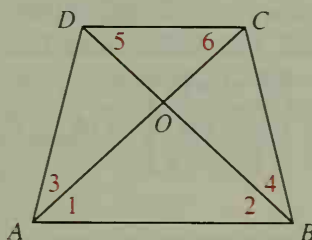


Flow Proofs

Proofs can be written in a variety of forms, including: (1) two-column form, (2) paragraph form, and (3) flow form. In a *flow proof*, a diagram with implication arrows (\rightarrow) shows the logical flow of the statements of a proof. The statements in the diagram are numbered and the reasons for each are given below the flow diagram.

Example 1 Given: $\angle 1 \cong \angle 2$;
 $\angle 3 \cong \angle 4$
 Prove: $\angle 5 \cong \angle 6$



Flow Proof:

1. $\angle 1 \cong \angle 2 \rightarrow$ 2. $\overline{AO} \cong \overline{BO}$
 3. $\angle 3 \cong \angle 4$
 4. $\angle AOD \cong \angle BOC$ } \rightarrow 5. $\triangle AOD \cong \triangle BOC$

6. $\overline{DO} \cong \overline{CO} \rightarrow$ 7. $\angle 5 \cong \angle 6$

Reasons

1. Given
2. If 2 \angle of a \triangle are \cong , the sides opp. them are \cong .
3. Given
4. Vertical \angle are \cong .
5. ASA Postulate
6. Corr. parts of $\cong \triangle$ are \cong .
7. Isosceles \triangle Theorem

Because this flow proof is long, we have drawn an arrow connecting steps 5 and 6 to show that the proof continues below. You can do this or turn your paper sideways to accommodate a long proof.

One advantage of flow proof is that it shows clearly which steps depend on other steps. In the example above, for instance, we see that step 5 (whose justification is ASA) depends on steps 2, 3, and 4, each of which provides one of the three congruences needed for ASA. The next example shows how a complex proof can be understood more easily by organizing it into a flow proof.