

# Package ‘dils’

July 19, 2013

**Type** Package

**Title** Data-Informed Link Strength. Combine multiple-relationship networks into a single weighted network.

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**Depends** R (>= 2.15.0), igraph

**Suggests** testthat

**Description** Combine multiple-relationship networks into a single weighted network. The approach is similar to factor analysis in that contribution from each constituent network varies so as to maximize the information gleaned from the multimetwork. This implementation uses Principal Component Analysis calculated using ‘prcomp’ with bootstrap subsampling.

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**Collate**

‘GetSampleFromDataFrame.R’ ‘RelationStrengthSimilarity.R’ ‘ScalablePCA.R’ ‘GetSampleFromFile.R’ ‘GetSampleFromIgraph.R’

## R topics documented:

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dils-package	<i>Data-Informed Link Strength. Combine multiple-relationship networks into a single weighted network.</i>
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## Description

Combine multiple-relationship networks into a single weighted network. The approach is similar to factor analysis in the that contribution from each constituent network varies so as to maximize the information gleaned from the multimetwork. This implementation uses Principal Component Analysis calculated using 'prcomp' with bootstrap subsampling.

## Details

Package: dils  
 Type: Package  
 Version: 0.5  
 Date: 2013-07-17  
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Start with a table (data.frame, tab-delimited file, database) where each row/record represents a link between two nodes (a dyad) in a directed or undirected network and each column represents a different relationship between the two nodes, ie. each column is a network. DILS combines these columns/networks into a single network that is a weighted sum of the constituent networks. The resulting DILS network uses information from all of the constituent networks and contains more information than any of the constituent networks. The output is a data.frame of DILS scores for each dyad, therefore is a single network ready for analysis using **igraph** or other social network analysis (SNA) tools.

Workflow synthesizing networks might typically look like this:

1. Start with several networks in igraph, adjacency list, or edgelist form.
2. Is necessary, use [EdgelistFromIgraph](#) or [EdgelistFromAdjacency](#) to convert igraph and adjacency list networks to edgelist form.
3. Use [MergeEdgelists](#) to combine the individual network datasets into a single dataset.
4. Use [GenerateDilsNetwork](#) to synthesize the networks in the merged data set into a single weighted network.
5. Use [IgraphFromEdgelist](#) or [AdjacencyFromEdgelist](#) to convert the edgelist output to the desired output.
6. Use [MeasureNetworkInformation](#) on input networks and DILS network to see if/how much

Workflow for imputing edges for a binary network might typically look like this:

1. Start with a binary network as an adjacency matrix (for an igraph use `get.adjacency`).
2. Use [RelationStrengthSimilarity](#) to Calculate RSS scores for each dyad.

3. Use `RssSuggestedNetwork` on the original network and the `RelationStrengthSimilarity` output to get a new suggested network with more edges.

### Author(s)

Stephen R. Haptonstahl <srh@haptonstahl.org>

### References

"Discovering Missing Links in Networks Using Similarity Measures", Hung-Hsuan Chen, Liang Gou, Xiaolong (Luke) Zhang, C. Lee Giles. 2012.

---

AdjacencyFromEdgelist *Convert an edgelist to an adjacency matrix*

---

### Description

Given the adjacency matrix for a network return a data.frame listing all possible edges and the weights for each edge.

### Usage

```
AdjacencyFromEdgelist(elist)
```

### Arguments

`elist` data.frame, see 'Details' for formatting assumptions.

### Details

This assumes that `elist` is a data.frame with three columns. Each row is an edge in the network. The first column lists the node the edge is coming from, the second column lists the node the edge is going to, and the third column lists the weight of the edge.

### Value

list, containing an adjacency matrix and a vector of node ids identifying the rows and columns

`adjacency` The adjacency matrix for the network. The row indicates the node the edge is coming 'from', the column indicates the node the edge is going 'to'.

`nodelist` The ids of the nodes in the same order as the the rows and columns of the adjacency matrix.

### Author(s)

Stephen R. Haptonstahl <srh@haptonstahl.org>

### References

<https://github.com/shaptonstahl/>

### See Also

[EdgelistFill](#)

**Examples**

```
edgelist <- cbind(expand.grid(letters[1:2], letters[1:2]), runif(4))
AdjacencyFromEdgelist(edgelist)
```

---

EdgelistFill

*Ensure an edgelist has all dyads and a column of weights.*


---

**Description**

Given a matrix or data.frame edgelist, fill in all possible edges not already listed with a weight of 0 or the value of fillBlanksWith.

**Usage**

```
EdgelistFill(elist, fillBlanksWith = 0, nodelist)
```

**Arguments**

elist                    data.frame or matrix, see 'Details' for formatting assumptions.  
fillBlanksWith        numeric, default weight for edges not already listed in elist.  
nodelist                character, optional list of node names.

**Details**

The elist can be either a data.frame or a matrix with either 2 or 3 columns. Each row is an edge. The first column lists the node the edge is 'from' and the second column lists the node the edge is 'to'. If there is a third column, it lists the weight of the edge.

**Value**

data.frame, full list of all possible edges with weights for each in third column.

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<https://github.com/shaptonstahl/>

**Examples**

```
g <- erdos.renyi.game(10, 2/10)
EdgelistFill(get.edgelist(g))
EdgelistFill(get.edgelist(g), nodelist=1:10)

E(g)$weight <- runif(ecount(g))
el <- cbind(get.edgelist(g), E(g)$weight)
EdgelistFill(el)
EdgelistFill(el, nodelist=1:10)
```

---

EdgelistFromAdjacency *Convert an adjacency matrix to filled edgelist.*

---

### Description

Given the adjacency matrix for a network return a data.frame listing all possible edges and the weights for each edge.

### Usage

```
EdgelistFromAdjacency(A,  
  nodelist = paste("node", 1:nrow(A), sep = ""))
```

### Arguments

A	matrix, see 'Details' for formatting assumptions.
nodelist	character, optional list of node names.

### Details

This assumes that the row of the adjacency matrix indicates the node the edge is coming 'from', the column represent the node the edge is going 'to', and the value in the adjacency matrix is the weight given to the edge.

### Value

data.frame, full list of all possible edges with weights for each in third column.

### Author(s)

Stephen R. Haptonstahl <srh@haptonstahl.org>

### References

<https://github.com/shaptonstahl/>

### See Also

[EdgelistFromIgraph](#)

### Examples

```
n <- 10  
A <- matrix(rnorm(n*n), nrow=n)  
A  
EdgelistFromAdjacency(A)  
  
n <- 100  
A <- matrix(rnorm(n*n), nrow=n)  
A  
EdgelistFromAdjacency(A)  
  
n <- 500
```

```
A <- matrix(rnorm(n*n), nrow=n)
A
## Not run: EdgelistFromAdjacency(A)
```

---

EdgelistFromIgraph	<i>Convert an igraph to filled edgelist</i>
--------------------	---

---

## Description

Given an igraph object for a network return a data.frame listing all possible edges and the weights for each edge.

## Usage

```
EdgelistFromIgraph(g, useWeight = FALSE)
```

## Arguments

g	igraph, from <a href="#">igraph</a> package.
useWeight	logical, Should E(g)\$weight be used as the weights for the edges?

## Details

This function is preferred to the igraph function `get.edgelist` because `get.edgelist` only returns rows for edges that have non-zero weight and does not return weights, if present.

## Value

data.frame, full list of all possible edges with weights for each in third column.

## Author(s)

Stephen R. Haptonstahl <[srh@haptonstahl.org](mailto:srh@haptonstahl.org)>

## References

<https://github.com/shaptonstahl/>

## See Also

[EdgelistFromAdjacency](#)

## Examples

```
g <- erdos.renyi.game(10, 2/10)
EdgelistFromIgraph(g)

V(g)$name <- letters[1:vcount(g)]
EdgelistFromIgraph(g)

E(g)$weight <- runif(ecount(g))
EdgelistFromIgraph(g, useWeight=TRUE)
```

---

GenerateDilsNetwork     *Combine multiple networks into a single weighted network.*

---

## Description

Use ScalablePCA to recover optimal weights for each network, then calculate the weighted average across networks for each edge.

## Usage

```
GenerateDilsNetwork(x, subsample = 10000,
  n.subsamples = 1000, ignore.cols, use.cols,
  progress.bar = FALSE)
```

## Arguments

x	data.frame, data over which to run PCA
subsample	numeric or logical, If an integer, size of each subsample. If FALSE, runs PCA on entire data set.
n.subsamples	numeric, number of subsamples.
ignore.cols	numeric, indices of columns not to include
use.cols	numeric, indices of columns to use
progress.bar	logical, if TRUE then progress in running subsamples will be shown.

## Value

list	
dils	vector, named vector of component weights for first dimension of principal component analysis (see example)
coefficients	named vector, weights that generate dils by taking dot-product with network data.
weights	named vector, raw.weights scaled by standard deviations of network edges, then scaled to sum to 1.

## Author(s)

Stephen R. Haptonstahl <srh@haptonstahl.org>

## References

<https://github.com/shaptonstahl/>

## See Also

[prcomp](#)

## Examples

```
data(iris)                    # provides example data
GenerateDilsNetwork(iris, subsample=10, use.cols=1:4)
GenerateDilsNetwork(iris, subsample=10, ignore.cols=5)
```

---

`GetSampleFromDataFrame`*Randomly select rows from a data.frame.*

---

**Description**

Randomly select n rows from data.frame x.

**Usage**

```
GetSampleFromDataFrame(n, x)
```

**Arguments**

n	numeric, size of sample.
x	data.frame, data whose rows will be sampled.

**Value**

data.frame, size n random subset of the rows of x

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<https://github.com/shaptonstahl/>

**See Also**

[ScalablePCA](#), [GetSampleFromFile](#), [GetSampleFromFile](#)

**Examples**

```
data(iris) # provides example data
x <- dils::GetSampleFromDataFrame(10, iris)
```

---

`GetSampleFromDb`*Sample from the rows of a (possibly large) database table (NOT IMPLEMENTED)*

---

**Description**

Access a database table directly. Return a data.frame whose rows are the sample.

**Usage**

```
GetSampleFromDb(n, db)
```



**Arguments**

n                      numeric, size of sample to be taken.  
 db                     connection, connection to the database table containing the data.

**Value**

data.frame, size n random subset of the rows of filename

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<https://github.com/shaptonstahl/>

**See Also**

[ScalablePCA](#), [GetSampleFromDataFrame](#), [GetSampleFromFile](#)

**Examples**

```
## Not run: x <- dils:::GetSampleFromDb(10, my.db)
```

---

GetSampleFromFile	<i>Sample from the rows of a (possibly large) text file (NOT IMPLEMENTED)</i>
-------------------	---

---

**Description**

Read a large text file in batches, keeping the rows to be included in the sample. Return a data.frame whose rows are the sample.

**Usage**

```
GetSampleFromFile(n, out.of, filename)
```

**Arguments**

n                      numeric, size of sample to be taken.  
 out.of                numeric, number of rows in the data set not including the header.  
 filename             character, name of the file containing the data. This must be a tab-delimited file with a header row formatted per the default options for [read.delim](#).

**Value**

data.frame, size n random subset of the rows of filename

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<https://github.com/shaptonstahl/>

**See Also**

[ScalablePCA](#), [GetSampleFromDataFrame](#), [GetSampleFromDb](#)

**Examples**

```
## Not run: x <- dils::GetSampleFromFile(10, 150, "folder/containing/data.txt")
```

---

IgraphFromEdgelist	<i>Convert an edgelist to an igraph</i>
--------------------	---

---

**Description**

Given the adjacency matrix for a network return a data.frame listing all possible edges and the weights for each edge.

**Usage**

```
IgraphFromEdgelist(elist, directed = TRUE)
```

**Arguments**

elist	data.frame, see 'Details' for formatting assumptions.
directed	logical, If TRUE, the returned igraph is directed.

**Details**

This assumes that elist is a data.frame with three columns. Each row is an edge in the network. The first column lists the node the edge is coming from, the second column lists the node the edge is going to, and the third column lists the weight of the edge.

**Value**

igraph, If the edgelist third column has values other than 0, 1 then the weights are stored in E(returned graph)\$weight.

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<https://github.com/shaptonstahl/>

**See Also**

[EdgelistFill](#)

**Examples**

```
edgelist <- cbind(expand.grid(letters[1:2], letters[1:2]), runif(4))
g <- IgraphFromEdgelist(edgelist)
get.edgelist(g)
E(g)$weight
plot(g, edge.width=5*E(g)$weight, edge.curved=TRUE)
```

---

MeasureNetworkInformation

*Measure informativeness of a network of a particular network measure.*

---

**Description**

Given an igraph network, repeatedly perturb the graph and take some measure of the network to see how much the measure varies.

**Usage**

```
MeasureNetworkInformation(g, FUN = betweenness,
  remove.share = 0.2, sample.size = 100,
  progress.bar = FALSE)
```

**Arguments**

<code>g</code>	igraph, graph to measure
<code>FUN</code>	function, a function that takes an igraph and returns a value for each node in the network.
<code>remove.share</code>	numeric, fraction of the edges that are removed randomly when perturbing the network.
<code>sample.size</code>	numeric, number of perturbed graphs to generate
<code>progress.bar</code>	logical, if TRUE then a progress bar is shown.

**Details**

Here information is measured as  $1 / \text{mean across and perturbed graphs nodes of the relative error of a network node measure}$ .

Specifically, FUN is applied to the graph `g` to generate reference values. Some `sample.size` copies of the igraph are generated. For each, `round(remove.share * n.edges)` randomly selected edges are dropped to generate a perturbed graph. For each perturbed graph FUN is applied, generating a value for each node in the network. For each node the relative error

$$\left| \frac{\text{measureofperturbedg} - \text{measureofg}}{\text{measureofg}} \right|$$

The mean of these across nodes and perturbed graphs is calculated, generating a mean relative error for the network. This value is reciprocated to get a measure of precision.

This measure appears to be very sensitive to the choice of FUN.

**Value**

numeric, mean precision of the measure FUN across the network

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<https://github.com/shaptonstahl/>

**Examples**

```
g.rand <- random.graph.game(100, 5/100)
m.rand <- MeasureNetworkInformation(g.rand)
m.rand

pf <- matrix( c(.8, .2, .3, .7), nr=2)
g.pref <- preference.game(100, 2, pref.matrix=pf)
m.pref <- MeasureNetworkInformation(g.pref)
m.pref

m.pref / m.rand # Relative informativeness of this preference graph
                # to this random graph with respect to betweenness
## Not run: p.values <- 1:50
mnis <- sapply(p.values, function(p)
  MeasureNetworkInformation(random.graph.game(100, p/100)))
plot(p.values/100, mnis,
     type="l",
     main="Network Information of random graphs",
     xlab="probability of link formation",
     ylab="information")
mtext("with respect to betweenness measure", line=0.5)
## End(Not run)
```

---

MergeEdgelists

---

Combine edgelists into a single data.frame

---

**Description**

Given two or more edgelists, create a single edgelist with multiple columns, two for the from and to nodes and one for the weights from each constituent network.

**Usage**

```
MergeEdgelists(...)
```

**Arguments**

... data.frames, edgelists to be merged.

**Value**

data.frame, single multinetwork edgelist

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

**References**

<http://www.haptonstahl.org/R>

**See Also**

[EdgelistFill](#)

**Examples**

```
edgelist1 <- data.frame(expand.grid(letters[1:2], letters[1:2]),
                        uniform=runif(4))
edgelist2 <- data.frame(v1=c("a", "a"), v2=c("a", "b"), manual=c(.3, .5))
MergeEdgelist1(edgelist1, edgelist2)
```

---

RelationStrengthSimilarity

*Calculate the RSS from one node to another.*

---

**Description**

For a single pair of nodes, implement the RSS algorithm of Chen et al. (2012).

**Usage**

```
RelationStrengthSimilarity(xadj, v1, v2, radius)
```

**Arguments**

xadj	numeric matrix, then description of arg1.
v1	numeric Object type, then description of arg2.
v2	numeric Object type, then description of arg2.
radius	numeric, length of longest path examined from v1 to v2.

**Details**

If v1 and v2 are specified, this returns the RSS from v1 to v2. If not, it calculates the RSS scores for all dyads in the network.

**Value**

numeric, Relation Strength Similarity score(s).

**Author(s)**

Stephen R. Haptonstahl <srh@haptonstahl.org>

## References

"Discovering Missing Links in Networks Using Similarity Measures", Hung-Hsuan Chen, Liang Gou, Xiaolong (Luke) Zhang, C. Lee Giles. 2012.

<https://github.com/shaptonstahl/>

## See Also

[ScalablePCA](#)

## Examples

```
M <- as.matrix(get.adjacency(graph.atlas(128)))
M
RelationStrengthSimilarity(xadj=M, v1=5, v2=6, radius=1)
RelationStrengthSimilarity(xadj=M, v1=5, v2=6, radius=2)
RelationStrengthSimilarity(xadj=M, v1=5, v2=6, radius=3)
RelationStrengthSimilarity(xadj=M, v1=5, v2=6, radius=4)
RelationStrengthSimilarity(xadj=M, radius=2)
## Not run: RelationStrengthSimilarity(xadj=M, radius=3)
```

---

RssCell

*Calculate the RSS from one node to another.*

---

## Description

This is a helper function for RelationStrengthSimilarity that returns the RSS for a single directed dyad.

## Usage

```
RssCell(xadj, v1, v2, radius)
```

## Arguments

xadj	numeric matrix, adjacency matrix where the [i,j] entry gives the strength of the link from node i to node j.
v1	numeric, index of the 'from' node.
v2	numeric, index of the 'to' node.
radius	numeric, length of longest path examined from v1 to v2.

## Details

This is an internal function. There are no guardians and it assumes that the adjacency matrix xadj has had zeros entered on the diagonal and then each row divided by the row mean.

## Value

numeric, the Relation Strength Similarity score from v1 to v2.

## Author(s)

Stephen R. Haptonstahl <srh@haptonstahl.org>

## References

"Discovering Missing Links in Networks Using Similarity Measures", Hung-Hsuan Chen, Liang Gou, Xiaolong (Luke) Zhang, C. Lee Giles. 2012.

<https://github.com/shaptonstahl/>

## See Also

[RelationStrengthSimilarity](#)

## Examples

```
M <- as.matrix(get.adjacency(graph.atlas(128)))
M
M <- sweep(M, 1, rowMeans(M), "/")
M
dils:::RssCell(xadj=M, v1=5, v2=6, radius=1)
dils:::RssCell(xadj=M, v1=5, v2=6, radius=2)
dils:::RssCell(xadj=M, v1=5, v2=6, radius=3)
dils:::RssCell(xadj=M, v1=5, v2=6, radius=4)
```

---

RssThisRadius

---

*Calculate part of the RSS from one node to another.*


---

## Description

This is a helper function for `RelationStrengthSimilarity` that returns the component of RSS contributed by paths of one particular length `r`.

## Usage

```
RssThisRadius(x, v1, v2, r, prepped = FALSE)
```

## Arguments

<code>x</code>	numeric matrix, adjacency matrix where the <code>[i,j]</code> entry gives the strength of the link from node <code>i</code> to node <code>j</code> .
<code>v1</code>	numeric, index of the 'from' node.
<code>v2</code>	numeric, index of the 'to' node.
<code>r</code>	numeric, length of paths examined from <code>v1</code> to <code>v2</code> .
<code>prepped</code>	logical, whether or not the adjacency matrix <code>x</code> has had zeros entered on the diagonal and each row divided by the row sum.

## Value

numeric, the part of the Relation Strength Similarity score from `v1` to `v2` contributed by paths of length `r`.

## Author(s)

Stephen R. Haptonstahl <[srh@haptonstahl.org](mailto:srh@haptonstahl.org)>

## References

"Discovering Missing Links in Networks Using Similarity Measures", Hung-Hsuan Chen, Liang Gou, Xiaolong (Luke) Zhang, C. Lee Giles. 2012.

<https://github.com/shaptonstahl/>

## See Also

[RelationStrengthSimilarity](#)

## Examples

```
M <- as.matrix(get.adjacency(graph.atlas(128)))
M
dils:::RssThisRadius(x=M, v1=5, v2=6, r=1)
dils:::RssThisRadius(x=M, v1=5, v2=6, r=2)
dils:::RssThisRadius(x=M, v1=5, v2=6, r=3)
dils:::RssThisRadius(x=M, v1=5, v2=6, r=4)
```

---

ScalablePCA

*Perform Principal Component Analysis on a large data set*

---

## Description

Run prcomp on subsamples of the data set and compile the results for the first dimension.

## Usage

```
ScalablePCA(x, filename = NULL, db = NULL,
  subsample = 10000, n.subsamples = 1000, ignore.cols,
  use.cols, return.sds = FALSE, progress.bar = FALSE)
```

## Arguments

x	data.frame, data over which to run PCA
filename	character, name of the file containing the data. This must be a tab-delimited file with a header row formatted per the default options for <a href="#">read.delim</a> .
db	Object type, database connection to table containing the data (NOT IMPLEMENTED).
subsample	numeric or logical, If an integer, size of each subsample. If FALSE, runs PCA on entire data set.
n.subsamples	numeric, number of subsamples.
ignore.cols	numeric, indices of columns not to include.
use.cols	numeric, indices of columns to use.
return.sds	logical, if TRUE return the standard deviations of each network's edge weights.
progress.bar	logical, if TRUE then progress in running subsamples will be shown.

## Details

Scales the function [prcomp](#) to data sets with an arbitrarily large number of rows by running prcomp on repeated subsamples of the rows.



**Value**

If `return.sds` is `FALSE`, return named vector of component weights for first dimension of principal component analysis (see example for comparison to [prcomp](#)).

If `return.sds` is `TRUE`, return a list.

<code>coefficients</code>	named vector of the component weights for first dimension of principal component analysis (see example for
<code>sds</code>	named vector of the standard deviations of each network's edge weights.

**Author(s)**

Stephen R. Haptonstahl <[srh@haptonstahl.org](mailto:srh@haptonstahl.org)>

**References**

<https://github.com/shaptonstahl/>

**See Also**

[prcomp](#)

**Examples**

```
data(iris)          # provides example data
prcomp(iris[,1:4], center=FALSE, scale.=FALSE)$rotation[,1]
ScalablePCA(iris, subsample=10, use.cols=1:4)
ScalablePCA(iris, subsample=10, ignore.cols=5)
```

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