Now consider another pyramid with the same base and height but having 100 steps instead of 10 steps. The height of each layer is  $\frac{10}{100} = \frac{1}{10}$ , and the volume of each layer is computed using the formula V = Bh:

Volume of top layer 
$$= \left(\frac{1}{10}\right)^2 \cdot \frac{1}{10}$$
  
Volume of second layer  $= \left(2 \cdot \frac{1}{10}\right)^2 \cdot \frac{1}{10} = \left(\frac{2}{10}\right)^2 \cdot \frac{1}{10}$   
Volume of third layer  $= \left(3 \cdot \frac{1}{10}\right)^2 \cdot \frac{1}{10} = \left(\frac{3}{10}\right)^2 \cdot \frac{1}{10}$   
 $\vdots$   
Volume of 99th layer  $= \left(99 \cdot \frac{1}{10}\right)^2 \cdot \frac{1}{10} = \left(\frac{99}{10}\right)^2 \cdot \frac{1}{10}$   
Volume of 100th layer  $= \left(100 \cdot \frac{1}{10}\right)^2 \cdot \frac{1}{10} = \left(\frac{100}{10}\right)^2 \cdot \frac{1}{10}$ 

Thus, the volume of the pyramid is:

$$V = \left(\frac{1}{10}\right)^2 \cdot \frac{1}{10} + \left(\frac{2}{10}\right)^2 \cdot \frac{1}{10} + \left(\frac{3}{10}\right)^2 \cdot \frac{1}{10} + \cdots + \left(\frac{99}{10}\right)^2 \cdot \frac{1}{10} + \left(\frac{100}{10}\right)^2 \cdot \frac{1}{10}$$

The following computer program finds the total volume for the given pyramid with N steps.

```
10 LET V = 0

20 PRINT "HOW MANY STEPS ARE THERE";

30 INPUT N

40 LET H = 10/N

50 FOR X = 1 TO N

60 LET V = V + (X * H) ↑2 * H
```

70 NEXT X

80 PRINT "VOLUME OF PYRAMID WITH ";N;" STEPS IS ";V

90 END

## **Exercises**

- 1. RUN the given program to verify the volume of the 10-step pyramid and to find the volume of the 100-step pyramid.
- 2. a. Suppose that another pyramid with the same base and height has 1000 steps. RUN the program to find the volume.
  - **b.** Make a chart that shows the volume for the given number of steps: 10, 100, 500, 750, 900, 1000.
  - **c.** As the number of steps increases, what value do the volumes seem to be approaching?
  - **d.** What is the volume of a regular square pyramid with base edge of 10 and height 10?
  - e. What can you conclude from comparing the answers to parts (b)-(d)?