Ratio, Proportion, and Similarity

Objectives

- 1. Express a ratio in simplest form.
- 2. Solve for an unknown term in a given proportion.
- 3. Express a given proportion in an equivalent form.
- 4. State and apply the properties of similar polygons.

7-1 Ratio and Proportion

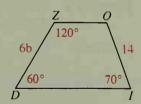
The **ratio** of one number to another is the quotient when the first number is divided by the second. This quotient is usually expressed in *simplest form*.

The ratio of 8 to 12 is
$$\frac{8}{12}$$
, or $\frac{2}{3}$.

If
$$y \neq 0$$
, the ratio of x to y is $\frac{x}{y}$.

Since we cannot divide by zero, a ratio $\frac{r}{s}$ is defined only if $s \neq 0$. When an expression such as $\frac{r}{s}$ appears in this book, you may assume that $s \neq 0$.

- **Example 1** a. Find the ratio of OI to ZD.
 - **b.** Find the ratio of the measure of the smallest angle of the trapezoid to that of the largest angle.



Solution

a.
$$\frac{OI}{ZD} = \frac{14}{6b} = \frac{7}{3b}$$

The ratio of OI to ZD is 7 to 3b.

b. $\angle O$ has measure 180 - 70, or 110. Thus $\angle D$ is the smallest angle and $\angle Z$ is the largest angle.

$$\frac{m \angle D}{m \angle Z} = \frac{60}{120} = \frac{1}{2}$$

The ratio of the measure of the smallest angle of the trapezoid to that of the largest angle is 1 to 2.

Ratios can be used to compare two numbers. To find the ratio of the lengths of two segments, the segments must be measured in terms of the same unit.