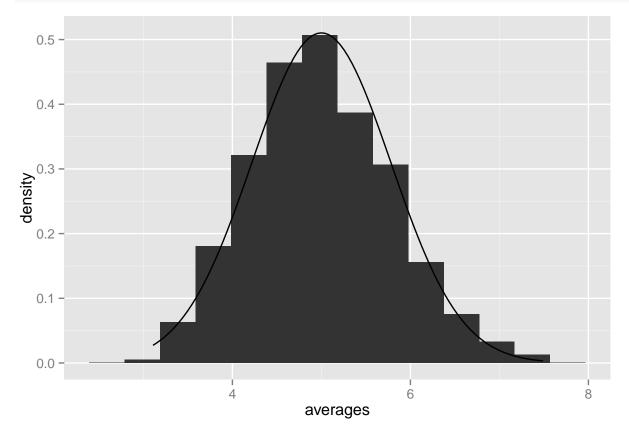
[1] 0.6111

3. Show that the distribution is approximately normal.

To do so, we plot an histogram of the sampled means and overlay the normal distribution with mean 5 and standard deviation 0.7817 on top of it. We see that the normal distribution indeed closely matches the barplot of the means.

```
library(ggplot2)
# Sturges' formula
k <- ceiling(log2(length(simulations)) + 1)
bw <- (range(averages)[2] - range(averages)[1]) / k
averages.sd <- sd(averages)

p <- ggplot(data.frame(averages), aes(x=averages))
p <- p + geom_histogram(aes(y=..density..), binwidth=bw)
p <- p + stat_function(fun = dnorm, args=list(mean=5, sd=averages.sd))
p</pre>
```



4. Evaluate the coverage.

Evaluate the coverage of the confidence interval for 1/lambda:

$$\bar{X} \pm 1.96 \frac{S}{\sqrt{n}}$$

mean(averages) + c(-1,1) * 1.96 * sd(averages) / sqrt(length(averages))

[1] 4.942 5.038