Social network Graph Link Prediction - Facebook Challenge

```
In [10]:
          #Importing Libraries
              # please do go through this python notebook:
             import warnings
             warnings.filterwarnings("ignore")
             import pandas as pd#pandas to create small dataframes
             import datetime #Convert to unix time
             import time #Convert to unix time
              # if numpy is not installed already : pip3 install numpy
             {\bf import} \ {\bf numpy} \ {\bf as} \ {\bf np} {\it \#Do} \ {\it aritmetic operations} \ {\it on arrays}
              # matplotlib: used to plot graphs
             import matplotlib
             import matplotlib.pylab as plt
              import seaborn as sns#Plots
             from matplotlib import rcParams#Size of plots
             from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
             import math
             import pickle
              import os
              # to install xgboost: pip3 install xgboost
             import xgboost as xgb
             import warnings
             import networkx as nx
             import pdb
             import pickle
              from pandas import HDFStore, DataFrame
             from pandas import read hdf
              from scipy.sparse.linalg import svds, eigs
              import gc
```

1. Reading Data

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = \frac{|X \cap Y|}{|X \cup Y|}$$

2.2 Cosine distance

$$Cosine Distance = \frac{|X \cap Y|}{|X| \cdot |Y|}$$

```
In [18]: \parallel #for followees
             def cosine_for_followees(a,b):
                 try:
                     if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(b))) == 0:
                     sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))))/\
                                                 (math.sqrt(len(set(train graph.successors(a)))*len((set(train graph.suc
                     return sim
                 except:
                     return 0
In [19]:
             0.0
In [20]:
          Ы
             0
In [21]: | def cosine_for_followers(a,b):
                 try:
                     if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph.predecessors(b))) == 0:
                     sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(b)))))/\
                                                  (math.sqrt(len(set(train graph.predecessors(a))))*(len(set(train graph
                    return sim
                 except:
                    return 0
In [22]: ▶
            0.02886751345948129
In [23]:
            0
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html (https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

4.2 Checking for same community

```
wcc=list(nx.weakly_connected_components(train_graph))
            def belongs_to_same_wcc(a,b):
               index = []
               if train_graph.has_edge(b,a):
                   {\tt return} \ 1
               if train_graph.has_edge(a,b):
                      for i in wcc:
                          if a in i:
                              index= i
                              break
                       if (b in index):
                          train_graph.remove_edge(a,b)
                          if compute_shortest_path_length(a,b) ==-1:
                              train_graph.add_edge(a,b)
                              return 0
                          else:
                              train_graph.add_edge(a,b)
                              return 1
                       else:
                          return 0
               else:
                       for i in wcc:
                          if a in i:
                              index= i
                              break
                       if(b in index):
                          return 1
                       else:
In [30]: N
   Out[30]: 0
In [31]: Ŋ └──
   Out[31]: 0
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x, y) = \sum_{u \in N(x) \cap N(y)} \frac{1}{log(|N(u)|)}$$

```
In [32]: 

#adar index
             def calc_adar_in(a,b):
                 sum=0
                 try:
                     \verb|n=list(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))||
                     if len(n)!=0:
                         for i in n:
                             sum=sum+(1/np.log10(len(list(train graph.predecessors(i)))))
                         return sum
                     else:
                         return 0
                 except:
In [33]: N
   Out[33]: 0
In [34]: N
   Out[34]: 0
```

4.4 Is persion was following back:

```
In [36]: M Cout[36]: 1

In [37]: M Cout[37]: 0
```

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz_centrality (https://en.wikipedia.org/wiki/Katz_centrality)

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/ (https://www.geeksforgeeks.org/katz-centrality-measure/) Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node is

$$x_i = \alpha \sum_j A_{ij} x_j + \beta,$$
 where $\,$ A $\,$ is the adjacency matrix of the graph G with eigenvalues $\,$.

The parameter

controls the initial centrality and

$$\alpha < \frac{1}{\lambda_{\dots}}$$

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm (https://en.wikipedia.org/wiki/HITS_algorithm)

4.7 Preferential Attachment

In Preferential Attachment, We estimate how "rich" our two vertices are by calculating the multiplication between the number of friends $(|\Gamma(x)|)$ or followers each vertex has

```
In [84]:  # calculating preferential attachment as multiplication of number of neighbors of each vertex in pair
def preferential_attachment(a,b):
    try:
        n_a = len(set(train_graph.neighbors(a)))
        n_b = len(set(train_graph.neighbors(b)))
        return n_a * n_b

    except:
```

5. Featurization

5. 1 Reading a sample of Data from both train and test

```
In [42]: | import random
             if os.path.isfile('C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebook/data/afte
                 filename = "C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebook/data/after
                 # you uncomment this line, if you dont know the lentgh of the file name
                 # here we have hardcoded the number of lines as 15100030
                 # n train = sum(1 for line in open(filename)) #number of records in file (excludes header)
                 n train = 15100028
                 s = 100000 #desired sample size
                 skip train = sorted(random.sample(range(1, n train+1), n train-s))
                 #https://stackoverflow.com/a/22259008/4084039
In [43]: 🔰 if os.path.isfile('C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebook/data/afte
                 filename = "C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebook/data/after_
                 # you uncomment this line, if you dont know the lentgh of the file name
                 # here we have hardcoded the number of lines as 3775008
                 # n test = sum(1 for line in open(filename)) #number of records in file (excludes header)
                 n_{test} = 3775006
                 s = 50000 #desired sample size
                 skip_test = sorted(random.sample(range(1, n_test+1), n_test-s))
                 #https://stackoverflow.com/a/22259008/4084039
In [44]:  print("Number of rows in the train data file:", n_train)
             print("Number of rows we are going to elimiate in train data are",len(skip_train))
             print("Number of rows in the test data file:", n_test)
             Number of rows in the train data file: 15100028
             Number of rows we are going to elimiate in train data are 15000028
             Number of rows in the test data file: 3775006
             Number of rows we are going to elimiate in test data are 3725006
In [45]: M df final train = pd.read csv('C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebook
             df_final_train['indicator_link'] = pd.read_csv('C:/Users/PareshBhatia/Downloads/Learning/Data Science/anal
             print("Our train matrix size ", df_final_train.shape)
             df final train.head(2)
             Our train matrix size (100002, 3)
   Out[45]:
                source node destination node indicator link
             0
                    273084
                                 1505602
             1
                   1222366
                                 1493194
          | df_final_test = pd.read_csv('C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebool
In [46]:
             df_final_test['indicator_link'] = pd.read_csv('C:/Users/PareshBhatia/Downloads/Learning/Data Science/analy
             print("Our test matrix size ", df_final_test.shape)
             df_final_test.head(2)
             Our test matrix size (50002, 3)
   Out.[46]:
                source_node destination_node indicator_link
                    848424
                                 784690
                   1631553
                                 1034818
```

5.2 Adding a set of features

1. jaccard followers

we will create these each of these features for both train and test data points

```
2. jaccard followees
           3. cosine followers
           4. cosine followees
           5. num followers s
           6. num_followees_s
           7. num_followers_d
           8. num_followees_d
           9. inter_followers
          10. inter_followees
          if not os.path.isfile('data/fea_sample/storage_sample_stage1.h5'):
                 #mapping jaccrd followers to train and test data
                 df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:
                                                          jaccard_for_followers(row['source_node'],row['destination_node
                 df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                                          jaccard_for_followers(row['source_node'],row['destination_node
                 #mapping jaccrd followees to train and test data
                 df final train['jaccard followees'] = df final train.apply(lambda row:
                                                          jaccard_for_followees(row['source_node'], row['destination_node
                 df_final_test['jaccard_followees'] = df_final_test.apply(lambda row:
                                                          jaccard_for_followees(row['source_node'],row['destination_node
                     #mapping jaccrd followers to train and test data
                 df_final_train['cosine_followers'] = df_final_train.apply(lambda row:
                                                          cosine for followers(row['source node'], row['destination node']
                 df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
                                                          cosine_for_followers(row['source_node'],row['destination_node'
                 #mapping jaccrd followees to train and test data
                 df_final_train['cosine_followees'] = df_final_train.apply(lambda row:
                                                          cosine_for_followees(row['source_node'],row['destination_node'
                 df_final_test['cosine_followees'] = df_final_test.apply(lambda row:
                                                          cosine_for_followees(row['source_node'],row['destination node']
In [48]:  def compute features stage1(df final):
                 #calculating no of followers followees for source and destination
                 #calculating intersection of followers and followees for source and destination
                 num_followers_s=[]
                 num_followees_s=[]
                 num followers d=[]
                 num_followees_d=[]
                 inter_followers=[]
                 inter followees=[]
                 for i,row in df final.iterrows():
                         s1=set(train_graph.predecessors(row['source_node']))
                         s2=set(train_graph.successors(row['source_node']))
                     except:
                         s1 = set()
                     try:
                         d1=set(train graph.predecessors(row['destination node']))
                         d2=set(train graph.successors(row['destination node']))
                     except:
                         d1 = set()
                         d2 = set()
                     num_followers_s.append(len(s1))
                     num\_followees\_s.append(len(s2))
                     num_followers_d.append(len(d1))
                     num_followees_d.append(len(d2))
                     inter_followers.append(len(s1.intersection(d1)))
                     inter followees.append(len(s2.intersection(d2)))
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [51]: | if not os.path.isfile('data/fea sample/storage sample stage2.h5'):
                                          #mapping adar index on train
                                         df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node'],row['de
                                         #mapping adar index on test
                                         df final test['adar index'] = df final test.apply(lambda row: calc adar in(row['source node'],row['des
                                          #mapping followback or not on train
                                         df_final_train['follows_back'] = df_final_train.apply(lambda row: follows_back(row['source_node'],row[
                                         #mapping followback or not on test
                                         df_final_test['follows_back'] = df_final_test.apply(lambda row: follows_back(row['source_node'],row['definal_test.apply(lambda row: follows_back(row['source_node'],row['definal_test.apply(lambda row: follows_back(row['source_node'],row['definal_test.apply(lambda row: follows_back(row['source_node'],row['definal_test.apply(lambda row: follows_back(row['source_node'],row['definal_test.apply(lambda row: follows_back(row['source_node'],row['definal_test.apply(lambda row]])
                                          #mapping same component of wcc or not on train
                                         df_final_train['same_comp'] = df_final_train.apply(lambda row: belongs_to_same_wcc(row['source_node'],
                                         ##mapping same component of wcc or not on train
                                         df_final_test['same_comp'] = df_final_test.apply(lambda row: belongs_to_same_wcc(row['source_node'],row
                                         #mapping shortest path on train
                                         df_final_train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path_length(row['selection of the compute_shortest_path_length) and train['shortest_path_length'] = df_final_train.apply(lambda row: compute_shortest_path_length) and train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path_length) and train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path_length) and train['shortest_path_length'] = df_final_train['shortest_path_length'] = df_final_tr
                                         #mapping shortest path on test
                                         df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute_shortest_path_length(row['sou
                                              hdf = HDFStore('data/fea_sample/storage_sample_stage2.h5')
                                             hdf.put('train_df',df_final_train, format='table', data_columns=True)
                                             hdf.put('test df', df final test, format='table', data columns=True)
                                             hdf.close()
                                # else:
                                             df final train = read hdf('data/fea sample/storage sample stage2.h5', 'train df',mode='r')
                                              df_final_test = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'test_df',mode='r')
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - · weight of incoming edges + weight of outgoing edges
 - · weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities_s of source
- 9. authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W = \frac{1}{\sqrt{1 + |X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
In [52]:
          | #weight for source and destination of each link
             Weight in = {}
             Weight_out = {}
             for i in tqdm(train_graph.nodes()):
                s1=set(train_graph.predecessors(i))
                 w_{in} = 1.0/(np.sqrt(1+len(s1)))
                Weight in[i]=w in
                 s2=set(train graph.successors(i))
                 w \text{ out } = 1.0/(np.sqrt(1+len(s2)))
                Weight_out[i]=w_out
             #for imputing with mean
             mean_weight_in = np.mean(list(Weight_in.values()))
             100%|
                                                                                 1780722/1780722 [00:25<00:00,
```

69509.22it/s]

```
In [57]: | if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
                   #mapping to pandas train
                   df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x, mean weight)
                   df_final_train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out.get(x,mean_weight
                    #mapping to pandas test
                   df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x, mean weight
                   df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x, mean weight o
                   #some features engineerings on the in and out weights
                   df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_out
df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight_out
                   df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.weight_out)
                   df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_train.weight_out)
                    #some features engineerings on the in and out weights
                   df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
                   df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
```

```
In [67]: | if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
                 #page rank for source and destination in Train and Test
                 #if anything not there in train graph then adding mean page rank
                 df_final_train['page_rank_s'] = df_final_train.source_node.apply(lambda x:pr.get(x,mean_pr))
                 df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda x:pr.get(x,mean_pr))
                 df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
                 df final test['page rank d'] = df final test.destination node.apply(lambda x:pr.get(x,mean pr))
                 #Katz centrality score for source and destination in Train and test
                 #if anything not there in train graph then adding mean katz score
                 df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.get(x,mean_katz))
                 df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.get(x,mean_katz))
                 df final test['katz s'] = df final test.source node.apply(lambda x: katz.get(x,mean katz))
                 df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
                 #Hits algorithm score for source and destination in Train and test
                 \#if anything not there in train graph then adding 0
                 df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x,0))
df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda x: hits[0].get(x,0))
                 #Hits algorithm score for source and destination in Train and Test
                 #if anything not there in train graph then adding 0
                 \texttt{df\_final\_train['authorities\_s']} = \texttt{df\_final\_train.source\_node.apply(lambda x: hits[1].get(x,0))}
                  df_{final\_train['authorities\_d']} = df_{final\_train.destination\_node.apply(lambda x: hits[1].get(x,0)) 
                 \texttt{df\_final\_test['authorities\_s']} = \texttt{df\_final\_test.source\_node.apply(lambda} \ x: \ \texttt{hits[1].get(x,0))}
                 df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda x: hits[1].get(x,0))
                   hdf = HDFStore('data/fea_sample/storage_sample_stage3.h5')
                   hdf.put('train df',df final train, format='table', data columns=True)
                   hdf.put('test df',df final test, format='table', data columns=True)
                   hdf.close()
             # else:
                   df_final_train = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'train_df',mode='r')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [72]: | if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
                                 df_final_train.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
                                df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] = \
                                df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
                                df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
                                df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5','svd_v_d_6']] = \
                                df_final_train.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
                                df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
                                df final test[['svd u d 1', 'svd u d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] = \
                                \label{eq:df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)} $$ df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series) $$ df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(lambda x: svd(x, U)
                                df_final_test.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
                                hdf = HDFStore('data/fea_sample/storage_sample_stage4.h5')
                                    hdf.put('train df',df final train, format='table', data columns=True)
                                    hdf.put('test_df',df_final_test, format='table', data_columns=True)
```

Create additional feature for preferential attachment and svd dot product - Stage 5

```
In [85]:
          #mapping preferential attachment on train
             df final train['preferential attachment'] = df final train.apply(lambda row: preferential attachment(row['
             #mapping preferential attachment on test
             df_final_test['preferential_attachment'] = df_final_test.apply(lambda row: preferential_attachment(row['so
In [87]: 🔰 # create additional features for multiplication of svd features on source and node
             # create for train
             df_final_train['svd_u_dot'] = df_final_train.apply(lambda row: np.sum(np.multiply(svd(row['source_node'],U
             df_final_train['svd_v_dot'] = df_final_train.apply(lambda row: np.sum(np.multiply(svd(row['source_node'],v))
             df final test['svd u dot'] = df final test.apply(lambda row: np.sum(np.multiply(svd(row['source node'],U),:
             df final test['svd v dot'] = df final test.apply(lambda row: np.sum(np.multiply(svd(row['source node'], V.T
In [88]: N
   Out[88]:
                source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num
              0
                    273084
                                  1505602
                                                                0
                                                                                        0.000000
                                                                                                                        11
                                                                          0.000000
                                                                                                      0.000000
              1
                    1222366
                                  1493194
                                                  1
                                                                0
                                                                          0.000000
                                                                                        0.000000
                                                                                                     0.000000
                                                                                                                         2
                                                                                                                         4
              2
                    1331983
                                  270629
                                                  1
                                                                0
                                                                          0.055556
                                                                                        0.046875
                                                                                                      0.119523
              3
                    1150809
                                  1440757
                                                  1
                                                                0
                                                                          0.000000
                                                                                        0.111166
                                                                                                      0.000000
                                                                                                                         7
                    1825888
                                   356016
                                                                0
                                                                          0.230769
                                                                                        0.306186
                                                                                                      0.433013
                                                                                                                         6
              4
             5 rows × 58 columns
          | # store train and test data in h5 file
In [92]:
             hdf = HDFStore('C:/Users/PareshBhatia/Downloads/Learning/Data Science/analytics vidya/facebook/data/fea sa
             hdf.put('train_df',df_final_train, format='table', data_columns=True)
             hdf.put('test df',df final test, format='table', data columns=True)
             hdf.close()
```