

Application*Finding the Shortest Path*

The owners of pipeline l plan to construct a pumping station at a point S on line l in order to pipe oil to two major customers, located at A and B . To minimize the cost of constructing lines from S to A and B , they wish to locate S along l so that the distance $SA + SB$ is as small as possible.



The construction engineer uses the following method to locate S :

1. Draw a line through B perpendicular to l , intersecting l at point P .
2. On this perpendicular, locate point C so that $PC = PB$.
3. Draw \overline{AC} .
4. Locate S at the intersection of \overline{AC} and l .

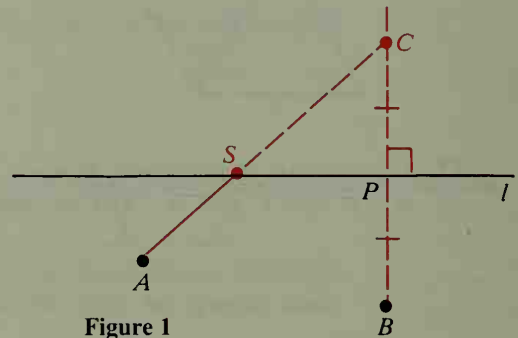


Figure 1

Figure 2 shows the path of the new pipelines through the pumping station located at S , and an alternative path going through a different point, X , on l . You can use Theorem 6-4 (the Triangle Inequality) to show that if X is any point on l other than S , then $AX + XB > AS + SB$. So any alternative path is longer than the path through S .

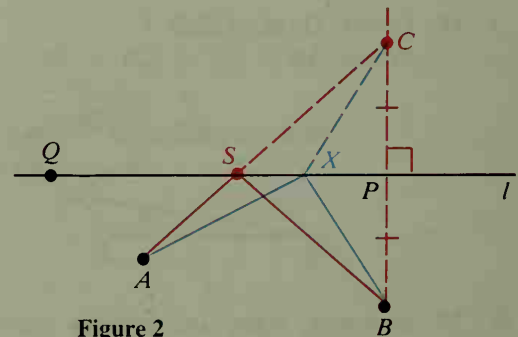


Figure 2

