

SAMPLE PROBLEM B

Diffraction Gratings

PROBLEM

Monochromatic light from a helium-neon laser ($\lambda = 632.8 \text{ nm}$) shines at a right angle to the surface of a diffraction grating that contains 150 500 lines/m. Find the angles at which one would observe the first-order and second-order maxima.

SOLUTION

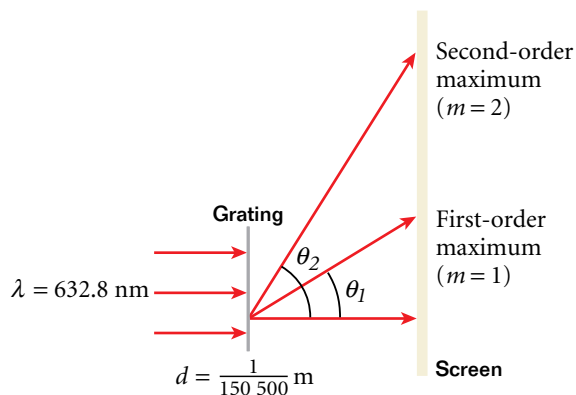
1. DEFINE

Given: $\lambda = 632.8 \text{ nm} = 6.328 \times 10^{-7} \text{ m}$ $m = 1 \text{ and } 2$

$$d = \frac{1}{150\,500 \frac{\text{lines}}{\text{m}}} = \frac{1}{150\,500} \text{ m}$$

Unknown: $\theta_1 = ?$ $\theta_2 = ?$

Diagram:



2. PLAN **Choose an equation or situation:** Use the equation for a diffraction grating.

$$d \sin \theta = \pm m \lambda$$

Rearrange the equation to isolate the unknown:

$$\theta = \sin^{-1} \left(\frac{m \lambda}{d} \right)$$

3. CALCULATE **Substitute the values into the equation and solve:**

For the first-order maximum, $m = 1$:

$$\theta_1 = \sin^{-1} \left(\frac{\lambda}{d} \right) = \sin^{-1} \left(\frac{6.328 \times 10^{-7} \text{ m}}{\frac{1}{150\,500} \text{ m}} \right)$$

$\theta_1 = 5.465^\circ$

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