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GATE Question Paper 2018, CS Question Number 49

Q.49 Consider the minterm list form of a Boolean function F given below.

$$F(P,Q,R,S) = \sum m(0,2,5,7,9,11) + d(3,8,10,12,14)$$

Here, m denotes a minterm and d denotes a don't care term. The number of essential prime implicants of the function F is ____.

ANSWER

1. Create the 4 variable K-map:

We have a function F(P,Q,R,S) with 4 variables, so we'll need a 4-variable K-map.

RS	00	01	11	10
PQ 00	m_0	m_1	m_3	m_2
PQ 01	m_4	m_5	m_7	m_6
PQ 11	m_{12}	m_{13}	m_{15}	m_{14}
PQ 10	m_8	m_9	m_{11}	m_{10}

2. Fill in the minterms (m) and don't cares (d):

• Minterms (m): 0, 2, 5, 7, 9, 11

• Don't cares (d): 3, 8, 10, 12, 14

RS	00	01	11	10
PQ 00	1	0	1	1
PQ 01	0	1	1	0
PQ 11	d	0	0	d
PQ 10	d	1	1	d

Table 1: k map for(p,q,r,s)

	$00(r'\dot{s}')$	$01(r'\dot{s})$	11(rs)	$10(r\dot{s}')$
$00(p'\dot{q}')$	1		X	1
$01(p'\dot{q})$		1	1	
11(pq)	X			X
$10(p'\dot{q})$	X	1	1	X

3. Identify the prime implicants:

Prime implicant: A group of 1's (or 1's and don't cares) that cannot be further combined into a larger group.

Let's look for the largest possible groups:

- Group 1: The 1's in cells 8, 9, 10 and 11 can be combined: PQ'
- Group 2: The 1's in cells 0, 2, 8 and 10 can be combined: PS'
- Group 3: The 1's in cells 2, 3, 10 and 11 can be combined: RQ'

4. Identify the essential prime implicants:

Essential prime implicant: A prime implicant that covers at least one minterm that is not covered by any other prime implicant.

Let's check each minterm:

- Minterm 0: Covered only by P'Q'S' (Essential)
- Minterm 2: Covered only by P'Q'S' (Essential)
- Minterm 9: Covered only by PQ'S (Essential)

Therefore, all for all three implicants are essential.

Answer: The number of essential prime implicants of the function F is 3.