



## **Mechanical, Automotive, & Materials Engineering**

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## CHAPTER 1

# INTRODUCTION

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### 1.1 Geometry Diagram

The system geometry is shown in the following diagram.

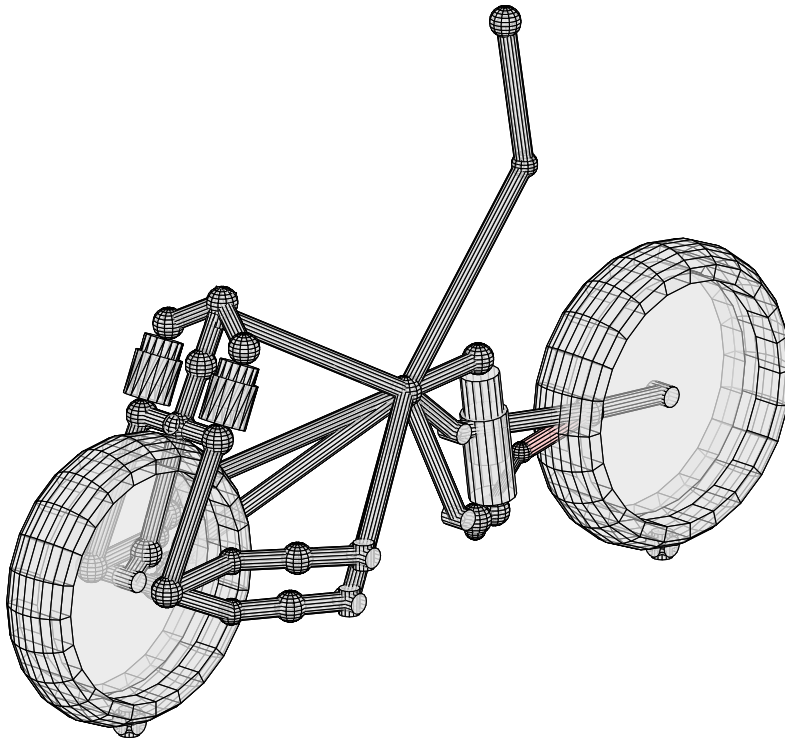


Figure 1.1: Geometry

## 1.2 System Description

The properties of the bodies are given in Tables 1.1 and 1.2. The properties of the connections are given in Tables 1.3, 1.4, and 1.5.

**Table 1.1:** Body CG Locations and Mass

| No. | Body Name         | Location [m]         | Mass [kg] |
|-----|-------------------|----------------------|-----------|
| 1   | bike              | 0.678, 0.000, 0.472  | 165.130   |
| 2   | upper body        | 0.415, 0.000, 1.140  | 33.680    |
| 3   | upper fork        | 1.164, 0.000, 0.770  | 9.990     |
| 4   | lower fork        | 1.365, 0.000, 0.324  | 7.250     |
| 5   | swing arm         | 0.196, 0.000, 0.311  | 8.000     |
| 6   | bell crank        | 0.493, 0.000, 0.173  | 0.000     |
| 7   | front wheel, bike | 1.410, 0.000, 0.282  | 11.900    |
| 8   | rear wheel, bike  | 0.000, 0.000, 0.297  | 14.700    |
| 9   | fork rod          | 1.276, 0.000, 0.550  | 0.000     |
| 10  | left fork arm     | 1.410, 0.100, 0.282  | 0.000     |
| 11  | right fork arm    | 1.410, -0.100, 0.282 | 0.000     |
| 12  | steer arm         | 1.220, 0.000, 0.660  | 0.000     |
| 13  | lower left arm    | 1.140, 0.156, 0.200  | 2.000     |
| 14  | upper left arm    | 1.140, 0.175, 0.300  | 2.000     |
| 15  | lower right arm   | 1.140, -0.156, 0.200 | 2.000     |
| 16  | upper right arm   | 1.140, -0.175, 0.300 | 2.000     |

**Table 1.2:** Body Inertia Properties

| No. | Body Name         | Inertia [kg·m <sup>2</sup> ] ( $I_{xx}$ , $I_{yy}$ , $I_{zz}$ ; $I_{xy}$ , $I_{yz}$ , $I_{zx}$ ) |
|-----|-------------------|--|
| 1   | bike              | 11.085, 22.013, 14.982; 0.000, 0.000, 3.691  |
| 2   | upper body        | 1.428, 1.347, 0.916; 0.000, 0.000, -0.443  |
| 3   | upper fork        | 1.341, 1.548, 0.413; 0.000, 0.000, 0.000   |
| 4   | lower fork        | 0.000, 0.000, 0.000; 0.000, 0.000, 0.000   |
| 5   | swing arm         | 0.020, 0.259, 0.259; 0.000, 0.000, 0.000   |
| 6   | bell crank        | 0.000, 0.000, 0.000; 0.000, 0.000, 0.000   |
| 7   | front wheel, bike | 0.270, 0.484, 0.270; 0.000, 0.000, 0.000   |
| 8   | rear wheel, bike  | 0.383, 0.638, 0.383; 0.000, 0.000, 0.000   |
| 9   | fork rod          | 0.000, 0.000, 0.000; 0.000, 0.000, 0.000   |
| 10  | left fork arm     | 0.000, 0.000, 0.000; 0.000, 0.000, 0.000   |
| 11  | right fork arm    | 0.000, 0.000, 0.000; 0.000, 0.000, 0.000   |
| 12  | steer arm         | 0.000, 0.000, 0.000; 0.000, 0.000, 0.000   |
| 13  | lower left arm    | 0.002, 0.007, 0.009; -0.004, 0.000, 0.000  |
| 14  | upper left arm    | 0.004, 0.007, 0.010; -0.005, 0.000, 0.000  |
| 15  | lower right arm   | 0.002, 0.007, 0.009; 0.004, 0.000, 0.000   |
| 16  | upper right arm   | 0.004, 0.007, 0.010; 0.005, 0.000, 0.000   |

Note: inertias are defined as the positive integral over the body, e.g.,  
 $I_{xy} = + \int r_x r_y dm$ .

**Table 1.3:** Connection Location and Direction

| No. | Connection Name         | Location [m]         | Unit Axis            |
|-----|-------------------------|----------------------|----------------------|
| 1   | rear axle               | 0.000, 0.000, 0.297  | 0.000, 1.000, 0.000  |
| 2   | arm pivot               | 0.549, 0.000, 0.361  | 0.000, 1.000, 0.000  |
| 3   | bell crank pivot        | 0.539, 0.000, 0.188  | 0.000, 1.000, 0.000  |
| 4   | rider                   | 0.364, 0.000, 0.844  | 0.000, 1.000, 0.000  |
| 5   | steering head           | 1.173, 0.000, 0.749  | 0.407, 0.000, -0.914 |
| 6   | front axle              | 1.410, 0.000, 0.282  | 0.000, 1.000, 0.000  |
| 7   | left fork joint         | 1.276, 0.100, 0.550  | - , - , -            |
| 8   | right fork joint        | 1.276, -0.100, 0.550 | - , - , -            |
| 9   | joint                   | 1.040, 0.212, 0.200  | 1.000, 0.000, 0.000  |
| 10  | joint                   | 1.240, 0.100, 0.200  | - , - , -            |
| 11  | joint                   | 1.040, 0.250, 0.300  | 1.000, 0.000, 0.000  |
| 12  | joint                   | 1.240, 0.100, 0.300  | - , - , -            |
| 13  | joint                   | 1.040, -0.212, 0.200 | 1.000, 0.000, 0.000  |
| 14  | joint                   | 1.240, -0.100, 0.200 | - , - , -            |
| 15  | joint                   | 1.040, -0.250, 0.300 | 1.000, 0.000, 0.000  |
| 16  | joint                   | 1.240, -0.100, 0.300 | - , - , -            |
| 17  | steering arm joint 1    | 1.164, 0.000, 0.770  | -0.447, 0.000, 0.894 |
| 18  | steering arm joint 2    | 1.276, 0.000, 0.550  | -0.447, 0.000, 0.894 |
| 19  | fork joint              | 1.276, 0.000, 0.550  | -0.447, 0.000, 0.894 |
| 20  | front tire lateral      | 1.410, 0.000, 0.000  | 0.000, 1.000, 0.000  |
| 21  | rear tire lateral       | 0.000, 0.000, 0.000  | 0.000, 1.000, 0.000  |
| 22  | front tire longitudinal | 1.410, 0.000, 0.000  | 1.000, 0.000, 0.000  |
| 23  | rear tire longitudinal  | 0.000, 0.000, 0.000  | 1.000, 0.000, 0.000  |
| 24  | front tire vertical     | 1.410, 0.000, 0.000  | 0.000, 0.000, 1.000  |
| 25  | rear tire vertical      | 0.000, 0.000, 0.000  | 0.000, 0.000, 1.000  |

**Table 1.4:** Connection Locations

| No. | Connection Name    | Location [m]         | Location [m]         |
|-----|--------------------|----------------------|----------------------|
| 1   | rear spring        | 0.487, 0.000, 0.489  | 0.444, 0.000, 0.178  |
| 2   | right front spring | 1.206, -0.100, 0.714 | 1.276, -0.100, 0.550 |
| 3   | left front spring  | 1.206, 0.100, 0.714  | 1.276, 0.100, 0.550  |
| 4   | rear pull rod      | 0.372, 0.000, 0.275  | 0.495, 0.000, 0.152  |

**Table 1.5:** Connection Properties

| No. | Connection Name         | Stiffness [N/m] | Damping [Ns/m] |
|-----|-------------------------|-----------------|----------------|
| 1   | front tire lateral      | 0               | 4,000          |
| 2   | rear tire lateral       | 0               | 4,000          |
| 3   | front tire longitudinal | 0               | 6,000          |
| 4   | rear tire longitudinal  | 0               | 6,000          |
| 5   | front tire vertical     | 130,000         | 0              |
| 6   | rear tire vertical      | 141,000         | 0              |
| 1   | rear spring             | 58,570          | 11,650         |
| 2   | right front spring      | 12,500          | 1,067          |
| 3   | left front spring       | 12,500          | 1,067          |

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## CHAPTER 2

# ANALYSIS

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Replace this text with the body of your report. Add sections or subsections as appropriate.

### 2.1 Eigenvalue Analysis

The eigenvalue properties are given in Tables 2.1 and 2.2.

Table 2.1: Eigenvalues

| No. | Real [rad/s]                    | Imaginary [rad/s]              | Real [Hz]                       | Imaginary [Hz]                 |
|-----|---------------------------------|--------------------------------|---------------------------------|--------------------------------|
| 1   | $-1.0235713109 \times 10^3$     | $0.0000000000 \times 10^0$     | $-1.6290643373 \times 10^2$     | $0.0000000000 \times 10^0$     |
| 2   | $-8.5584181906 \times 10^2$     | $0.0000000000 \times 10^0$     | $-1.3621145601 \times 10^2$     | $0.0000000000 \times 10^0$     |
| 3   | $-1.1961513311 \times 10^2$     | $1.3472965152 \times 10^2$     | $-1.9037339703 \times 10^1$     | $2.1442890021 \times 10^1$     |
| 4   | $-1.1961513311 \times 10^2$     | $-1.3472965152 \times 10^2$    | $-1.9037339703 \times 10^1$     | $-2.1442890021 \times 10^1$    |
| 5   | $-1.0652306175 \times 10^2$     | $0.0000000000 \times 10^0$     | $-1.6953671832 \times 10^1$     | $0.0000000000 \times 10^0$     |
| 6   | $-9.6216901283 \times 10^1$     | $0.0000000000 \times 10^0$     | $-1.5313395448 \times 10^1$     | $0.0000000000 \times 10^0$     |
| 7   | $-4.2153340178 \times 10^1$     | $5.0945855064 \times 10^1$     | $-6.7089124571 \times 10^0$     | $8.1082846635 \times 10^0$     |
| 8   | $-4.2153340178 \times 10^1$     | $-5.0945855064 \times 10^1$    | $-6.7089124571 \times 10^0$     | $-8.1082846635 \times 10^0$    |
| 9   | $-3.3979900604 \times 10^0$     | $3.6416317307 \times 10^1$     | $-5.4080691468 \times 10^{-1}$  | $5.7958369085 \times 10^0$     |
| 10  | $-3.3979900604 \times 10^0$     | $-3.6416317307 \times 10^1$    | $-5.4080691468 \times 10^{-1}$  | $-5.7958369085 \times 10^0$    |
| 11  | $-1.2048595998 \times 10^1$     | $1.6188197076 \times 10^1$     | $-1.9175936103 \times 10^0$     | $2.5764315844 \times 10^0$     |
| 12  | $-1.2048595998 \times 10^1$     | $-1.6188197076 \times 10^1$    | $-1.9175936103 \times 10^0$     | $-2.5764315844 \times 10^0$    |
| 13  | $-1.2803100038 \times 10^1$     | $9.5187926500 \times 10^0$     | $-2.0376766580 \times 10^0$     | $1.5149629025 \times 10^0$     |
| 14  | $-1.2803100038 \times 10^1$     | $-9.5187926500 \times 10^0$    | $-2.0376766580 \times 10^0$     | $-1.5149629025 \times 10^0$    |
| 15  | $-7.2666127400 \times 10^0$     | $0.0000000000 \times 10^0$     | $-1.1565173371 \times 10^0$     | $0.0000000000 \times 10^0$     |
| 16  | $-1.4958693993 \times 10^{-12}$ | $1.1175970408 \times 10^{-6}$  | $-2.3807500911 \times 10^{-13}$ | $1.7787109342 \times 10^{-7}$  |
| 17  | $-1.4958693993 \times 10^{-12}$ | $-1.1175970408 \times 10^{-6}$ | $-2.3807500911 \times 10^{-13}$ | $-1.7787109342 \times 10^{-7}$ |
| 18  | $1.1065797246 \times 10^0$      | $0.0000000000 \times 10^0$     | $1.7611763309 \times 10^{-1}$   | $0.0000000000 \times 10^0$     |
| 19  | $-2.2818588554 \times 10^{-13}$ | $2.6312696740 \times 10^{-6}$  | $-3.6316911628 \times 10^{-14}$ | $4.1877957523 \times 10^{-7}$  |
| 20  | $-2.2818588554 \times 10^{-13}$ | $-2.6312696740 \times 10^{-6}$ | $-3.6316911628 \times 10^{-14}$ | $-4.1877957523 \times 10^{-7}$ |
| 21  | $-1.9605760675 \times 10^{-12}$ | $0.0000000000 \times 10^0$     | $-3.1203537244 \times 10^{-13}$ | $0.0000000000 \times 10^0$     |
| 22  | $-9.8910142123 \times 10^{-12}$ | $0.0000000000 \times 10^0$     | $-1.5742038041 \times 10^{-12}$ | $0.0000000000 \times 10^0$     |

Note: oscillatory roots appear as complex conjugates.



Table 2.2: Eigenvalue Analysis

| No. | Frequency ( $\omega_n$ ) [Hz] | Damping Ratio ( $\zeta$ )     | Time Constant ( $\tau$ ) [s]   | Wavelength ( $\lambda$ ) [s]  |
|-----|-------------------------------|-------------------------------|--------------------------------|-------------------------------|
| 1   | —                             | —                             | $9.7697150103 \times 10^{-4}$  | —                             |
| 2   | —                             | —                             | $1.1684402161 \times 10^{-3}$  | —                             |
| 3   | $2.8674341063 \times 10^1$    | $6.6391550764 \times 10^{-1}$ | $8.3601461954 \times 10^{-3}$  | $4.6635504777 \times 10^{-2}$ |
| 4   | $2.8674341063 \times 10^1$    | $6.6391550764 \times 10^{-1}$ | $8.3601461954 \times 10^{-3}$  | $4.6635504777 \times 10^{-2}$ |
| 5   | —                             | —                             | $9.3876385407 \times 10^{-3}$  | —                             |
| 6   | —                             | —                             | $1.0393184427 \times 10^{-2}$  | —                             |
| 7   | $1.0523962492 \times 10^1$    | $6.3748920257 \times 10^{-1}$ | $2.3722912485 \times 10^{-2}$  | $1.2333064779 \times 10^{-1}$ |
| 8   | $1.0523962492 \times 10^1$    | $6.3748920257 \times 10^{-1}$ | $2.3722912485 \times 10^{-2}$  | $1.2333064779 \times 10^{-1}$ |
| 9   | $5.8210134504 \times 10^0$    | $9.2905972352 \times 10^{-2}$ | $2.9429162012 \times 10^{-1}$  | $1.7253763620 \times 10^{-1}$ |
| 10  | $5.8210134504 \times 10^0$    | $9.2905972352 \times 10^{-2}$ | $2.9429162012 \times 10^{-1}$  | $1.7253763620 \times 10^{-1}$ |
| 11  | $3.2117230521 \times 10^0$    | $5.9706069896 \times 10^{-1}$ | $8.2997222265 \times 10^{-2}$  | $3.8813372964 \times 10^{-1}$ |
| 12  | $3.2117230521 \times 10^0$    | $5.9706069896 \times 10^{-1}$ | $8.2997222265 \times 10^{-2}$  | $3.8813372964 \times 10^{-1}$ |
| 13  | $2.5391413427 \times 10^0$    | $8.0250619517 \times 10^{-1}$ | $7.8106083451 \times 10^{-2}$  | $6.6008216989 \times 10^{-1}$ |
| 14  | $2.5391413427 \times 10^0$    | $8.0250619517 \times 10^{-1}$ | $7.8106083451 \times 10^{-2}$  | $6.6008216989 \times 10^{-1}$ |
| 15  | —                             | —                             | $1.3761570016 \times 10^{-1}$  | —                             |
| 16  | $1.7787109342 \times 10^{-7}$ | $1.3384693630 \times 10^{-6}$ | $6.6850755854 \times 10^{11}$  | $5.6220489837 \times 10^6$    |
| 17  | $1.7787109342 \times 10^{-7}$ | $1.3384693630 \times 10^{-6}$ | $6.6850755854 \times 10^{11}$  | $5.6220489837 \times 10^6$    |
| 18  | —                             | —                             | $-9.0368545327 \times 10^{-1}$ | —                             |
| 19  | $4.1877957523 \times 10^{-7}$ | $8.6720828275 \times 10^{-8}$ | $4.3823920030 \times 10^{12}$  | $2.3878910509 \times 10^6$    |
| 20  | $4.1877957523 \times 10^{-7}$ | $8.6720828275 \times 10^{-8}$ | $4.3823920030 \times 10^{12}$  | $2.3878910509 \times 10^6$    |
| 21  | —                             | —                             | $5.1005417061 \times 10^{11}$  | —                             |
| 22  | —                             | —                             | $1.0110186666 \times 10^{11}$  | —                             |

Notes: a) oscillatory roots are listed twice, b) negative time constants denote unstable roots.

There are 11 degrees of freedom.

There are 7 oscillatory modes, 14 damped modes, 1 unstable modes, and 0 rigid body modes.

## 2.2 Frequency Response Plots

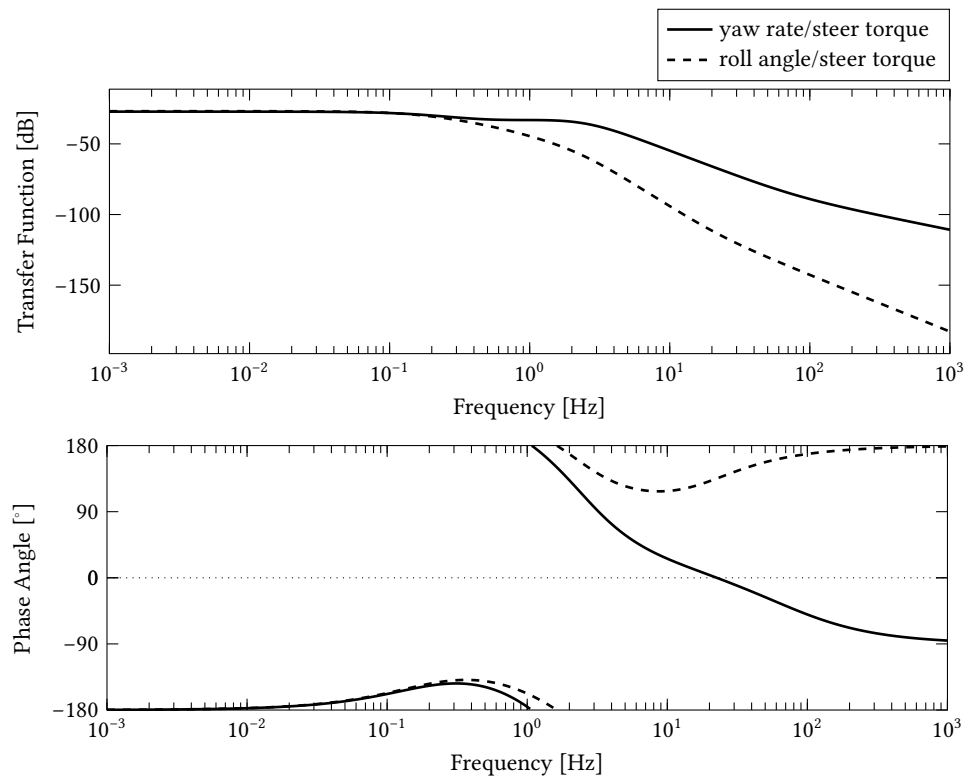


Figure 2.1: Frequency response: steer torque

## 2.3 Steady State Gains

The steady state gains are given in Table 2.3.

Table 2.3: Steady State Gains

| No. | Output/Input            | Gain                           |
|-----|-------------------------|--------------------------------|
| 1   | yaw rate/steer torque   | $-3.7647960000 \times 10^{-2}$ |
| 2   | roll angle/steer torque | $-2.9888300000 \times 10^{-2}$ |

## 2.4 Equilibrium Analysis

The results of the equilibrium load analysis are given in Tables 2.4 and 2.5.

Table 2.4: System Static Deflections

| No. | Body Name         | Type        | Deflection [m] or [rad]   |
|-----|-------------------|-------------|---|
| 1   | bike              | translation | $1.0339 \times 10^{-3}, 0.0000 \times 10^0, -6.4458 \times 10^{-2}$     |
| –   | –                 | rotation    | $0.0000 \times 10^0, -1.1227 \times 10^{-2}, 0.0000 \times 10^0$        |
| 2   | upper body        | translation | $-6.4613 \times 10^{-3}, 0.0000 \times 10^0, -6.7410 \times 10^{-2}$    |
| –   | –                 | rotation    | $0.0000 \times 10^0, -1.1227 \times 10^{-2}, 0.0000 \times 10^0$        |
| 3   | upper fork        | translation | $-2.3073 \times 10^{-3}, 0.0000 \times 10^0, -5.9001 \times 10^{-2}$    |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, -1.1227 \times 10^{-2}, 2.0000 \times 10^{-8}$ |
| 4   | lower fork        | translation | $2.7000 \times 10^{-3}, 0.0000 \times 10^0, -9.8662 \times 10^{-3}$     |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, -1.1227 \times 10^{-2}, 2.0000 \times 10^{-8}$ |
| 5   | swing arm         | translation | $-2.8111 \times 10^{-3}, 0.0000 \times 10^0, -2.9551 \times 10^{-2}$    |
| –   | –                 | rotation    | $0.0000 \times 10^0, 1.0299 \times 10^{-1}, 0.0000 \times 10^0$         |
| 6   | bell crank        | translation | $-1.2558 \times 10^{-3}, 0.0000 \times 10^0, -4.9138 \times 10^{-2}$    |
| –   | –                 | rotation    | $0.0000 \times 10^0, 3.6404 \times 10^{-1}, 0.0000 \times 10^0$         |
| 7   | front wheel, bike | translation | $3.1716 \times 10^{-3}, 0.0000 \times 10^0, -9.3610 \times 10^{-3}$     |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, 0.0000 \times 10^0, 2.0000 \times 10^{-8}$     |
| 8   | rear wheel, bike  | translation | $-4.2838 \times 10^{-3}, 1.0000 \times 10^{-8}, -9.3647 \times 10^{-3}$ |
| –   | –                 | rotation    | $0.0000 \times 10^0, 0.0000 \times 10^0, 0.0000 \times 10^0$            |
| 9   | fork rod          | translation | $1.5731 \times 10^{-4}, 0.0000 \times 10^0, -1.0864 \times 10^{-2}$     |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, -1.1227 \times 10^{-2}, 2.0000 \times 10^{-8}$ |
| 10  | left fork arm     | translation | $3.1716 \times 10^{-3}, 0.0000 \times 10^0, -9.3610 \times 10^{-3}$     |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, -1.1227 \times 10^{-2}, 2.0000 \times 10^{-8}$ |
| 11  | right fork arm    | translation | $3.1716 \times 10^{-3}, 0.0000 \times 10^0, -9.3610 \times 10^{-3}$     |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, -1.1227 \times 10^{-2}, 2.0000 \times 10^{-8}$ |
| 12  | steer arm         | translation | $-1.0410 \times 10^{-2}, 0.0000 \times 10^0, -1.6262 \times 10^{-2}$    |
| –   | –                 | rotation    | $-1.0000 \times 10^{-8}, -9.6277 \times 10^{-2}, 2.0000 \times 10^{-8}$ |
| 13  | lower left arm    | translation | $4.0922 \times 10^{-3}, 0.0000 \times 10^0, -3.5831 \times 10^{-2}$     |
| –   | –                 | rotation    | $0.0000 \times 10^0, -2.4562 \times 10^{-1}, -2.0000 \times 10^{-8}$    |
| 14  | upper left arm    | translation | $2.9695 \times 10^{-3}, 0.0000 \times 10^0, -3.5831 \times 10^{-2}$     |
| –   | –                 | rotation    | $0.0000 \times 10^0, -2.4562 \times 10^{-1}, -2.0000 \times 10^{-8}$    |
| 15  | lower right arm   | translation | $4.0922 \times 10^{-3}, 0.0000 \times 10^0, -3.5831 \times 10^{-2}$     |
| –   | –                 | rotation    | $0.0000 \times 10^0, -2.4562 \times 10^{-1}, -2.0000 \times 10^{-8}$    |
| 16  | upper right arm   | translation | $2.9695 \times 10^{-3}, 0.0000 \times 10^0, -3.5831 \times 10^{-2}$     |
| –   | –                 | rotation    | $0.0000 \times 10^0, -2.4562 \times 10^{-1}, -2.0000 \times 10^{-8}$    |

Table 2.5: System Preloads

| No. | Connector Name          | Type   | Load [N] or [Nm] (Components; Magnitude) |                       |                       |                       |
|-----|-------------------------|--------|--|-----------------------|-----------------------|-----------------------|
| 1   | rear axle               | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $1.1762 \times 10^3$  | $1.1762 \times 10^3$  |
| 2   | arm pivot               | force  | $-2.3492 \times 10^3$                    | $0.0000 \times 10^0$  | $1.2553 \times 10^3$  | $2.6635 \times 10^3$  |
| 3   | bell crank pivot        | force  | $2.6261 \times 10^3$                     | $0.0000 \times 10^0$  | $-3.3862 \times 10^2$ | $2.6478 \times 10^3$  |
| 4   | rider                   | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $3.3040 \times 10^2$  | $3.3040 \times 10^2$  |
| –   | –                       | moment | $0.0000 \times 10^0$                     | $-1.6850 \times 10^1$ | $0.0000 \times 10^0$  | $1.6850 \times 10^1$  |
| 5   | steering head           | force  | $4.2458 \times 10^2$                     | $0.0000 \times 10^0$  | $-8.9183 \times 10^2$ | $9.8774 \times 10^2$  |
| –   | –                       | moment | $0.0000 \times 10^0$                     | $1.8686 \times 10^1$  | $0.0000 \times 10^0$  | $1.8686 \times 10^1$  |
| 6   | front axle              | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $1.1002 \times 10^3$  | $1.1002 \times 10^3$  |
| 7   | left fork joint         | force  | $2.1229 \times 10^2$                     | $-1.2543 \times 10^2$ | $1.9620 \times 10^1$  | $2.4736 \times 10^2$  |
| –   | –                       | moment | $-4.1547 \times 10^1$                    | $-7.0475 \times 10^1$ | $4.5332 \times 10^0$  | $8.1936 \times 10^1$  |
| 8   | right fork joint        | force  | $2.1229 \times 10^2$                     | $1.2543 \times 10^2$  | $1.9620 \times 10^1$  | $2.4736 \times 10^2$  |
| –   | –                       | moment | $4.1547 \times 10^1$                     | $-7.0475 \times 10^1$ | $-4.5332 \times 10^0$ | $8.1936 \times 10^1$  |
| 9   | joint                   | force  | $-1.8010 \times 10^2$                    | $1.0129 \times 10^2$  | $9.8100 \times 10^0$  | $2.0686 \times 10^2$  |
| 10  | joint                   | force  | $1.8010 \times 10^2$                     | $-1.0129 \times 10^2$ | $9.8100 \times 10^0$  | $2.0686 \times 10^2$  |
| 11  | joint                   | force  | $-3.2189 \times 10^1$                    | $2.4142 \times 10^1$  | $9.8100 \times 10^0$  | $4.1415 \times 10^1$  |
| 12  | joint                   | force  | $3.2189 \times 10^1$                     | $-2.4142 \times 10^1$ | $9.8100 \times 10^0$  | $4.1415 \times 10^1$  |
| 13  | joint                   | force  | $-1.8010 \times 10^2$                    | $-1.0129 \times 10^2$ | $9.8100 \times 10^0$  | $2.0686 \times 10^2$  |
| 14  | joint                   | force  | $1.8010 \times 10^2$                     | $1.0129 \times 10^2$  | $9.8100 \times 10^0$  | $2.0686 \times 10^2$  |
| 15  | joint                   | force  | $-3.2189 \times 10^1$                    | $-2.4142 \times 10^1$ | $9.8100 \times 10^0$  | $4.1415 \times 10^1$  |
| 16  | joint                   | force  | $3.2189 \times 10^1$                     | $2.4142 \times 10^1$  | $9.8100 \times 10^0$  | $4.1415 \times 10^1$  |
| 17  | steering arm joint 1    | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  |
| 18  | steering arm joint 2    | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  |
| 19  | fork joint              | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $1.0291 \times 10^3$  | $1.0291 \times 10^3$  |
| –   | –                       | moment | $0.0000 \times 10^0$                     | $-1.4095 \times 10^2$ | $0.0000 \times 10^0$  | $1.4095 \times 10^2$  |
| 20  | front tire lateral      | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  |
| 21  | rear tire lateral       | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  |
| 22  | front tire longitudinal | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  |
| 23  | rear tire longitudinal  | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  | $0.0000 \times 10^0$  |
| 24  | front tire vertical     | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $1.2169 \times 10^3$  | $1.2169 \times 10^3$  |
| 25  | rear tire vertical      | force  | $0.0000 \times 10^0$                     | $0.0000 \times 10^0$  | $1.3204 \times 10^3$  | $1.3204 \times 10^3$  |
| 26  | rear spring             | force  | $2.7693 \times 10^2$                     | $0.0000 \times 10^0$  | $2.0144 \times 10^3$  | $-2.0333 \times 10^3$ |
| 27  | right front spring      | force  | $-2.1229 \times 10^2$                    | $0.0000 \times 10^0$  | $4.9491 \times 10^2$  | $-5.3852 \times 10^2$ |
| 28  | left front spring       | force  | $-2.1229 \times 10^2$                    | $0.0000 \times 10^0$  | $4.9491 \times 10^2$  | $-5.3852 \times 10^2$ |
| 29  | rear pull rod           | force  | $2.3492 \times 10^3$                     | $0.0000 \times 10^0$  | $-2.3530 \times 10^3$ | $3.3249 \times 10^3$  |

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## CHAPTER 3

## CONCLUSION

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Replace this text with the conclusion to your report.

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## APPENDIX A

# EQUATIONS OF MOTION

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The equations of motion are of the form

$$\begin{bmatrix} \mathbf{I} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{M} & -\mathbf{G} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{Bmatrix} \dot{\mathbf{p}} \\ \dot{\mathbf{w}} \\ \dot{\mathbf{u}} \end{Bmatrix} + \begin{bmatrix} \mathbf{V} & -\mathbf{I} & \mathbf{0} \\ \mathbf{K} & \mathbf{L} & -\mathbf{F} \\ \mathbf{0} & \mathbf{0} & \mathbf{I} \end{bmatrix} \begin{Bmatrix} \mathbf{p} \\ \mathbf{w} \\ \mathbf{u} \end{Bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{I} \end{bmatrix} \{ \mathbf{u} \}$$

The mass matrix of the system is

| Row | Column | Value                       | Row | Column | Value                        |
|-----|--------|-----------------------------|-----|--------|------------------------------|
| 1   | 1      | $1.65130000 \times 10^2$    | 44  | 44     | $1.47000000 \times 10^1$     |
| 2   | 2      | $1.65130000 \times 10^2$    | 45  | 45     | $1.47000000 \times 10^1$     |
| 3   | 3      | $1.65130000 \times 10^2$    | 46  | 46     | $3.83000000 \times 10^{-1}$  |
| 4   | 4      | $1.10850000 \times 10^1$    | 47  | 47     | $6.38000000 \times 10^{-1}$  |
| 6   | 4      | $-3.69100000 \times 10^0$   | 48  | 48     | $3.83000000 \times 10^{-1}$  |
| 5   | 5      | $2.20130000 \times 10^1$    | 73  | 73     | $2.00000000 \times 10^0$     |
| 4   | 6      | $-3.69100000 \times 10^0$   | 74  | 74     | $2.00000000 \times 10^0$     |
| 6   | 6      | $1.49820000 \times 10^1$    | 75  | 75     | $2.00000000 \times 10^0$     |
| 7   | 7      | $3.36800000 \times 10^1$    | 76  | 76     | $2.10862507 \times 10^{-3}$  |
| 8   | 8      | $3.36800000 \times 10^1$    | 77  | 76     | $3.74933333 \times 10^{-3}$  |
| 9   | 9      | $3.36800000 \times 10^1$    | 76  | 77     | $3.74933333 \times 10^{-3}$  |
| 10  | 10     | $1.42800000 \times 10^0$    | 77  | 77     | $6.66666667 \times 10^{-3}$  |
| 12  | 10     | $4.43000000 \times 10^{-1}$ | 78  | 78     | $8.77529173 \times 10^{-3}$  |
| 11  | 11     | $1.34700000 \times 10^0$    | 79  | 79     | $2.00000000 \times 10^0$     |
| 10  | 12     | $4.43000000 \times 10^{-1}$ | 80  | 80     | $2.00000000 \times 10^0$     |
| 12  | 12     | $9.16000000 \times 10^{-1}$ | 81  | 81     | $2.00000000 \times 10^0$     |
| 13  | 13     | $9.99000000 \times 10^0$    | 82  | 82     | $3.75000000 \times 10^{-3}$  |
| 14  | 14     | $9.99000000 \times 10^0$    | 83  | 82     | $5.00000000 \times 10^{-3}$  |
| 15  | 15     | $9.99000000 \times 10^0$    | 82  | 83     | $5.00000000 \times 10^{-3}$  |
| 16  | 16     | $1.34100000 \times 10^0$    | 83  | 83     | $6.66666667 \times 10^{-3}$  |
| 17  | 17     | $1.54800000 \times 10^0$    | 84  | 84     | $1.04166667 \times 10^{-2}$  |
| 18  | 18     | $4.12500000 \times 10^{-1}$ | 85  | 85     | $2.00000000 \times 10^0$     |
| 19  | 19     | $7.25000000 \times 10^0$    | 86  | 86     | $2.00000000 \times 10^0$     |
| 20  | 20     | $7.25000000 \times 10^0$    | 87  | 87     | $2.00000000 \times 10^0$     |
| 21  | 21     | $7.25000000 \times 10^0$    | 88  | 88     | $2.10862507 \times 10^{-3}$  |
| 25  | 25     | $8.00000000 \times 10^0$    | 89  | 88     | $-3.74933333 \times 10^{-3}$ |

## A. EQUATIONS OF MOTION

|    |    |                             |    |    |                              |
|----|----|-----------------------------|----|----|------------------------------|
| 26 | 26 | $8.00000000 \times 10^0$    | 88 | 89 | $-3.74933333 \times 10^{-3}$ |
| 27 | 27 | $8.00000000 \times 10^0$    | 89 | 89 | $6.66666667 \times 10^{-3}$  |
| 28 | 28 | $2.00000000 \times 10^{-2}$ | 90 | 90 | $8.77529173 \times 10^{-3}$  |
| 29 | 29 | $2.59000000 \times 10^{-1}$ | 91 | 91 | $2.00000000 \times 10^0$     |
| 30 | 30 | $2.59000000 \times 10^{-1}$ | 92 | 92 | $2.00000000 \times 10^0$     |
| 37 | 37 | $1.19000000 \times 10^1$    | 93 | 93 | $2.00000000 \times 10^0$     |
| 38 | 38 | $1.19000000 \times 10^1$    | 94 | 94 | $3.75000000 \times 10^{-3}$  |
| 39 | 39 | $1.19000000 \times 10^1$    | 95 | 94 | $-5.00000000 \times 10^{-3}$ |
| 40 | 40 | $2.70000000 \times 10^{-1}$ | 94 | 95 | $-5.00000000 \times 10^{-3}$ |
| 41 | 41 | $4.84000000 \times 10^{-1}$ | 95 | 95 | $6.66666667 \times 10^{-3}$  |
| 42 | 42 | $2.70000000 \times 10^{-1}$ | 96 | 96 | $1.04166667 \times 10^{-2}$  |
| 43 | 43 | $1.47000000 \times 10^1$    | —  | —  | —                            |

The damping matrix is

| Row | Column | Value                       | Row | Column | Value                     |
|-----|--------|-----------------------------|-----|--------|---------------------------|
| 1   | 1      | $2.16096323 \times 10^2$    | 1   | 33     | $-1.57188566 \times 10^3$ |
| 3   | 1      | $1.57188566 \times 10^3$    | 3   | 33     | $-1.14339037 \times 10^4$ |
| 5   | 1      | $3.03616953 \times 10^2$    | 5   | 33     | $-2.20851114 \times 10^3$ |
| 31  | 1      | $-2.16096323 \times 10^2$   | 31  | 33     | $1.57188566 \times 10^3$  |
| 33  | 1      | $-1.57188566 \times 10^3$   | 33  | 33     | $1.14339037 \times 10^4$  |
| 35  | 1      | $-7.71558003 \times 10^1$   | 35  | 33     | $5.61231653 \times 10^2$  |
| 1   | 3      | $1.57188566 \times 10^3$    | 1   | 35     | $-7.71558003 \times 10^1$ |
| 3   | 3      | $1.14339037 \times 10^4$    | 3   | 35     | $-5.61231653 \times 10^2$ |
| 5   | 3      | $2.20851114 \times 10^3$    | 5   | 35     | $-1.08404478 \times 10^2$ |
| 31  | 3      | $-1.57188566 \times 10^3$   | 31  | 35     | $7.71558003 \times 10^1$  |
| 33  | 3      | $-1.14339037 \times 10^4$   | 33  | 35     | $5.61231653 \times 10^2$  |
| 35  | 3      | $-5.61231653 \times 10^2$   | 35  | 35     | $2.75479816 \times 10^1$  |
| 1   | 5      | $3.03616953 \times 10^2$    | 37  | 37     | $6.00000000 \times 10^3$  |
| 3   | 5      | $2.20851114 \times 10^3$    | 41  | 37     | $-1.69200000 \times 10^3$ |
| 5   | 5      | $4.26584094 \times 10^2$    | 38  | 38     | $4.00000000 \times 10^3$  |
| 31  | 5      | $-3.03616953 \times 10^2$   | 40  | 38     | $1.12800000 \times 10^3$  |
| 33  | 5      | $-2.20851114 \times 10^3$   | 38  | 40     | $1.12800000 \times 10^3$  |
| 35  | 5      | $-1.08404478 \times 10^2$   | 40  | 40     | $3.18096000 \times 10^2$  |
| 13  | 13     | $3.31623337 \times 10^2$    | 37  | 41     | $-1.69200000 \times 10^3$ |
| 15  | 13     | $-7.73117173 \times 10^2$   | 41  | 41     | $4.77144000 \times 10^2$  |
| 17  | 13     | $1.39000144 \times 10^1$    | 43  | 43     | $6.00000000 \times 10^3$  |
| 49  | 13     | $-3.31623337 \times 10^2$   | 47  | 43     | $-1.78200000 \times 10^3$ |
| 51  | 13     | $7.73117173 \times 10^2$    | 44  | 44     | $4.00000000 \times 10^3$  |
| 13  | 15     | $-7.73117173 \times 10^2$   | 46  | 44     | $1.18800000 \times 10^3$  |
| 15  | 15     | $1.80237666 \times 10^3$    | 44  | 46     | $1.18800000 \times 10^3$  |
| 17  | 15     | $-3.24052582 \times 10^1$   | 46  | 46     | $3.52836000 \times 10^2$  |
| 49  | 15     | $7.73117173 \times 10^2$    | 43  | 47     | $-1.78200000 \times 10^3$ |
| 51  | 15     | $-1.80237666 \times 10^3$   | 47  | 47     | $5.29254000 \times 10^2$  |
| 16  | 16     | $1.80237666 \times 10^1$    | 13  | 49     | $-3.31623337 \times 10^2$ |
| 18  | 16     | $7.73117173 \times 10^0$    | 15  | 49     | $7.73117173 \times 10^2$  |
| 52  | 16     | $-1.80237666 \times 10^1$   | 17  | 49     | $-1.39000144 \times 10^1$ |
| 54  | 16     | $-7.73117173 \times 10^0$   | 49  | 49     | $3.31623337 \times 10^2$  |
| 13  | 17     | $1.39000144 \times 10^1$    | 51  | 49     | $-7.73117173 \times 10^2$ |
| 15  | 17     | $-3.24052582 \times 10^1$   | 13  | 51     | $7.73117173 \times 10^2$  |
| 17  | 17     | $5.82620036 \times 10^{-1}$ | 15  | 51     | $-1.80237666 \times 10^3$ |
| 49  | 17     | $-1.39000144 \times 10^1$   | 17  | 51     | $3.24052582 \times 10^1$  |
| 51  | 17     | $3.24052582 \times 10^1$    | 49  | 51     | $-7.73117173 \times 10^2$ |
| 16  | 18     | $7.73117173 \times 10^0$    | 51  | 51     | $1.80237666 \times 10^3$  |
| 18  | 18     | $3.31623337 \times 10^0$    | 16  | 52     | $-1.80237666 \times 10^1$ |

## A. EQUATIONS OF MOTION

|    |    |                           |    |    |                           |
|----|----|---------------------------|----|----|---------------------------|
| 52 | 18 | $-7.73117173 \times 10^0$ | 18 | 52 | $-7.73117173 \times 10^0$ |
| 54 | 18 | $-3.31623337 \times 10^0$ | 52 | 52 | $1.80237666 \times 10^1$  |
| 1  | 31 | $-2.16096323 \times 10^2$ | 54 | 52 | $7.73117173 \times 10^0$  |
| 3  | 31 | $-1.57188566 \times 10^3$ | 16 | 54 | $-7.73117173 \times 10^0$ |
| 5  | 31 | $-3.03616953 \times 10^2$ | 18 | 54 | $-3.31623337 \times 10^0$ |
| 31 | 31 | $2.16096323 \times 10^2$  | 52 | 54 | $7.73117173 \times 10^0$  |
| 33 | 31 | $1.57188566 \times 10^3$  | 54 | 54 | $3.31623337 \times 10^0$  |
| 35 | 31 | $7.71558003 \times 10^1$  | –  | –  | –                         |

The stiffness matrix is

| Row | Column | Value                       | Row | Column | Value                     |
|-----|--------|-----------------------------|-----|--------|---------------------------|
| 1   | 1      | $-5.27876227 \times 10^3$   | 15  | 49     | $1.12501476 \times 10^4$  |
| 3   | 1      | $8.77766307 \times 10^3$    | 17  | 49     | $-5.41251476 \times 10^2$ |
| 5   | 1      | $1.98354865 \times 10^3$    | 23  | 49     | $-1.02906856 \times 10^3$ |
| 31  | 1      | $5.27876227 \times 10^3$    | 49  | 49     | $-1.22759422 \times 10^3$ |
| 33  | 1      | $-8.77766307 \times 10^3$   | 51  | 49     | $-1.12501476 \times 10^4$ |
| 35  | 1      | $-3.95396481 \times 10^2$   | 53  | 49     | $3.92400000 \times 10^1$  |
| 2   | 2      | $-6.48547899 \times 10^3$   | 14  | 50     | $6.05326828 \times 10^3$  |
| 4   | 2      | $-2.88102620 \times 10^2$   | 16  | 50     | $3.38983024 \times 10^2$  |
| 6   | 2      | $1.51500789 \times 10^3$    | 18  | 50     | $2.54237268 \times 10^2$  |
| 32  | 2      | $6.48547899 \times 10^3$    | 22  | 50     | $1.02906856 \times 10^3$  |
| 34  | 2      | $-3.54539518 \times 10^1$   | 50  | 50     | $-6.05326828 \times 10^3$ |
| 36  | 2      | $-3.13464818 \times 10^2$   | 52  | 50     | $-3.92400000 \times 10^1$ |
| 1   | 3      | $8.77766307 \times 10^3$    | 54  | 50     | $4.24580208 \times 10^2$  |
| 3   | 3      | $5.73632833 \times 10^4$    | 13  | 51     | $1.12501476 \times 10^4$  |
| 5   | 3      | $1.08176745 \times 10^4$    | 15  | 51     | $-2.01743259 \times 10^4$ |
| 31  | 3      | $-8.77766307 \times 10^3$   | 17  | 51     | $2.17313424 \times 10^2$  |
| 33  | 3      | $-5.73632833 \times 10^4$   | 49  | 51     | $-1.12501476 \times 10^4$ |
| 35  | 3      | $-2.82054325 \times 10^3$   | 51  | 51     | $2.01743259 \times 10^4$  |
| 2   | 4      | $1.06361855 \times 10^2$    | 53  | 51     | $-4.24580208 \times 10^2$ |
| 4   | 4      | $2.43481740 \times 10^1$    | 16  | 52     | $-2.01743259 \times 10^2$ |
| 6   | 4      | $-2.61021306 \times 10^1$   | 18  | 52     | $-1.12501476 \times 10^2$ |
| 32  | 4      | $-1.06361855 \times 10^2$   | 52  | 52     | $2.01743259 \times 10^2$  |
| 34  | 4      | $5.81444810 \times 10^{-1}$ | 54  | 52     | $1.12501476 \times 10^2$  |
| 36  | 4      | $5.14082301 \times 10^0$    | 16  | 54     | $-1.12501476 \times 10^2$ |
| 1   | 5      | $1.58908418 \times 10^3$    | 18  | 54     | $1.22759422 \times 10^1$  |
| 3   | 5      | $1.10946045 \times 10^4$    | 52  | 54     | $1.12501476 \times 10^2$  |
| 5   | 5      | $2.12419103 \times 10^3$    | 54  | 54     | $-1.22759422 \times 10^1$ |
| 31  | 5      | $-1.58908418 \times 10^3$   | 53  | 55     | $-1.96200000 \times 10^1$ |
| 33  | 5      | $-1.10946045 \times 10^4$   | 54  | 55     | $-1.25430694 \times 10^2$ |
| 35  | 5      | $-5.44926209 \times 10^2$   | 59  | 55     | $1.96200000 \times 10^1$  |
| 2   | 6      | $1.23807794 \times 10^3$    | 60  | 55     | $1.25430694 \times 10^2$  |
| 4   | 6      | $3.78001358 \times 10^2$    | 52  | 56     | $1.96200000 \times 10^1$  |
| 6   | 6      | $-2.82271523 \times 10^2$   | 54  | 56     | $-2.12290104 \times 10^2$ |
| 32  | 6      | $-1.23807794 \times 10^3$   | 58  | 56     | $-1.96200000 \times 10^1$ |
| 34  | 6      | $6.76815940 \times 10^0$    | 60  | 56     | $2.12290104 \times 10^2$  |
| 36  | 6      | $5.98404337 \times 10^1$    | 52  | 57     | $1.25430694 \times 10^2$  |
| 5   | 7      | $-3.30400800 \times 10^2$   | 53  | 57     | $2.12290104 \times 10^2$  |
| 4   | 8      | $3.30400800 \times 10^2$    | 58  | 57     | $-1.25430694 \times 10^2$ |
| 4   | 10     | $9.78647170 \times 10^1$    | 59  | 57     | $-2.12290104 \times 10^2$ |
| 10  | 10     | $-9.78647170 \times 10^1$   | 52  | 58     | $-5.26758365 \times 10^0$ |
| 12  | 10     | $1.68504408 \times 10^1$    | 54  | 58     | $5.69957127 \times 10^1$  |
| 5   | 11     | $9.78647170 \times 10^1$    | 58  | 58     | $5.26758365 \times 10^0$  |
| 11  | 11     | $-9.78647170 \times 10^1$   | 59  | 58     | $4.53314756 \times 10^0$  |



# A. EQUATIONS OF MOTION

|    |    |                           |    |    |                           |
|----|----|---------------------------|----|----|---------------------------|
| 4  | 12 | $-1.68504408 \times 10^1$ | 60 | 58 | $1.34797648 \times 10^1$  |
| 5  | 13 | $8.91826662 \times 10^2$  | 52 | 59 | $1.67900704 \times 10^1$  |
| 13 | 13 | $-1.22759422 \times 10^3$ | 53 | 59 | $2.31494304 \times 10^1$  |
| 15 | 13 | $-1.12501476 \times 10^4$ | 54 | 59 | $-3.36756713 \times 10^1$ |
| 17 | 13 | $5.41251476 \times 10^2$  | 58 | 59 | $-2.13232179 \times 10^1$ |
| 49 | 13 | $1.22759422 \times 10^3$  | 59 | 59 | $-2.31494304 \times 10^1$ |
| 51 | 13 | $1.12501476 \times 10^4$  | 60 | 59 | $-7.87110886 \times 10^0$ |
| 4  | 14 | $-8.91826662 \times 10^2$ | 52 | 60 | $-2.62632033 \times 10^0$ |
| 6  | 14 | $-4.24580208 \times 10^2$ | 54 | 60 | $2.84170141 \times 10^1$  |
| 14 | 14 | $-6.05326828 \times 10^3$ | 58 | 60 | $-6.78491572 \times 10^1$ |
| 16 | 14 | $-3.38983024 \times 10^2$ | 59 | 60 | $4.15467802 \times 10^1$  |
| 18 | 14 | $-2.54237268 \times 10^2$ | 60 | 60 | $-2.84170141 \times 10^1$ |
| 50 | 14 | $6.05326828 \times 10^3$  | 53 | 61 | $-1.96200000 \times 10^1$ |
| 5  | 15 | $4.24580208 \times 10^2$  | 54 | 61 | $1.25430694 \times 10^2$  |
| 13 | 15 | $-1.12501476 \times 10^4$ | 65 | 61 | $1.96200000 \times 10^1$  |
| 15 | 15 | $2.01743259 \times 10^4$  | 66 | 61 | $-1.25430694 \times 10^2$ |
| 17 | 15 | $-2.17313424 \times 10^2$ | 52 | 62 | $1.96200000 \times 10^1$  |
| 49 | 15 | $1.12501476 \times 10^4$  | 54 | 62 | $-2.12290104 \times 10^2$ |
| 51 | 15 | $-2.01743259 \times 10^4$ | 64 | 62 | $-1.96200000 \times 10^1$ |
| 4  | 16 | $-1.87283599 \times 10^1$ | 66 | 62 | $2.12290104 \times 10^2$  |
| 6  | 16 | $-8.91618438 \times 10^0$ | 52 | 63 | $-1.25430694 \times 10^2$ |
| 14 | 16 | $-3.38983024 \times 10^2$ | 53 | 63 | $2.12290104 \times 10^2$  |
| 16 | 16 | $1.53001654 \times 10^2$  | 64 | 63 | $1.25430694 \times 10^2$  |
| 18 | 16 | $6.78094421 \times 10^1$  | 65 | 63 | $-2.12290104 \times 10^2$ |
| 50 | 16 | $3.38983024 \times 10^2$  | 52 | 64 | $-5.26758365 \times 10^0$ |
| 52 | 16 | $-2.01743259 \times 10^2$ | 54 | 64 | $5.69957127 \times 10^1$  |
| 54 | 16 | $-1.12501476 \times 10^2$ | 64 | 64 | $5.26758365 \times 10^0$  |
| 5  | 17 | $-2.25495818 \times 10^1$ | 65 | 64 | $-4.53314756 \times 10^0$ |
| 13 | 17 | $5.41251476 \times 10^2$  | 66 | 64 | $1.34797648 \times 10^1$  |
| 15 | 17 | $-2.17313424 \times 10^2$ | 52 | 65 | $-1.67900704 \times 10^1$ |
| 17 | 17 | $-7.18961053 \times 10^1$ | 53 | 65 | $2.31494304 \times 10^1$  |
| 49 | 17 | $-5.41251476 \times 10^2$ | 54 | 65 | $3.36756713 \times 10^1$  |
| 51 | 17 | $2.17313424 \times 10^2$  | 64 | 65 | $2.13232179 \times 10^1$  |
| 4  | 18 | $-8.02643996 \times 10^0$ | 65 | 65 | $-2.31494304 \times 10^1$ |
| 6  | 18 | $-3.82122188 \times 10^0$ | 66 | 65 | $7.87110885 \times 10^0$  |
| 14 | 18 | $-2.54237268 \times 10^2$ | 52 | 66 | $-2.62632033 \times 10^0$ |
| 16 | 18 | $6.78094421 \times 10^1$  | 54 | 66 | $2.84170141 \times 10^1$  |
| 18 | 18 | $-4.39085382 \times 10^1$ | 64 | 66 | $-6.78491572 \times 10^1$ |
| 50 | 18 | $2.54237268 \times 10^2$  | 65 | 66 | $-4.15467802 \times 10^1$ |
| 52 | 18 | $-1.12501476 \times 10^2$ | 66 | 66 | $-2.84170141 \times 10^1$ |
| 54 | 18 | $1.22759422 \times 10^1$  | 5  | 73 | $-9.81000000 \times 10^0$ |
| 23 | 19 | $1.02906856 \times 10^3$  | 6  | 73 | $1.01288613 \times 10^2$  |
| 41 | 19 | $-1.10019106 \times 10^3$ | 59 | 73 | $-9.81000000 \times 10^0$ |
| 22 | 20 | $-1.02906856 \times 10^3$ | 60 | 73 | $-1.01288613 \times 10^2$ |
| 40 | 20 | $1.10019106 \times 10^3$  | 4  | 74 | $9.81000000 \times 10^0$  |
| 22 | 22 | $-4.62080246 \times 10^1$ | 6  | 74 | $1.80100664 \times 10^2$  |
| 24 | 22 | $-1.40950955 \times 10^2$ | 58 | 74 | $9.81000000 \times 10^0$  |
| 40 | 22 | $4.62080246 \times 10^1$  | 60 | 74 | $-1.80100664 \times 10^2$ |
| 23 | 23 | $-4.62080246 \times 10^1$ | 4  | 75 | $-1.01288613 \times 10^2$ |
| 41 | 23 | $4.62080246 \times 10^1$  | 5  | 75 | $-1.80100664 \times 10^2$ |
| 22 | 24 | $9.14423573 \times 10^1$  | 58 | 75 | $1.01288613 \times 10^2$  |
| 40 | 24 | $4.95085978 \times 10^1$  | 59 | 75 | $1.80100664 \times 10^2$  |
| 5  | 25 | $-1.25527100 \times 10^3$ | 4  | 76 | $-5.69647162 \times 10^0$ |
| 25 | 25 | $9.61195795 \times 10^3$  | 5  | 76 | $-1.01288613 \times 10^1$ |
| 27 | 25 | $9.59627775 \times 10^3$  | 58 | 76 | $-5.69647162 \times 10^0$ |
| 29 | 25 | $-2.04170061 \times 10^3$ | 59 | 76 | $-1.01288613 \times 10^1$ |
| 31 | 25 | $-9.61195795 \times 10^3$ | 76 | 76 | $1.13929432 \times 10^1$  |
| 33 | 25 | $-9.59627775 \times 10^3$ | 77 | 76 | $2.02577227 \times 10^1$  |
| 35 | 25 | $2.16238216 \times 10^2$  | 4  | 77 | $-1.01288613 \times 10^1$ |

## A. EQUATIONS OF MOTION

|    |    |                           |    |    |                              |
|----|----|---------------------------|----|----|------------------------------|
| 47 | 25 | $-1.17621944 \times 10^3$ | 5  | 77 | $-1.80100664 \times 10^1$    |
| 4  | 26 | $1.25527100 \times 10^3$  | 58 | 77 | $-1.01288613 \times 10^1$    |
| 6  | 26 | $2.34917193 \times 10^3$  | 59 | 77 | $-1.80100664 \times 10^1$    |
| 26 | 26 | $1.91925811 \times 10^4$  | 76 | 77 | $2.02577227 \times 10^1$     |
| 28 | 26 | $7.00529210 \times 10^2$  | 77 | 77 | $3.60201328 \times 10^1$     |
| 30 | 26 | $3.38173279 \times 10^3$  | 4  | 78 | $-9.81000000 \times 10^{-1}$ |
| 32 | 26 | $-1.91925811 \times 10^4$ | 5  | 78 | $5.51714400 \times 10^{-1}$  |
| 34 | 26 | $-3.94087665 \times 10^2$ | 6  | 78 | $-2.37065380 \times 10^1$    |
| 36 | 26 | $-3.77454095 \times 10^1$ | 58 | 78 | $9.81000000 \times 10^{-1}$  |
| 46 | 26 | $1.17621944 \times 10^3$  | 59 | 78 | $-5.51714400 \times 10^{-1}$ |
| 5  | 27 | $-2.34917193 \times 10^3$ | 60 | 78 | $-2.37065380 \times 10^1$    |
| 25 | 27 | $9.59627775 \times 10^3$  | 78 | 78 | $4.74130760 \times 10^1$     |
| 27 | 27 | $9.58062314 \times 10^3$  | 5  | 79 | $-9.81000000 \times 10^0$    |
| 29 | 27 | $-2.03836994 \times 10^3$ | 6  | 79 | $2.41420802 \times 10^1$     |
| 31 | 27 | $-9.59627775 \times 10^3$ | 59 | 79 | $-9.81000000 \times 10^0$    |
| 33 | 27 | $-9.58062314 \times 10^3$ | 60 | 79 | $-2.41420802 \times 10^1$    |
| 35 | 27 | $2.15885462 \times 10^2$  | 4  | 80 | $9.81000000 \times 10^0$     |
| 4  | 28 | $-6.21359147 \times 10^1$ | 6  | 80 | $3.21894403 \times 10^1$     |
| 6  | 28 | $-1.16284010 \times 10^2$ | 58 | 80 | $9.81000000 \times 10^0$     |
| 26 | 28 | $7.00529210 \times 10^2$  | 60 | 80 | $-3.21894403 \times 10^1$    |
| 28 | 28 | $1.56770174 \times 10^2$  | 4  | 81 | $-2.41420802 \times 10^1$    |
| 30 | 28 | $3.25462032 \times 10^2$  | 5  | 81 | $-3.21894403 \times 10^1$    |
| 32 | 28 | $-7.00529210 \times 10^2$ | 58 | 81 | $2.41420802 \times 10^1$     |
| 34 | 28 | $-1.43841998 \times 10^1$ | 59 | 81 | $3.21894403 \times 10^1$     |
| 36 | 28 | $-1.37770745 \times 10^0$ | 4  | 82 | $-1.81065602 \times 10^0$    |
| 46 | 28 | $1.68199380 \times 10^1$  | 5  | 82 | $-2.41420802 \times 10^0$    |
| 5  | 29 | $7.67121775 \times 10^2$  | 58 | 82 | $-1.81065602 \times 10^0$    |
| 25 | 29 | $-2.04170061 \times 10^3$ | 59 | 82 | $-2.41420802 \times 10^0$    |
| 27 | 29 | $-2.03836994 \times 10^3$ | 82 | 82 | $3.62131203 \times 10^0$     |
| 29 | 29 | $1.49550116 \times 10^2$  | 83 | 82 | $4.82841604 \times 10^0$     |
| 31 | 29 | $2.04170061 \times 10^3$  | 4  | 83 | $-2.41420802 \times 10^0$    |
| 33 | 29 | $2.03836994 \times 10^3$  | 5  | 83 | $-3.21894403 \times 10^0$    |
| 35 | 29 | $-4.59317133 \times 10^1$ | 58 | 83 | $-2.41420802 \times 10^0$    |
| 47 | 29 | $1.68199380 \times 10^1$  | 59 | 83 | $-3.21894403 \times 10^0$    |
| 4  | 30 | $4.43110664 \times 10^2$  | 82 | 83 | $4.82841604 \times 10^0$     |
| 6  | 30 | $8.29257690 \times 10^2$  | 83 | 83 | $6.43788805 \times 10^0$     |
| 26 | 30 | $3.38173279 \times 10^3$  | 4  | 84 | $-9.81000000 \times 10^{-1}$ |
| 28 | 30 | $3.25462032 \times 10^2$  | 5  | 84 | $7.35750000 \times 10^{-1}$  |
| 30 | 30 | $1.80527721 \times 10^2$  | 6  | 84 | $-5.02960004 \times 10^0$    |
| 32 | 30 | $-3.38173279 \times 10^3$ | 58 | 84 | $9.81000000 \times 10^{-1}$  |
| 34 | 30 | $-6.94382466 \times 10^1$ | 59 | 84 | $-7.35750000 \times 10^{-1}$ |
| 36 | 30 | $-6.65074115 \times 10^0$ | 60 | 84 | $-5.02960004 \times 10^0$    |
| 46 | 30 | $-2.30539010 \times 10^2$ | 84 | 84 | $1.00592001 \times 10^1$     |
| 1  | 31 | $5.27876227 \times 10^3$  | 5  | 85 | $-9.81000000 \times 10^0$    |
| 3  | 31 | $-8.77766307 \times 10^3$ | 6  | 85 | $-1.01288613 \times 10^2$    |
| 5  | 31 | $-1.25046351 \times 10^3$ | 65 | 85 | $-9.81000000 \times 10^0$    |
| 25 | 31 | $-9.61195795 \times 10^3$ | 66 | 85 | $1.01288613 \times 10^2$     |
| 27 | 31 | $-9.59627775 \times 10^3$ | 4  | 86 | $9.81000000 \times 10^0$     |
| 29 | 31 | $2.04170061 \times 10^3$  | 6  | 86 | $1.80100664 \times 10^2$     |
| 31 | 31 | $4.33319567 \times 10^3$  | 64 | 86 | $9.81000000 \times 10^0$     |
| 33 | 31 | $1.83739408 \times 10^4$  | 66 | 86 | $-1.80100664 \times 10^2$    |
| 35 | 31 | $1.79158265 \times 10^2$  | 4  | 87 | $1.01288613 \times 10^2$     |
| 2  | 32 | $6.48547899 \times 10^3$  | 5  | 87 | $-1.80100664 \times 10^2$    |
| 4  | 32 | $-4.44982522 \times 10^2$ | 64 | 87 | $-1.01288613 \times 10^2$    |
| 6  | 32 | $-3.86417982 \times 10^3$ | 65 | 87 | $1.80100664 \times 10^2$     |
| 26 | 32 | $-1.91925811 \times 10^4$ | 4  | 88 | $-5.69647162 \times 10^0$    |
| 28 | 32 | $-7.00529210 \times 10^2$ | 5  | 88 | $1.01288613 \times 10^1$     |
| 30 | 32 | $-3.38173279 \times 10^3$ | 64 | 88 | $-5.69647162 \times 10^0$    |
| 32 | 32 | $1.27071021 \times 10^4$  | 65 | 88 | $1.01288613 \times 10^1$     |

## A. EQUATIONS OF MOTION

|    |    |                           |    |    |                              |
|----|----|---------------------------|----|----|------------------------------|
| 34 | 32 | $4.29541617 \times 10^2$  | 88 | 88 | $1.13929432 \times 10^1$     |
| 36 | 32 | $3.51210227 \times 10^2$  | 89 | 88 | $-2.02577227 \times 10^1$    |
| 1  | 33 | $-8.77766307 \times 10^3$ | 4  | 89 | $1.01288613 \times 10^1$     |
| 3  | 33 | $-5.73632833 \times 10^4$ | 5  | 89 | $-1.80100664 \times 10^1$    |
| 5  | 33 | $-8.46850257 \times 10^3$ | 64 | 89 | $1.01288613 \times 10^1$     |
| 25 | 33 | $-9.59627775 \times 10^3$ | 65 | 89 | $-1.80100664 \times 10^1$    |
| 27 | 33 | $-9.58062314 \times 10^3$ | 88 | 89 | $-2.02577227 \times 10^1$    |
| 29 | 33 | $2.03836994 \times 10^3$  | 89 | 89 | $3.60201328 \times 10^1$     |
| 31 | 33 | $1.83739408 \times 10^4$  | 4  | 90 | $-9.81000000 \times 10^{-1}$ |
| 33 | 33 | $6.69439064 \times 10^4$  | 5  | 90 | $-5.51714400 \times 10^{-1}$ |
| 35 | 33 | $2.60465779 \times 10^3$  | 6  | 90 | $-2.37065380 \times 10^1$    |
| 2  | 34 | $-3.54539518 \times 10^1$ | 64 | 90 | $9.81000000 \times 10^{-1}$  |
| 4  | 34 | $5.68332952 \times 10^0$  | 65 | 90 | $5.51714400 \times 10^{-1}$  |
| 6  | 34 | $4.63347610 \times 10^1$  | 66 | 90 | $-2.37065380 \times 10^1$    |
| 26 | 34 | $-3.94087665 \times 10^2$ | 90 | 90 | $4.74130760 \times 10^1$     |
| 28 | 34 | $-1.43841998 \times 10^1$ | 5  | 91 | $-9.81000000 \times 10^0$    |
| 30 | 34 | $-6.94382466 \times 10^1$ | 6  | 91 | $-2.41420802 \times 10^1$    |
| 32 | 34 | $4.29541617 \times 10^2$  | 65 | 91 | $-9.81000000 \times 10^0$    |
| 34 | 34 | $-5.65309114 \times 10^1$ | 66 | 91 | $2.41420802 \times 10^1$     |
| 36 | 34 | $-8.72276167 \times 10^1$ | 4  | 92 | $9.81000000 \times 10^0$     |
| 1  | 35 | $-3.95396481 \times 10^2$ | 6  | 92 | $3.21894403 \times 10^1$     |
| 3  | 35 | $-2.82054325 \times 10^3$ | 64 | 92 | $9.81000000 \times 10^0$     |
| 5  | 35 | $-6.61587914 \times 10^2$ | 66 | 92 | $-3.21894403 \times 10^1$    |
| 25 | 35 | $2.16238216 \times 10^2$  | 4  | 93 | $2.41420802 \times 10^1$     |
| 27 | 35 | $2.15885462 \times 10^2$  | 5  | 93 | $-3.21894403 \times 10^1$    |
| 29 | 35 | $-4.59317133 \times 10^1$ | 64 | 93 | $-2.41420802 \times 10^1$    |
| 31 | 35 | $1.79158265 \times 10^2$  | 65 | 93 | $3.21894403 \times 10^1$     |
| 33 | 35 | $2.60465779 \times 10^3$  | 4  | 94 | $-1.81065602 \times 10^0$    |
| 35 | 35 | $2.09451894 \times 10^2$  | 5  | 94 | $2.41420802 \times 10^0$     |
| 2  | 36 | $-3.13464818 \times 10^2$ | 64 | 94 | $-1.81065602 \times 10^0$    |
| 4  | 36 | $-1.05598886 \times 10^1$ | 65 | 94 | $2.41420802 \times 10^0$     |
| 6  | 36 | $-6.19231567 \times 10^1$ | 94 | 94 | $3.62131203 \times 10^0$     |
| 26 | 36 | $-3.77454095 \times 10^1$ | 95 | 94 | $-4.82841605 \times 10^0$    |
| 28 | 36 | $-1.37770745 \times 10^0$ | 4  | 95 | $2.41420802 \times 10^0$     |
| 30 | 36 | $-6.65074115 \times 10^0$ | 5  | 95 | $-3.21894403 \times 10^0$    |
| 32 | 36 | $3.51210227 \times 10^2$  | 64 | 95 | $2.41420802 \times 10^0$     |
| 34 | 36 | $-8.72276167 \times 10^1$ | 65 | 95 | $-3.21894403 \times 10^0$    |
| 36 | 36 | $1.15451933 \times 10^2$  | 94 | 95 | $-4.82841605 \times 10^0$    |
| 41 | 37 | $1.10019106 \times 10^3$  | 95 | 95 | $6.43788806 \times 10^0$     |
| 40 | 38 | $-1.10019106 \times 10^3$ | 4  | 96 | $-9.81000000 \times 10^{-1}$ |
| 39 | 39 | $1.30000000 \times 10^5$  | 5  | 96 | $-7.35750000 \times 10^{-1}$ |
| 40 | 40 | $-3.43174277 \times 10^2$ | 6  | 96 | $-5.02960005 \times 10^0$    |
| 47 | 43 | $1.17621944 \times 10^3$  | 64 | 96 | $9.81000000 \times 10^{-1}$  |
| 46 | 44 | $-1.17621944 \times 10^3$ | 65 | 96 | $7.35750000 \times 10^{-1}$  |
| 45 | 45 | $1.41000000 \times 10^5$  | 66 | 96 | $-5.02960005 \times 10^0$    |
| 46 | 46 | $-3.92166652 \times 10^2$ | 96 | 96 | $1.00592001 \times 10^1$     |
| 13 | 49 | $1.22759422 \times 10^3$  | -  | -  | -                            |

The velocity matrix is

| Row | Column | Value                     | Row | Column | Value                     |
|-----|--------|---------------------------|-----|--------|---------------------------|
| 3   | 5      | $1.00000000 \times 10^1$  | 51  | 53     | $1.00000000 \times 10^1$  |
| 2   | 6      | $-1.00000000 \times 10^1$ | 50  | 54     | $-1.00000000 \times 10^1$ |
| 9   | 11     | $1.00000000 \times 10^1$  | 57  | 59     | $1.00000000 \times 10^1$  |
| 8   | 12     | $-1.00000000 \times 10^1$ | 56  | 60     | $-1.00000000 \times 10^1$ |

## A. EQUATIONS OF MOTION

|    |    |                           |    |    |                           |
|----|----|---------------------------|----|----|---------------------------|
| 15 | 17 | $1.00000000 \times 10^1$  | 63 | 65 | $1.00000000 \times 10^1$  |
| 14 | 18 | $-1.00000000 \times 10^1$ | 62 | 66 | $-1.00000000 \times 10^1$ |
| 21 | 23 | $1.00000000 \times 10^1$  | 69 | 71 | $1.00000000 \times 10^1$  |
| 20 | 24 | $-1.00000000 \times 10^1$ | 68 | 72 | $-1.00000000 \times 10^1$ |
| 27 | 29 | $1.00000000 \times 10^1$  | 75 | 77 | $1.00000000 \times 10^1$  |
| 26 | 30 | $-1.00000000 \times 10^1$ | 74 | 78 | $-1.00000000 \times 10^1$ |
| 33 | 35 | $1.00000000 \times 10^1$  | 81 | 83 | $1.00000000 \times 10^1$  |
| 32 | 36 | $-1.00000000 \times 10^1$ | 80 | 84 | $-1.00000000 \times 10^1$ |
| 39 | 41 | $1.00000000 \times 10^1$  | 87 | 89 | $1.00000000 \times 10^1$  |
| 38 | 42 | $-1.00000000 \times 10^1$ | 86 | 90 | $-1.00000000 \times 10^1$ |
| 45 | 47 | $1.00000000 \times 10^1$  | 93 | 95 | $1.00000000 \times 10^1$  |
| 44 | 48 | $-1.00000000 \times 10^1$ | 92 | 96 | $-1.00000000 \times 10^1$ |

The input force matrix is

| Row | Column | Value                        | Row | Column | Value                        |
|-----|--------|------------------------------|-----|--------|------------------------------|
| 4   | 1      | $-4.06755809 \times 10^{-1}$ | 16  | 1      | $4.06755809 \times 10^{-1}$  |
| 6   | 1      | $9.13536924 \times 10^{-1}$  | 18  | 1      | $-9.13536924 \times 10^{-1}$ |

The input force rate matrix is

| Row | Column | Value                    | Row | Column | Value |
|-----|--------|--------------------------|-----|--------|-------|
| 1   | 1      | $0.00000000 \times 10^0$ | –   | –      | –     |

The system is subject to constraints

$$\begin{bmatrix} \mathbf{J}_h & \mathbf{0} & \mathbf{0} \\ -\mathbf{J}_h \mathbf{V} & \mathbf{J}_h & \mathbf{0} \\ \mathbf{0} & \mathbf{J}_{nh} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \dot{\mathbf{p}} & \mathbf{p} \\ \dot{\mathbf{w}} & \mathbf{w} \\ \dot{\mathbf{u}} & \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix}$$

| Row | Column | Value                     | Row | Column | Value                        |
|-----|--------|---------------------------|-----|--------|------------------------------|
| 7   | 1      | $-1.00000000 \times 10^0$ | 142 | 84     | $1.00000000 \times 10^1$     |
| 12  | 1      | $-1.00000000 \times 10^0$ | 59  | 85     | $1.00000000 \times 10^0$     |
| 17  | 1      | $-1.00000000 \times 10^0$ | 63  | 85     | $1.00000000 \times 10^0$     |
| 23  | 1      | $-1.00000000 \times 10^0$ | 60  | 86     | $1.00000000 \times 10^0$     |
| 45  | 1      | $-1.00000000 \times 10^0$ | 64  | 86     | $1.00000000 \times 10^0$     |
| 52  | 1      | $-1.00000000 \times 10^0$ | 61  | 87     | $1.00000000 \times 10^0$     |
| 59  | 1      | $-1.00000000 \times 10^0$ | 65  | 87     | $1.00000000 \times 10^0$     |
| 66  | 1      | $-1.00000000 \times 10^0$ | 61  | 88     | $-5.62400000 \times 10^{-2}$ |
| 8   | 2      | $-1.00000000 \times 10^0$ | 62  | 88     | $1.00000000 \times 10^0$     |
| 13  | 2      | $-1.00000000 \times 10^0$ | 65  | 88     | $5.62400000 \times 10^{-2}$  |
| 18  | 2      | $-1.00000000 \times 10^0$ | 61  | 89     | $1.00000000 \times 10^{-1}$  |
| 24  | 2      | $-1.00000000 \times 10^0$ | 65  | 89     | $-1.00000000 \times 10^{-1}$ |
| 46  | 2      | $-1.00000000 \times 10^0$ | 146 | 89     | $-1.00000000 \times 10^1$    |
| 53  | 2      | $-1.00000000 \times 10^0$ | 150 | 89     | $-1.00000000 \times 10^1$    |
| 60  | 2      | $-1.00000000 \times 10^0$ | 59  | 90     | $5.62400000 \times 10^{-2}$  |

## A. EQUATIONS OF MOTION

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|     |   |                              |     |     |                              |
|-----|---|------------------------------|-----|-----|------------------------------|
| 67  | 2 | $-1.00000000 \times 10^0$    | 60  | 90  | $-1.00000000 \times 10^{-1}$ |
| 9   | 3 | $-1.00000000 \times 10^0$    | 63  | 90  | $-5.62400000 \times 10^{-2}$ |
| 14  | 3 | $-1.00000000 \times 10^0$    | 64  | 90  | $1.00000000 \times 10^{-1}$  |
| 19  | 3 | $-1.00000000 \times 10^0$    | 145 | 90  | $1.00000000 \times 10^1$     |
| 25  | 3 | $-1.00000000 \times 10^0$    | 149 | 90  | $1.00000000 \times 10^1$     |
| 47  | 3 | $-1.00000000 \times 10^0$    | 66  | 91  | $1.00000000 \times 10^0$     |
| 54  | 3 | $-1.00000000 \times 10^0$    | 70  | 91  | $1.00000000 \times 10^0$     |
| 61  | 3 | $-1.00000000 \times 10^0$    | 67  | 92  | $1.00000000 \times 10^0$     |
| 68  | 3 | $-1.00000000 \times 10^0$    | 71  | 92  | $1.00000000 \times 10^0$     |
| 8   | 4 | $-1.11600000 \times 10^{-1}$ | 68  | 93  | $1.00000000 \times 10^0$     |
| 10  | 4 | $1.00000000 \times 10^0$     | 72  | 93  | $1.00000000 \times 10^0$     |
| 13  | 4 | $-2.84600000 \times 10^{-1}$ | 68  | 94  | $-7.50000000 \times 10^{-2}$ |
| 15  | 4 | $1.00000000 \times 10^0$     | 69  | 94  | $1.00000000 \times 10^0$     |
| 18  | 4 | $3.71400000 \times 10^{-1}$  | 72  | 94  | $7.50000000 \times 10^{-2}$  |
| 20  | 4 | $-1.00000000 \times 10^0$    | 68  | 95  | $1.00000000 \times 10^{-1}$  |
| 24  | 4 | $2.76600000 \times 10^{-1}$  | 72  | 95  | $-1.00000000 \times 10^{-1}$ |
| 27  | 4 | $-9.13536924 \times 10^{-1}$ | 153 | 95  | $-1.00000000 \times 10^1$    |
| 46  | 4 | $-2.72400000 \times 10^{-1}$ | 157 | 95  | $-1.00000000 \times 10^1$    |
| 47  | 4 | $-2.12480000 \times 10^{-1}$ | 66  | 96  | $7.50000000 \times 10^{-2}$  |
| 48  | 4 | $-1.00000000 \times 10^0$    | 67  | 96  | $-1.00000000 \times 10^{-1}$ |
| 53  | 4 | $-1.72400000 \times 10^{-1}$ | 70  | 96  | $-7.50000000 \times 10^{-2}$ |
| 54  | 4 | $-2.50000000 \times 10^{-1}$ | 71  | 96  | $1.00000000 \times 10^{-1}$  |
| 55  | 4 | $-1.00000000 \times 10^0$    | 152 | 96  | $1.00000000 \times 10^1$     |
| 60  | 4 | $-2.72400000 \times 10^{-1}$ | 156 | 96  | $1.00000000 \times 10^1$     |
| 61  | 4 | $2.12480000 \times 10^{-1}$  | 92  | 97  | $-1.00000000 \times 10^0$    |
| 62  | 4 | $-1.00000000 \times 10^0$    | 97  | 97  | $-1.00000000 \times 10^0$    |
| 67  | 4 | $-1.72400000 \times 10^{-1}$ | 102 | 97  | $-1.00000000 \times 10^0$    |
| 68  | 4 | $2.50000000 \times 10^{-1}$  | 108 | 97  | $-1.00000000 \times 10^0$    |
| 69  | 4 | $-1.00000000 \times 10^0$    | 130 | 97  | $-1.00000000 \times 10^0$    |
| 7   | 5 | $1.11600000 \times 10^{-1}$  | 137 | 97  | $-1.00000000 \times 10^0$    |
| 9   | 5 | $-1.28900000 \times 10^{-1}$ | 144 | 97  | $-1.00000000 \times 10^0$    |
| 12  | 5 | $2.84600000 \times 10^{-1}$  | 151 | 97  | $-1.00000000 \times 10^0$    |
| 14  | 5 | $-1.38900000 \times 10^{-1}$ | 93  | 98  | $-1.00000000 \times 10^0$    |
| 17  | 5 | $-3.71400000 \times 10^{-1}$ | 98  | 98  | $-1.00000000 \times 10^0$    |
| 19  | 5 | $-3.13900000 \times 10^{-1}$ | 103 | 98  | $-1.00000000 \times 10^0$    |
| 21  | 5 | $-1.00000000 \times 10^0$    | 109 | 98  | $-1.00000000 \times 10^0$    |
| 23  | 5 | $-2.76600000 \times 10^{-1}$ | 131 | 98  | $-1.00000000 \times 10^0$    |
| 25  | 5 | $4.95100000 \times 10^{-1}$  | 138 | 98  | $-1.00000000 \times 10^0$    |
| 26  | 5 | $-1.00000000 \times 10^0$    | 145 | 98  | $-1.00000000 \times 10^0$    |
| 45  | 5 | $2.72400000 \times 10^{-1}$  | 152 | 98  | $-1.00000000 \times 10^0$    |
| 47  | 5 | $3.62100000 \times 10^{-1}$  | 94  | 99  | $-1.00000000 \times 10^0$    |
| 52  | 5 | $1.72400000 \times 10^{-1}$  | 99  | 99  | $-1.00000000 \times 10^0$    |
| 54  | 5 | $3.62100000 \times 10^{-1}$  | 104 | 99  | $-1.00000000 \times 10^0$    |
| 59  | 5 | $2.72400000 \times 10^{-1}$  | 110 | 99  | $-1.00000000 \times 10^0$    |
| 61  | 5 | $3.62100000 \times 10^{-1}$  | 132 | 99  | $-1.00000000 \times 10^0$    |
| 66  | 5 | $1.72400000 \times 10^{-1}$  | 139 | 99  | $-1.00000000 \times 10^0$    |
| 68  | 5 | $3.62100000 \times 10^{-1}$  | 146 | 99  | $-1.00000000 \times 10^0$    |
| 94  | 5 | $1.00000000 \times 10^1$     | 153 | 99  | $-1.00000000 \times 10^0$    |
| 99  | 5 | $1.00000000 \times 10^1$     | 93  | 100 | $-1.11600000 \times 10^{-1}$ |
| 104 | 5 | $1.00000000 \times 10^1$     | 95  | 100 | $1.00000000 \times 10^0$     |
| 110 | 5 | $1.00000000 \times 10^1$     | 98  | 100 | $-2.84600000 \times 10^{-1}$ |
| 132 | 5 | $1.00000000 \times 10^1$     | 100 | 100 | $1.00000000 \times 10^0$     |
| 139 | 5 | $1.00000000 \times 10^1$     | 103 | 100 | $3.71400000 \times 10^{-1}$  |
| 146 | 5 | $1.00000000 \times 10^1$     | 105 | 100 | $-1.00000000 \times 10^0$    |
| 153 | 5 | $1.00000000 \times 10^1$     | 109 | 100 | $2.76600000 \times 10^{-1}$  |
| 8   | 6 | $1.28900000 \times 10^{-1}$  | 112 | 100 | $-9.13536924 \times 10^{-1}$ |
| 11  | 6 | $-1.00000000 \times 10^0$    | 131 | 100 | $-2.72400000 \times 10^{-1}$ |
| 13  | 6 | $1.38900000 \times 10^{-1}$  | 132 | 100 | $-2.12480000 \times 10^{-1}$ |
| 16  | 6 | $-1.00000000 \times 10^0$    | 133 | 100 | $-1.00000000 \times 10^0$    |

# A. EQUATIONS OF MOTION

|     |    |                              |     |     |                              |
|-----|----|------------------------------|-----|-----|------------------------------|
| 18  | 6  | $3.13900000 \times 10^{-1}$  | 138 | 100 | $-1.72400000 \times 10^{-1}$ |
| 22  | 6  | $-1.00000000 \times 10^0$    | 139 | 100 | $-2.50000000 \times 10^{-1}$ |
| 24  | 6  | $-4.95100000 \times 10^{-1}$ | 140 | 100 | $-1.00000000 \times 10^0$    |
| 27  | 6  | $-4.06755809 \times 10^{-1}$ | 145 | 100 | $-2.72400000 \times 10^{-1}$ |
| 45  | 6  | $2.12480000 \times 10^{-1}$  | 146 | 100 | $2.12480000 \times 10^{-1}$  |
| 46  | 6  | $-3.62100000 \times 10^{-1}$ | 147 | 100 | $-1.00000000 \times 10^0$    |
| 52  | 6  | $2.50000000 \times 10^{-1}$  | 152 | 100 | $-1.72400000 \times 10^{-1}$ |
| 53  | 6  | $-3.62100000 \times 10^{-1}$ | 153 | 100 | $2.50000000 \times 10^{-1}$  |
| 59  | 6  | $-2.12480000 \times 10^{-1}$ | 154 | 100 | $-1.00000000 \times 10^0$    |
| 60  | 6  | $-3.62100000 \times 10^{-1}$ | 92  | 101 | $1.11600000 \times 10^{-1}$  |
| 66  | 6  | $-2.50000000 \times 10^{-1}$ | 94  | 101 | $-1.28900000 \times 10^{-1}$ |
| 67  | 6  | $-3.62100000 \times 10^{-1}$ | 97  | 101 | $2.84600000 \times 10^{-1}$  |
| 93  | 6  | $-1.00000000 \times 10^1$    | 99  | 101 | $-1.38900000 \times 10^{-1}$ |
| 98  | 6  | $-1.00000000 \times 10^1$    | 102 | 101 | $-3.71400000 \times 10^{-1}$ |
| 103 | 6  | $-1.00000000 \times 10^1$    | 104 | 101 | $-3.13900000 \times 10^{-1}$ |
| 109 | 6  | $-1.00000000 \times 10^1$    | 106 | 101 | $-1.00000000 \times 10^0$    |
| 131 | 6  | $-1.00000000 \times 10^1$    | 108 | 101 | $-2.76600000 \times 10^{-1}$ |
| 138 | 6  | $-1.00000000 \times 10^1$    | 110 | 101 | $4.95100000 \times 10^{-1}$  |
| 145 | 6  | $-1.00000000 \times 10^1$    | 111 | 101 | $-1.00000000 \times 10^0$    |
| 152 | 6  | $-1.00000000 \times 10^1$    | 130 | 101 | $2.72400000 \times 10^{-1}$  |
| 17  | 7  | $1.00000000 \times 10^0$     | 132 | 101 | $3.62100000 \times 10^{-1}$  |
| 18  | 8  | $1.00000000 \times 10^0$     | 137 | 101 | $1.72400000 \times 10^{-1}$  |
| 19  | 9  | $1.00000000 \times 10^0$     | 139 | 101 | $3.62100000 \times 10^{-1}$  |
| 18  | 10 | $2.96200000 \times 10^{-1}$  | 144 | 101 | $2.72400000 \times 10^{-1}$  |
| 20  | 10 | $1.00000000 \times 10^0$     | 146 | 101 | $3.62100000 \times 10^{-1}$  |
| 17  | 11 | $-2.96200000 \times 10^{-1}$ | 151 | 101 | $1.72400000 \times 10^{-1}$  |
| 19  | 11 | $5.10000000 \times 10^{-2}$  | 153 | 101 | $3.62100000 \times 10^{-1}$  |
| 21  | 11 | $1.00000000 \times 10^0$     | 93  | 102 | $1.28900000 \times 10^{-1}$  |
| 104 | 11 | $-1.00000000 \times 10^1$    | 96  | 102 | $-1.00000000 \times 10^0$    |
| 18  | 12 | $-5.10000000 \times 10^{-2}$ | 98  | 102 | $1.38900000 \times 10^{-1}$  |
| 22  | 12 | $1.00000000 \times 10^0$     | 101 | 102 | $-1.00000000 \times 10^0$    |
| 103 | 12 | $1.00000000 \times 10^1$     | 103 | 102 | $3.13900000 \times 10^{-1}$  |
| 23  | 13 | $1.00000000 \times 10^0$     | 107 | 102 | $-1.00000000 \times 10^0$    |
| 73  | 13 | $-8.94427191 \times 10^{-1}$ | 109 | 102 | $-4.95100000 \times 10^{-1}$ |
| 24  | 14 | $1.00000000 \times 10^0$     | 112 | 102 | $-4.06755809 \times 10^{-1}$ |
| 74  | 14 | $-1.00000000 \times 10^0$    | 130 | 102 | $2.12480000 \times 10^{-1}$  |
| 25  | 15 | $1.00000000 \times 10^0$     | 131 | 102 | $-3.62100000 \times 10^{-1}$ |
| 73  | 15 | $-4.47213596 \times 10^{-1}$ | 137 | 102 | $2.50000000 \times 10^{-1}$  |
| 24  | 16 | $2.10000000 \times 10^{-2}$  | 138 | 102 | $-3.62100000 \times 10^{-1}$ |
| 27  | 16 | $9.13536924 \times 10^{-1}$  | 144 | 102 | $-2.12480000 \times 10^{-1}$ |
| 75  | 16 | $4.47213596 \times 10^{-1}$  | 145 | 102 | $-3.62100000 \times 10^{-1}$ |
| 23  | 17 | $-2.10000000 \times 10^{-2}$ | 151 | 102 | $-2.50000000 \times 10^{-1}$ |
| 25  | 17 | $-9.00000000 \times 10^{-3}$ | 152 | 102 | $-3.62100000 \times 10^{-1}$ |
| 26  | 17 | $1.00000000 \times 10^0$     | 102 | 103 | $1.00000000 \times 10^0$     |
| 110 | 17 | $-1.00000000 \times 10^1$    | 103 | 104 | $1.00000000 \times 10^0$     |
| 158 | 17 | $4.47213596 \times 10^0$     | 104 | 105 | $1.00000000 \times 10^0$     |
| 24  | 18 | $9.00000000 \times 10^{-3}$  | 103 | 106 | $2.96200000 \times 10^{-1}$  |
| 27  | 18 | $4.06755809 \times 10^{-1}$  | 105 | 106 | $1.00000000 \times 10^0$     |
| 75  | 18 | $-8.94427191 \times 10^{-1}$ | 102 | 107 | $-2.96200000 \times 10^{-1}$ |
| 109 | 18 | $1.00000000 \times 10^1$     | 104 | 107 | $5.10000000 \times 10^{-2}$  |
| 159 | 18 | $-1.00000000 \times 10^1$    | 106 | 107 | $1.00000000 \times 10^0$     |
| 28  | 19 | $1.00000000 \times 10^0$     | 103 | 108 | $-5.10000000 \times 10^{-2}$ |
| 80  | 19 | $-1.00000000 \times 10^0$    | 107 | 108 | $1.00000000 \times 10^0$     |
| 29  | 20 | $1.00000000 \times 10^0$     | 108 | 109 | $1.00000000 \times 10^0$     |
| 81  | 20 | $-1.00000000 \times 10^0$    | 158 | 109 | $-8.94427191 \times 10^{-1}$ |
| 30  | 21 | $1.00000000 \times 10^0$     | 109 | 110 | $1.00000000 \times 10^0$     |
| 82  | 21 | $-1.00000000 \times 10^0$    | 159 | 110 | $-1.00000000 \times 10^0$    |
| 29  | 22 | $4.20000000 \times 10^{-2}$  | 110 | 111 | $1.00000000 \times 10^0$     |
| 31  | 22 | $-1.00000000 \times 10^0$    | 158 | 111 | $-4.47213596 \times 10^{-1}$ |

# A. EQUATIONS OF MOTION

|     |    |                              |     |     |                              |
|-----|----|------------------------------|-----|-----|------------------------------|
| 81  | 22 | $2.26480308 \times 10^{-1}$  | 109 | 112 | $2.10000000 \times 10^{-2}$  |
| 83  | 22 | $-1.00000000 \times 10^0$    | 112 | 112 | $9.13536924 \times 10^{-1}$  |
| 28  | 23 | $-4.20000000 \times 10^{-2}$ | 160 | 112 | $4.47213596 \times 10^{-1}$  |
| 30  | 23 | $-4.50000000 \times 10^{-2}$ | 108 | 113 | $-2.10000000 \times 10^{-2}$ |
| 80  | 23 | $-2.26480308 \times 10^{-1}$ | 110 | 113 | $-9.00000000 \times 10^{-3}$ |
| 82  | 23 | $-8.88593439 \times 10^{-2}$ | 111 | 113 | $1.00000000 \times 10^0$     |
| 84  | 23 | $-1.00000000 \times 10^0$    | 109 | 114 | $9.00000000 \times 10^{-3}$  |
| 115 | 23 | $-1.00000000 \times 10^1$    | 112 | 114 | $4.06755809 \times 10^{-1}$  |
| 167 | 23 | $1.00000000 \times 10^1$     | 160 | 114 | $-8.94427191 \times 10^{-1}$ |
| 29  | 24 | $4.50000000 \times 10^{-2}$  | 113 | 115 | $1.00000000 \times 10^0$     |
| 32  | 24 | $1.00000000 \times 10^0$     | 165 | 115 | $-1.00000000 \times 10^0$    |
| 81  | 24 | $8.88593439 \times 10^{-2}$  | 114 | 116 | $1.00000000 \times 10^0$     |
| 85  | 24 | $-1.00000000 \times 10^0$    | 166 | 116 | $-1.00000000 \times 10^0$    |
| 114 | 24 | $1.00000000 \times 10^1$     | 115 | 117 | $1.00000000 \times 10^0$     |
| 166 | 24 | $-1.00000000 \times 10^1$    | 167 | 117 | $-1.00000000 \times 10^0$    |
| 1   | 25 | $7.06529316 \times 10^{-1}$  | 114 | 118 | $4.20000000 \times 10^{-2}$  |
| 2   | 25 | $1.00000000 \times 10^0$     | 116 | 118 | $-1.00000000 \times 10^0$    |
| 7   | 25 | $1.00000000 \times 10^0$     | 166 | 118 | $2.26480308 \times 10^{-1}$  |
| 3   | 26 | $1.00000000 \times 10^0$     | 168 | 118 | $-1.00000000 \times 10^0$    |
| 8   | 26 | $1.00000000 \times 10^0$     | 113 | 119 | $-4.20000000 \times 10^{-2}$ |
| 1   | 27 | $-7.07683775 \times 10^{-1}$ | 115 | 119 | $-4.50000000 \times 10^{-2}$ |
| 4   | 27 | $1.00000000 \times 10^0$     | 165 | 119 | $-2.26480308 \times 10^{-1}$ |
| 9   | 27 | $1.00000000 \times 10^0$     | 167 | 119 | $-8.88593439 \times 10^{-2}$ |
| 3   | 28 | $1.43000000 \times 10^{-2}$  | 169 | 119 | $-1.00000000 \times 10^0$    |
| 5   | 28 | $-1.00000000 \times 10^0$    | 114 | 120 | $4.50000000 \times 10^{-2}$  |
| 8   | 28 | $-4.95000000 \times 10^{-2}$ | 117 | 120 | $1.00000000 \times 10^0$     |
| 10  | 28 | $-1.00000000 \times 10^0$    | 166 | 120 | $8.88593439 \times 10^{-2}$  |
| 1   | 29 | $9.89055612 \times 10^{-2}$  | 170 | 120 | $-1.00000000 \times 10^0$    |
| 2   | 29 | $-1.43000000 \times 10^{-2}$ | 86  | 121 | $7.06529316 \times 10^{-1}$  |
| 4   | 29 | $1.96000000 \times 10^{-1}$  | 87  | 121 | $1.00000000 \times 10^0$     |
| 7   | 29 | $4.95000000 \times 10^{-2}$  | 92  | 121 | $1.00000000 \times 10^0$     |
| 9   | 29 | $-3.53000000 \times 10^{-1}$ | 88  | 122 | $1.00000000 \times 10^0$     |
| 86  | 29 | $7.07683775 \times 10^0$     | 93  | 122 | $1.00000000 \times 10^0$     |
| 89  | 29 | $-1.00000000 \times 10^1$    | 86  | 123 | $-7.07683775 \times 10^{-1}$ |
| 94  | 29 | $-1.00000000 \times 10^1$    | 89  | 123 | $1.00000000 \times 10^0$     |
| 3   | 30 | $-1.96000000 \times 10^{-1}$ | 94  | 123 | $1.00000000 \times 10^0$     |
| 6   | 30 | $1.00000000 \times 10^0$     | 88  | 124 | $1.43000000 \times 10^{-2}$  |
| 8   | 30 | $3.53000000 \times 10^{-1}$  | 90  | 124 | $-1.00000000 \times 10^0$    |
| 11  | 30 | $1.00000000 \times 10^0$     | 93  | 124 | $-4.95000000 \times 10^{-2}$ |
| 88  | 30 | $1.00000000 \times 10^1$     | 95  | 124 | $-1.00000000 \times 10^0$    |
| 93  | 30 | $1.00000000 \times 10^1$     | 86  | 125 | $9.89055612 \times 10^{-2}$  |
| 1   | 31 | $-7.06529316 \times 10^{-1}$ | 87  | 125 | $-1.43000000 \times 10^{-2}$ |
| 12  | 31 | $1.00000000 \times 10^0$     | 89  | 125 | $1.96000000 \times 10^{-1}$  |
| 13  | 32 | $1.00000000 \times 10^0$     | 92  | 125 | $4.95000000 \times 10^{-2}$  |
| 1   | 33 | $7.07683775 \times 10^{-1}$  | 94  | 125 | $-3.53000000 \times 10^{-1}$ |
| 14  | 33 | $1.00000000 \times 10^0$     | 88  | 126 | $-1.96000000 \times 10^{-1}$ |
| 13  | 34 | $-1.50666667 \times 10^{-2}$ | 91  | 126 | $1.00000000 \times 10^0$     |
| 15  | 34 | $-1.00000000 \times 10^0$    | 93  | 126 | $3.53000000 \times 10^{-1}$  |
| 1   | 35 | $1.31156239 \times 10^{-2}$  | 96  | 126 | $1.00000000 \times 10^0$     |
| 12  | 35 | $1.50666667 \times 10^{-2}$  | 86  | 127 | $-7.06529316 \times 10^{-1}$ |
| 14  | 35 | $-4.63666667 \times 10^{-2}$ | 97  | 127 | $1.00000000 \times 10^0$     |
| 86  | 35 | $-7.07683775 \times 10^0$    | 98  | 128 | $1.00000000 \times 10^0$     |
| 99  | 35 | $-1.00000000 \times 10^1$    | 86  | 129 | $7.07683775 \times 10^{-1}$  |
| 13  | 36 | $4.63666667 \times 10^{-2}$  | 99  | 129 | $1.00000000 \times 10^0$     |
| 16  | 36 | $1.00000000 \times 10^0$     | 98  | 130 | $-1.50666667 \times 10^{-2}$ |
| 98  | 36 | $1.00000000 \times 10^1$     | 100 | 130 | $-1.00000000 \times 10^0$    |
| 28  | 37 | $-1.00000000 \times 10^0$    | 86  | 131 | $1.31156239 \times 10^{-2}$  |
| 29  | 38 | $-1.00000000 \times 10^0$    | 97  | 131 | $1.50666667 \times 10^{-2}$  |
| 30  | 39 | $-1.00000000 \times 10^0$    | 99  | 131 | $-4.63666667 \times 10^{-2}$ |

## A. EQUATIONS OF MOTION

|     |    |                              |     |     |                              |
|-----|----|------------------------------|-----|-----|------------------------------|
| 31  | 40 | $1.00000000 \times 10^0$     | 98  | 132 | $4.63666667 \times 10^{-2}$  |
| 115 | 41 | $1.00000000 \times 10^1$     | 101 | 132 | $1.00000000 \times 10^0$     |
| 32  | 42 | $-1.00000000 \times 10^0$    | 113 | 133 | $-1.00000000 \times 10^0$    |
| 114 | 42 | $-1.00000000 \times 10^1$    | 114 | 134 | $-1.00000000 \times 10^0$    |
| 2   | 43 | $-1.00000000 \times 10^0$    | 115 | 135 | $-1.00000000 \times 10^0$    |
| 3   | 44 | $-1.00000000 \times 10^0$    | 116 | 136 | $1.00000000 \times 10^0$     |
| 4   | 45 | $-1.00000000 \times 10^0$    | 117 | 138 | $-1.00000000 \times 10^0$    |
| 5   | 46 | $1.00000000 \times 10^0$     | 87  | 139 | $-1.00000000 \times 10^0$    |
| 89  | 47 | $1.00000000 \times 10^1$     | 88  | 140 | $-1.00000000 \times 10^0$    |
| 6   | 48 | $-1.00000000 \times 10^0$    | 89  | 141 | $-1.00000000 \times 10^0$    |
| 88  | 48 | $-1.00000000 \times 10^1$    | 90  | 142 | $1.00000000 \times 10^0$     |
| 33  | 49 | $-1.00000000 \times 10^0$    | 91  | 144 | $-1.00000000 \times 10^0$    |
| 39  | 49 | $-1.00000000 \times 10^0$    | 118 | 145 | $-1.00000000 \times 10^0$    |
| 76  | 49 | $1.00000000 \times 10^0$     | 124 | 145 | $-1.00000000 \times 10^0$    |
| 80  | 49 | $1.00000000 \times 10^0$     | 161 | 145 | $1.00000000 \times 10^0$     |
| 34  | 50 | $-1.00000000 \times 10^0$    | 165 | 145 | $1.00000000 \times 10^0$     |
| 40  | 50 | $-1.00000000 \times 10^0$    | 119 | 146 | $-1.00000000 \times 10^0$    |
| 77  | 50 | $1.00000000 \times 10^0$     | 125 | 146 | $-1.00000000 \times 10^0$    |
| 81  | 50 | $1.00000000 \times 10^0$     | 162 | 146 | $1.00000000 \times 10^0$     |
| 35  | 51 | $-1.00000000 \times 10^0$    | 166 | 146 | $1.00000000 \times 10^0$     |
| 41  | 51 | $-1.00000000 \times 10^0$    | 120 | 147 | $-1.00000000 \times 10^0$    |
| 78  | 51 | $1.00000000 \times 10^0$     | 126 | 147 | $-1.00000000 \times 10^0$    |
| 82  | 51 | $1.00000000 \times 10^0$     | 163 | 147 | $1.00000000 \times 10^0$     |
| 35  | 52 | $-1.00000000 \times 10^{-1}$ | 167 | 147 | $1.00000000 \times 10^0$     |
| 36  | 52 | $-1.00000000 \times 10^0$    | 120 | 148 | $-1.00000000 \times 10^{-1}$ |
| 41  | 52 | $1.00000000 \times 10^{-1}$  | 121 | 148 | $-1.00000000 \times 10^0$    |
| 42  | 52 | $-1.00000000 \times 10^0$    | 126 | 148 | $1.00000000 \times 10^{-1}$  |
| 79  | 52 | $-4.47213596 \times 10^{-1}$ | 127 | 148 | $-1.00000000 \times 10^0$    |
| 83  | 52 | $1.00000000 \times 10^0$     | 164 | 148 | $-4.47213596 \times 10^{-1}$ |
| 37  | 53 | $-1.00000000 \times 10^0$    | 168 | 148 | $1.00000000 \times 10^0$     |
| 43  | 53 | $-1.00000000 \times 10^0$    | 122 | 149 | $-1.00000000 \times 10^0$    |
| 84  | 53 | $1.00000000 \times 10^0$     | 128 | 149 | $-1.00000000 \times 10^0$    |
| 120 | 53 | $1.00000000 \times 10^1$     | 169 | 149 | $1.00000000 \times 10^0$     |
| 126 | 53 | $1.00000000 \times 10^1$     | 118 | 150 | $1.00000000 \times 10^{-1}$  |
| 163 | 53 | $-1.00000000 \times 10^1$    | 123 | 150 | $-1.00000000 \times 10^0$    |
| 167 | 53 | $-1.00000000 \times 10^1$    | 124 | 150 | $-1.00000000 \times 10^{-1}$ |
| 33  | 54 | $1.00000000 \times 10^{-1}$  | 129 | 150 | $-1.00000000 \times 10^0$    |
| 38  | 54 | $-1.00000000 \times 10^0$    | 164 | 150 | $8.94427191 \times 10^{-1}$  |
| 39  | 54 | $-1.00000000 \times 10^{-1}$ | 170 | 150 | $1.00000000 \times 10^0$     |
| 44  | 54 | $-1.00000000 \times 10^0$    | 118 | 151 | $1.00000000 \times 10^0$     |
| 79  | 54 | $8.94427191 \times 10^{-1}$  | 134 | 151 | $-1.00000000 \times 10^0$    |
| 85  | 54 | $1.00000000 \times 10^0$     | 141 | 151 | $-1.00000000 \times 10^0$    |
| 119 | 54 | $-1.00000000 \times 10^1$    | 119 | 152 | $1.00000000 \times 10^0$     |
| 125 | 54 | $-1.00000000 \times 10^1$    | 135 | 152 | $-1.00000000 \times 10^0$    |
| 162 | 54 | $1.00000000 \times 10^1$     | 142 | 152 | $-1.00000000 \times 10^0$    |
| 166 | 54 | $1.00000000 \times 10^1$     | 120 | 153 | $1.00000000 \times 10^0$     |
| 33  | 55 | $1.00000000 \times 10^0$     | 136 | 153 | $-1.00000000 \times 10^0$    |
| 49  | 55 | $-1.00000000 \times 10^0$    | 143 | 153 | $-1.00000000 \times 10^0$    |
| 56  | 55 | $-1.00000000 \times 10^0$    | 119 | 154 | $-2.68480308 \times 10^{-1}$ |
| 34  | 56 | $1.00000000 \times 10^0$     | 121 | 154 | $1.00000000 \times 10^0$     |
| 50  | 56 | $-1.00000000 \times 10^0$    | 135 | 154 | $-8.20000000 \times 10^{-2}$ |
| 57  | 56 | $-1.00000000 \times 10^0$    | 142 | 154 | $1.80000000 \times 10^{-2}$  |
| 35  | 57 | $1.00000000 \times 10^0$     | 118 | 155 | $2.68480308 \times 10^{-1}$  |
| 51  | 57 | $-1.00000000 \times 10^0$    | 120 | 155 | $1.33859344 \times 10^{-1}$  |
| 58  | 57 | $-1.00000000 \times 10^0$    | 122 | 155 | $1.00000000 \times 10^0$     |
| 34  | 58 | $-2.68480308 \times 10^{-1}$ | 134 | 155 | $8.20000000 \times 10^{-2}$  |
| 36  | 58 | $1.00000000 \times 10^0$     | 136 | 155 | $-1.70000000 \times 10^{-1}$ |
| 50  | 58 | $-8.20000000 \times 10^{-2}$ | 141 | 155 | $-1.80000000 \times 10^{-2}$ |
| 57  | 58 | $1.80000000 \times 10^{-2}$  | 143 | 155 | $-1.70000000 \times 10^{-1}$ |



# A. EQUATIONS OF MOTION

|     |    |                              |     |     |                              |
|-----|----|------------------------------|-----|-----|------------------------------|
| 33  | 59 | $2.68480308 \times 10^{-1}$  | 119 | 156 | $-1.33859344 \times 10^{-1}$ |
| 35  | 59 | $1.33859344 \times 10^{-1}$  | 123 | 156 | $1.00000000 \times 10^0$     |
| 37  | 59 | $1.00000000 \times 10^0$     | 135 | 156 | $1.70000000 \times 10^{-1}$  |
| 49  | 59 | $8.20000000 \times 10^{-2}$  | 142 | 156 | $1.70000000 \times 10^{-1}$  |
| 51  | 59 | $-1.70000000 \times 10^{-1}$ | 124 | 157 | $1.00000000 \times 10^0$     |
| 56  | 59 | $-1.80000000 \times 10^{-2}$ | 148 | 157 | $-1.00000000 \times 10^0$    |
| 58  | 59 | $-1.70000000 \times 10^{-1}$ | 155 | 157 | $-1.00000000 \times 10^0$    |
| 120 | 59 | $-1.00000000 \times 10^1$    | 125 | 158 | $1.00000000 \times 10^0$     |
| 136 | 59 | $1.00000000 \times 10^1$     | 149 | 158 | $-1.00000000 \times 10^0$    |
| 143 | 59 | $1.00000000 \times 10^1$     | 156 | 158 | $-1.00000000 \times 10^0$    |
| 34  | 60 | $-1.33859344 \times 10^{-1}$ | 126 | 159 | $1.00000000 \times 10^0$     |
| 38  | 60 | $1.00000000 \times 10^0$     | 150 | 159 | $-1.00000000 \times 10^0$    |
| 50  | 60 | $1.70000000 \times 10^{-1}$  | 157 | 159 | $-1.00000000 \times 10^0$    |
| 57  | 60 | $1.70000000 \times 10^{-1}$  | 125 | 160 | $-2.68480308 \times 10^{-1}$ |
| 119 | 60 | $1.00000000 \times 10^1$     | 127 | 160 | $1.00000000 \times 10^0$     |
| 135 | 60 | $-1.00000000 \times 10^1$    | 149 | 160 | $-8.20000000 \times 10^{-2}$ |
| 142 | 60 | $-1.00000000 \times 10^1$    | 156 | 160 | $1.80000000 \times 10^{-2}$  |
| 39  | 61 | $1.00000000 \times 10^0$     | 124 | 161 | $2.68480308 \times 10^{-1}$  |
| 63  | 61 | $-1.00000000 \times 10^0$    | 126 | 161 | $1.33859344 \times 10^{-1}$  |
| 70  | 61 | $-1.00000000 \times 10^0$    | 128 | 161 | $1.00000000 \times 10^0$     |
| 40  | 62 | $1.00000000 \times 10^0$     | 148 | 161 | $8.20000000 \times 10^{-2}$  |
| 64  | 62 | $-1.00000000 \times 10^0$    | 150 | 161 | $-1.70000000 \times 10^{-1}$ |
| 71  | 62 | $-1.00000000 \times 10^0$    | 155 | 161 | $-1.80000000 \times 10^{-2}$ |
| 41  | 63 | $1.00000000 \times 10^0$     | 157 | 161 | $-1.70000000 \times 10^{-1}$ |
| 65  | 63 | $-1.00000000 \times 10^0$    | 125 | 162 | $-1.33859344 \times 10^{-1}$ |
| 72  | 63 | $-1.00000000 \times 10^0$    | 129 | 162 | $1.00000000 \times 10^0$     |
| 40  | 64 | $-2.68480308 \times 10^{-1}$ | 149 | 162 | $1.70000000 \times 10^{-1}$  |
| 42  | 64 | $1.00000000 \times 10^0$     | 156 | 162 | $1.70000000 \times 10^{-1}$  |
| 64  | 64 | $-8.20000000 \times 10^{-2}$ | 158 | 163 | $8.94427191 \times 10^{-1}$  |
| 71  | 64 | $1.80000000 \times 10^{-2}$  | 161 | 163 | $-1.00000000 \times 10^0$    |
| 39  | 65 | $2.68480308 \times 10^{-1}$  | 159 | 164 | $1.00000000 \times 10^0$     |
| 41  | 65 | $1.33859344 \times 10^{-1}$  | 162 | 164 | $-1.00000000 \times 10^0$    |
| 43  | 65 | $1.00000000 \times 10^0$     | 158 | 165 | $4.47213596 \times 10^{-1}$  |
| 63  | 65 | $8.20000000 \times 10^{-2}$  | 163 | 165 | $-1.00000000 \times 10^0$    |
| 65  | 65 | $-1.70000000 \times 10^{-1}$ | 159 | 166 | $-1.09759846 \times 10^{-1}$ |
| 70  | 65 | $-1.80000000 \times 10^{-2}$ | 160 | 166 | $-4.47213596 \times 10^{-1}$ |
| 72  | 65 | $-1.70000000 \times 10^{-1}$ | 162 | 166 | $-1.09759846 \times 10^{-1}$ |
| 126 | 65 | $-1.00000000 \times 10^1$    | 164 | 166 | $4.47213596 \times 10^{-1}$  |
| 150 | 65 | $1.00000000 \times 10^1$     | 158 | 167 | $1.23247604 \times 10^{-1}$  |
| 157 | 65 | $1.00000000 \times 10^1$     | 161 | 167 | $1.09759846 \times 10^{-1}$  |
| 40  | 66 | $-1.33859344 \times 10^{-1}$ | 163 | 167 | $5.60703280 \times 10^{-2}$  |
| 44  | 66 | $1.00000000 \times 10^0$     | 159 | 168 | $-5.60703280 \times 10^{-2}$ |
| 64  | 66 | $1.70000000 \times 10^{-1}$  | 160 | 168 | $8.94427191 \times 10^{-1}$  |
| 71  | 66 | $1.70000000 \times 10^{-1}$  | 162 | 168 | $-5.60703280 \times 10^{-2}$ |
| 125 | 66 | $1.00000000 \times 10^1$     | 164 | 168 | $-8.94427191 \times 10^{-1}$ |
| 149 | 66 | $-1.00000000 \times 10^1$    | 130 | 169 | $1.00000000 \times 10^0$     |
| 156 | 66 | $-1.00000000 \times 10^1$    | 134 | 169 | $1.00000000 \times 10^0$     |
| 73  | 67 | $8.94427191 \times 10^{-1}$  | 131 | 170 | $1.00000000 \times 10^0$     |
| 76  | 67 | $-1.00000000 \times 10^0$    | 135 | 170 | $1.00000000 \times 10^0$     |
| 74  | 68 | $1.00000000 \times 10^0$     | 132 | 171 | $1.00000000 \times 10^0$     |
| 77  | 68 | $-1.00000000 \times 10^0$    | 136 | 171 | $1.00000000 \times 10^0$     |
| 73  | 69 | $4.47213596 \times 10^{-1}$  | 132 | 172 | $5.62400000 \times 10^{-2}$  |
| 78  | 69 | $-1.00000000 \times 10^0$    | 133 | 172 | $1.00000000 \times 10^0$     |
| 74  | 70 | $-1.09759846 \times 10^{-1}$ | 136 | 172 | $-5.62400000 \times 10^{-2}$ |
| 75  | 70 | $-4.47213596 \times 10^{-1}$ | 132 | 173 | $1.00000000 \times 10^{-1}$  |
| 77  | 70 | $-1.09759846 \times 10^{-1}$ | 136 | 173 | $-1.00000000 \times 10^{-1}$ |
| 79  | 70 | $4.47213596 \times 10^{-1}$  | 130 | 174 | $-5.62400000 \times 10^{-2}$ |
| 73  | 71 | $1.23247604 \times 10^{-1}$  | 131 | 174 | $-1.00000000 \times 10^{-1}$ |
| 76  | 71 | $1.09759846 \times 10^{-1}$  | 134 | 174 | $5.62400000 \times 10^{-2}$  |

## A. EQUATIONS OF MOTION

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|     |    |                              |     |     |                              |
|-----|----|------------------------------|-----|-----|------------------------------|
| 78  | 71 | $5.60703280 \times 10^{-2}$  | 135 | 174 | $1.00000000 \times 10^{-1}$  |
| 158 | 71 | $-4.47213596 \times 10^0$    | 137 | 175 | $1.00000000 \times 10^0$     |
| 163 | 71 | $1.00000000 \times 10^1$     | 141 | 175 | $1.00000000 \times 10^0$     |
| 74  | 72 | $-5.60703280 \times 10^{-2}$ | 138 | 176 | $1.00000000 \times 10^0$     |
| 75  | 72 | $8.94427191 \times 10^{-1}$  | 142 | 176 | $1.00000000 \times 10^0$     |
| 77  | 72 | $-5.60703280 \times 10^{-2}$ | 139 | 177 | $1.00000000 \times 10^0$     |
| 79  | 72 | $-8.94427191 \times 10^{-1}$ | 143 | 177 | $1.00000000 \times 10^0$     |
| 159 | 72 | $1.00000000 \times 10^1$     | 139 | 178 | $7.50000000 \times 10^{-2}$  |
| 162 | 72 | $-1.00000000 \times 10^1$    | 140 | 178 | $1.00000000 \times 10^0$     |
| 45  | 73 | $1.00000000 \times 10^0$     | 143 | 178 | $-7.50000000 \times 10^{-2}$ |
| 49  | 73 | $1.00000000 \times 10^0$     | 139 | 179 | $1.00000000 \times 10^{-1}$  |
| 46  | 74 | $1.00000000 \times 10^0$     | 143 | 179 | $-1.00000000 \times 10^{-1}$ |
| 50  | 74 | $1.00000000 \times 10^0$     | 137 | 180 | $-7.50000000 \times 10^{-2}$ |
| 47  | 75 | $1.00000000 \times 10^0$     | 138 | 180 | $-1.00000000 \times 10^{-1}$ |
| 51  | 75 | $1.00000000 \times 10^0$     | 141 | 180 | $7.50000000 \times 10^{-2}$  |
| 47  | 76 | $5.62400000 \times 10^{-2}$  | 142 | 180 | $1.00000000 \times 10^{-1}$  |
| 48  | 76 | $1.00000000 \times 10^0$     | 144 | 181 | $1.00000000 \times 10^0$     |
| 51  | 76 | $-5.62400000 \times 10^{-2}$ | 148 | 181 | $1.00000000 \times 10^0$     |
| 47  | 77 | $1.00000000 \times 10^{-1}$  | 145 | 182 | $1.00000000 \times 10^0$     |
| 51  | 77 | $-1.00000000 \times 10^{-1}$ | 149 | 182 | $1.00000000 \times 10^0$     |
| 132 | 77 | $-1.00000000 \times 10^1$    | 146 | 183 | $1.00000000 \times 10^0$     |
| 136 | 77 | $-1.00000000 \times 10^1$    | 150 | 183 | $1.00000000 \times 10^0$     |
| 45  | 78 | $-5.62400000 \times 10^{-2}$ | 146 | 184 | $-5.62400000 \times 10^{-2}$ |
| 46  | 78 | $-1.00000000 \times 10^{-1}$ | 147 | 184 | $1.00000000 \times 10^0$     |
| 49  | 78 | $5.62400000 \times 10^{-2}$  | 150 | 184 | $5.62400000 \times 10^{-2}$  |
| 50  | 78 | $1.00000000 \times 10^{-1}$  | 146 | 185 | $1.00000000 \times 10^{-1}$  |
| 131 | 78 | $1.00000000 \times 10^1$     | 150 | 185 | $-1.00000000 \times 10^{-1}$ |
| 135 | 78 | $1.00000000 \times 10^1$     | 144 | 186 | $5.62400000 \times 10^{-2}$  |
| 52  | 79 | $1.00000000 \times 10^0$     | 145 | 186 | $-1.00000000 \times 10^{-1}$ |
| 56  | 79 | $1.00000000 \times 10^0$     | 148 | 186 | $-5.62400000 \times 10^{-2}$ |
| 53  | 80 | $1.00000000 \times 10^0$     | 149 | 186 | $1.00000000 \times 10^{-1}$  |
| 57  | 80 | $1.00000000 \times 10^0$     | 151 | 187 | $1.00000000 \times 10^0$     |
| 54  | 81 | $1.00000000 \times 10^0$     | 155 | 187 | $1.00000000 \times 10^0$     |
| 58  | 81 | $1.00000000 \times 10^0$     | 152 | 188 | $1.00000000 \times 10^0$     |
| 54  | 82 | $7.50000000 \times 10^{-2}$  | 156 | 188 | $1.00000000 \times 10^0$     |
| 55  | 82 | $1.00000000 \times 10^0$     | 153 | 189 | $1.00000000 \times 10^0$     |
| 58  | 82 | $-7.50000000 \times 10^{-2}$ | 157 | 189 | $1.00000000 \times 10^0$     |
| 54  | 83 | $1.00000000 \times 10^{-1}$  | 153 | 190 | $-7.50000000 \times 10^{-2}$ |
| 58  | 83 | $-1.00000000 \times 10^{-1}$ | 154 | 190 | $1.00000000 \times 10^0$     |
| 139 | 83 | $-1.00000000 \times 10^1$    | 157 | 190 | $7.50000000 \times 10^{-2}$  |
| 143 | 83 | $-1.00000000 \times 10^1$    | 153 | 191 | $1.00000000 \times 10^{-1}$  |
| 52  | 84 | $-7.50000000 \times 10^{-2}$ | 157 | 191 | $-1.00000000 \times 10^{-1}$ |
| 53  | 84 | $-1.00000000 \times 10^{-1}$ | 151 | 192 | $7.50000000 \times 10^{-2}$  |
| 56  | 84 | $7.50000000 \times 10^{-2}$  | 152 | 192 | $-1.00000000 \times 10^{-1}$ |
| 57  | 84 | $1.00000000 \times 10^{-1}$  | 155 | 192 | $-7.50000000 \times 10^{-2}$ |
| 138 | 84 | $1.00000000 \times 10^1$     | 156 | 192 | $1.00000000 \times 10^{-1}$  |

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The full state space equations:

$$\begin{bmatrix} \mathbf{E} & \mathbf{0} \\ \mathbf{0} & \mathbf{I} \end{bmatrix} \begin{Bmatrix} \dot{\mathbf{x}} \\ \mathbf{y} \end{Bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} \begin{Bmatrix} \mathbf{x} \\ \mathbf{u} \end{Bmatrix}$$

## A. EQUATIONS OF MOTION

$$\begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} = \begin{bmatrix} -1.19210883 \times 10^1 & -4.84897992 \times 10^2 & -5.02897774 \times 10^2 & -1.16094827 \times 10^2 & -1.41722568 \times 10^2 & 3.69204693 \times 10^2 & 1.04555301 \times 10^2 \\ 1.82316138 \times 10^2 & -2.55781454 \times 10^2 & 5.05407060 \times 10^2 & -4.07742268 \times 10^2 & 1.01460694 \times 10^2 & -8.81795166 \times 10^1 & -4.22072875 \times 10^2 \\ -1.62396146 \times 10^1 & 1.94405996 \times 10^2 & 1.06286511 \times 10^3 & -7.34927274 \times 10^2 & 6.84211663 \times 10^2 & -3.17877193 \times 10^2 & -6.63540894 \times 10^2 \\ 9.35131279 \times 10^1 & 4.22133585 \times 10^2 & 3.40081009 \times 10^2 & 1.46029863 \times 10^2 & 1.51880139 \times 10^2 & -3.16164674 \times 10^2 & 7.98887891 \times 10^0 \\ 8.62155818 \times 10^0 & -1.50595594 \times 10^2 & -3.05192857 \times 10^2 & -8.66972880 \times 10^1 & 1.34521125 \times 10^2 & 3.96109082 \times 10^2 & -3.43951597 \times 10^1 \\ 1.36527657 \times 10^2 & -1.97804606 \times 10^2 & 4.55210777 \times 10^2 & -5.35914302 \times 10^2 & 3.48884395 \times 10^2 & 3.92858714 \times 10^1 & -3.61291918 \times 10^2 \\ -2.16356148 \times 10^2 & 7.63681184 \times 10^2 & -1.44296765 \times 10^3 & 1.59120969 \times 10^3 & -8.50495464 \times 10^2 & -6.57790429 \times 10^1 & 1.42097237 \times 10^3 \\ 2.82701041 \times 10^2 & -8.50863097 \times 10^2 & 4.11873980 \times 10^2 & -9.89777931 \times 10^2 & 3.53203864 \times 10^2 & 3.77432291 \times 10^2 & -6.50281624 \times 10^2 \\ -3.60155323 \times 10^2 & 1.58014990 \times 10^3 & -1.00930150 \times 10^3 & 1.93242224 \times 10^3 & -5.71540156 \times 10^2 & -4.12938446 \times 10^2 & 1.38929935 \times 10^3 \\ 4.95397539 \times 10^1 & -6.07423172 \times 10^2 & -6.66571468 \times 10^2 & -5.40466140 \times 10^1 & -2.68904454 \times 10^2 & 4.04961000 \times 10^2 & 1.46207580 \times 10^2 \\ -3.13058586 \times 10^2 & 1.00658849 \times 10^3 & -5.68215239 \times 10^2 & 1.19074959 \times 10^3 & -4.20483732 \times 10^2 & -3.74735915 \times 10^2 & 8.20551521 \times 10^2 \\ 4.29936917 \times 10^2 & -1.65438462 \times 10^3 & -2.99434639 \times 10^2 & -1.20942232 \times 10^3 & 1.13299262 \times 10^2 & 8.61425561 \times 10^2 & -4.86505321 \times 10^2 \\ -6.46384583 \times 10^2 & 1.47810351 \times 10^3 & -3.72010652 \times 10^3 & 4.01814436 \times 10^3 & -2.40685275 \times 10^3 & 8.30615295 \times 10^1 & 3.25975005 \times 10^3 \\ -1.63825158 \times 10^2 & 4.72469435 \times 10^2 & -3.52159018 \times 10^2 & 7.75406776 \times 10^2 & -3.65300722 \times 10^2 & -1.08811769 \times 10^2 & 4.40948043 \times 10^2 \\ -1.44717016 \times 10^2 & 6.80922916 \times 10^2 & -2.46214046 \times 10^2 & 7.20967288 \times 10^2 & -1.61536444 \times 10^2 & -2.12762936 \times 10^2 & 3.86117011 \times 10^2 \\ -4.39009068 \times 10^1 & 5.77415472 \times 10^1 & -2.49212743 \times 10^2 & 2.35463148 \times 10^2 & -2.21566750 \times 10^2 & 1.74773658 \times 10^0 & 1.34921308 \times 10^2 \\ -1.88001942 \times 10^2 & -4.37359556 \times 10^2 & -1.01866986 \times 10^3 & 2.75212916 \times 10^2 & -5.27307540 \times 10^2 & 3.52390793 \times 10^2 & 4.79490602 \times 10^2 \\ 9.26662297 \times 10^1 & -1.29668836 \times 10^2 & -2.08376845 \times 10^2 & 1.79268017 \times 10^1 & -6.76805011 \times 10^0 & 1.77439263 \times 10^2 & 1.16006035 \times 10^2 \\ -1.25657732 \times 10^2 & -1.48836123 \times 10^2 & -9.78512926 \times 10^2 & 6.09580851 \times 10^2 & -5.60484819 \times 10^2 & 2.73353225 \times 10^2 & 5.83750308 \times 10^2 \\ -5.23032298 \times 10^1 & -1.64585579 \times 10^2 & -8.69558427 \times 10^2 & 7.05712387 \times 10^2 & -7.37085673 \times 10^2 & 1.12846318 \times 10^2 & 6.69344166 \times 10^2 \\ 3.61409277 \times 10^2 & -1.37708954 \times 10^3 & 1.19575813 \times 10^3 & -1.88432510 \times 10^3 & 5.91301849 \times 10^2 & 2.05069509 \times 10^2 & -1.41518130 \times 10^3 \\ 2.16438426 \times 10^2 & -7.05720590 \times 10^2 & 1.03684150 \times 10^3 & -1.42157029 \times 10^3 & 6.93707494 \times 10^2 & 3.42585671 \times 10^1 & -1.06631071 \times 10^3 \\ 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 \\ -1.27255391 \times 10^{-2} & -1.31803126 \times 10^{-2} & 2.89409422 \times 10^{-2} & 6.32092926 \times 10^{-2} & -8.00101526 \times 10^{-2} & 8.57558971 \times 10^{-2} & 1.22773744 \times 10^{-3} \\ -1.74361664 \times 10^{-2} & 4.25847834 \times 10^{-2} & 1.06163569 \times 10^{-2} & -2.74888616 \times 10^{-2} & 5.53137714 \times 10^{-2} & 4.62868172 \times 10^{-2} & -2.97304190 \times 10^{-2} \end{bmatrix}$$

$$\mathbf{E} = \begin{bmatrix} 1.27557686 \times 10^0 & -4.56964952 \times 10^{-1} & 9.13843435 \times 10^{-1} & 4.71602121 \times 10^{-1} & -2.77614345 \times 10^0 & -1.80078191 \times 10^0 & 1.16896924 \times 10^0 & 2.48251 \\ -7.80908508 \times 10^{-1} & 4.37170359 \times 10^0 & 1.18290164 \times 10^{-2} & -6.30143436 \times 10^{-1} & -9.13602598 \times 10^{-1} & 1.31977341 \times 10^{-1} & 5.10820807 \times 10^{-1} & -3.62189 \\ 4.26803425 \times 10^{-1} & -1.97038291 \times 10^0 & -3.80125352 \times 10^{-2} & 8.65743452 \times 10^{-1} & 2.93589425 \times 10^0 & 1.08148376 \times 10^0 & -1.09299378 \times 10^0 & -3.49236 \\ -5.88492027 \times 10^{-1} & 3.15822893 \times 10^{-1} & -2.91710279 \times 10^{-1} & 4.29015220 \times 10^{-1} & -9.47954295 \times 10^{-1} & -5.58362275 \times 10^{-1} & 1.22794989 \times 10^0 & 1.03055 \\ 2.43777822 \times 10^{-1} & -1.31755568 \times 10^0 & -1.08177058 \times 10^{-1} & -6.47014017 \times 10^{-1} & -1.93833230 \times 10^{-1} & -1.25922992 \times 10^0 & 4.51826243 \times 10^{-1} & 2.49700 \\ 1.14544607 \times 10^{-1} & -5.01588368 \times 10^{-1} & -2.85651318 \times 10^{-1} & 5.02400702 \times 10^{-1} & 1.59550876 \times 10^0 & 4.40599528 \times 10^{-1} & -1.08774311 \times 10^0 & -5.39105 \\ -1.82284413 \times 10^0 & -1.02742683 \times 10^0 & -6.92454114 \times 10^{-1} & -2.40878770 \times 10^0 & 8.23375245 \times 10^{-1} & 1.15262023 \times 10^0 & -2.79571423 \times 10^0 & -2.74101 \\ 7.42159204 \times 10^{-1} & -1.46530789 \times 10^{-1} & 4.29799921 \times 10^{-1} & 3.47670743 \times 10^{-1} & 9.01181162 \times 10^{-1} & 2.39988665 \times 10^{-1} & -1.06148323 \times 10^0 & -2.63679 \\ -1.48451021 \times 10^0 & -1.23320091 \times 10^0 & -7.41625425 \times 10^{-1} & -3.01190755 \times 10^0 & -3.60034350 \times 10^0 & -1.72003741 \times 10^0 & 9.41973171 \times 10^{-1} & 2.01734 \\ 1.99088568 \times 10^{-1} & 1.68004736 \times 10^0 & 7.98340915 \times 10^{-1} & -7.21893933 \times 10^{-1} & -3.43238044 \times 10^0 & -8.74533211 \times 10^{-1} & 9.27870296 \times 10^{-1} & -2.73859 \\ 1.25923038 \times 10^{-1} & -3.23721219 \times 10^0 & 3.80139028 \times 10^{-1} & 9.52718297 \times 10^{-1} & 1.51728256 \times 10^{-1} & -5.00365248 \times 10^{-1} & 6.88081961 \times 10^{-1} & 4.01857 \\ 4.30326182 \times 10^{-1} & 4.16959254 \times 10^{-1} & 9.08481855 \times 10^{-1} & -3.73413035 \times 10^{-1} & -3.08598069 \times 10^{-1} & 8.21855505 \times 10^{-1} & -2.30419006 \times 10^0 & -2.30939 \\ -1.64087620 \times 10^0 & -2.64876422 \times 10^0 & -2.81473221 \times 10^{-1} & -4.10966021 \times 10^0 & -5.94376207 \times 10^0 & -2.38120258 \times 10^0 & 6.02939500 \times 10^{-1} & 2.40749 \\ 3.20448850 \times 10^{-1} & 7.44509709 \times 10^{-1} & 9.88220889 \times 10^{-2} & -4.56394056 \times 10^{-1} & -2.68073934 \times 10^0 & -2.37531924 \times 10^0 & 2.42237795 \times 10^0 & 2.41957 \\ -5.71303173 \times 10^{-1} & -1.02395778 \times 10^0 & 7.49967777 \times 10^{-2} & -7.85571779 \times 10^{-1} & -2.59503443 \times 10^0 & -1.22268192 \times 10^0 & 1.38381826 \times 10^0 & 2.08950 \\ 2.91175400 \times 10^{-1} & -2.06590542 \times 10^0 & 3.70369891 \times 10^{-1} & 8.83970969 \times 10^{-1} & 1.43971374 \times 10^0 & 8.26958906 \times 10^{-1} & -5.43712352 \times 10^{-1} & 1.00603 \\ 1.57537014 \times 10^0 & -3.21644480 \times 10^0 & 1.10556282 \times 10^0 & 1.98937715 \times 10^0 & 1.18146554 \times 10^{-1} & 3.98863829 \times 10^{-1} & -3.67611849 \times 10^{-1} & 2.80084 \\ -1.30086857 \times 10^{-1} & -1.41248354 \times 10^0 & -3.66586913 \times 10^{-1} & -7.63703235 \times 10^{-1} & -1.26041544 \times 10^{-1} & -4.92175813 \times 10^{-2} & -7.24771159 \times 10^{-1} & -2.94226 \\ 2.93687429 \times 10^{-1} & -1.99798262 \times 10^0 & 2.19576261 \times 10^{-1} & -6.89568550 \times 10^{-1} & -1.13407591 \times 10^0 & -2.25620827 \times 10^{-1} & -1.15226777 \times 10^{-1} & 1.40592 \\ -3.62661572 \times 10^{-1} & 1.93380460 \times 10^0 & 2.22939149 \times 10^{-1} & -1.66860302 \times 10^0 & -1.56067269 \times 10^0 & -1.44976538 \times 10^{-1} & -5.26356930 \times 10^{-2} & -1.95197 \\ 6.84877008 \times 10^{-1} & 3.38079926 \times 10^0 & 1.14006882 \times 10^0 & 9.91907097 \times 10^{-1} & 1.59364382 \times 10^0 & 1.41807611 \times 10^0 & -1.01495352 \times 10^0 & -4.46040 \\ 9.99750826 \times 10^{-1} & 9.42344739 \times 10^{-1} & 1.18677730 \times 10^0 & 2.25977693 \times 10^0 & 1.09187186 \times 10^0 & 9.72514433 \times 10^{-1} & 2.01301607 \times 10^{-1} & -4.49164 \\ 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000000 \times 10^0 & 0.00000 \end{bmatrix}$$

The reduced state space equations:

$$\begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} = \begin{bmatrix} -1.34760647 \times 10^2 & -1.28263750 \times 10^1 & 3.05020151 \times 10^{-1} & -4.67808985 \times 10^0 & -1.14783821 \times 10^1 & 1.25575171 \times 10^0 & -3.07158897 \times 10^1 \\ 2.71415755 \times 10^2 & 1.15239076 \times 10^1 & -1.15137026 \times 10^1 & 1.00594801 \times 10^1 & 2.46824151 \times 10^1 & -2.70029216 \times 10^0 & 6.60495823 \times 10^1 \\ -1.11343442 \times 10^2 & -6.05983085 \times 10^1 & -5.23832059 \times 10^1 & 5.69689291 \times 10^1 & -3.19878815 \times 10^1 & 3.49952081 \times 10^0 & -8.55988442 \times 10^1 \\ 1.57836812 \times 10^2 & 4.16301512 \times 10^1 & 2.53074576 \times 10^1 & -2.90623659 \times 10^1 & 2.58009940 \times 10^1 & -3.08983944 \times 10^0 & 7.55779717 \times 10^1 \\ -2.44686313 \times 10^2 & 1.56838075 \times 10^1 & 2.91582211 \times 10^1 & -2.67343359 \times 10^1 & -2.64192159 \times 10^1 & 1.16652431 \times 10^0 & -2.85387209 \times 10^1 \\ -3.21314161 \times 10^1 & 2.19877100 \times 10^1 & 2.64576267 \times 10^1 & -2.70957232 \times 10^1 & 4.85342459 \times 10^0 & -1.01242898 \times 10^0 & 2.18531708 \times 10^1 \\ -8.72872142 \times 10^1 & -4.81189676 \times 10^0 & 6.33900734 \times 10^0 & -7.85700663 \times 10^0 & -5.71847594 \times 10^0 & 3.14296674 \times 10^0 & -1.68599270 \times 10^1 \\ -1.26259684 \times 10^2 & 1.34599317 \times 10^1 & 1.76367128 \times 10^1 & -1.96764664 \times 10^1 & -9.99232985 \times 10^0 & 2.79051503 \times 10^0 & -1.31491516 \times 10^1 \\ 2.90079211 \times 10^{-2} & -9.40069537 \times 10^{-3} & -1.57262249 \times 10^{-3} & 2.62953689 \times 10^{-2} & 1.21094367 \times 10^{-2} & 3.34840862 \times 10^{-4} & -8.17329215 \times 10^{-3} \\ -1.40803243 \times 10^{-3} & -1.29513098 \times 10^{-2} & 1.28097181 \times 10^{-2} & 2.49273270 \times 10^{-2} & -2.15688967 \times 10^{-3} & -2.21952130 \times 10^{-4} & 5.43875327 \times 10^{-3} \end{bmatrix}$$