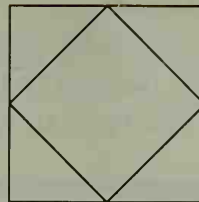


10. The inner square in the diagram is formed by connecting the midpoints of the outer square. It is possible to map the outer square to the inner square by performing a rotation followed by a dilation.



- a. Give the center of the rotation and the amount of the rotation.
  - b. Give the center of the dilation and the scale factor.
- 11–21. Work Exercises 32, 42 on page 527; Classroom Exercise 7 on page 532; Exercises 28–31, 33 on pages 533–534; Classroom Exercise 11 on page 536; Exercise 23 on page 538; and Classroom Exercise 5 on page 541.

## Circles (Chapter 9)

**Objective:** Write the equations of tangent lines, and make observations about circles and their symmetry. (Requires understanding of Lessons 13-1 through 13-7 and 14-1 through 14-5.)

Many relationships among circles and their chords and tangents can be investigated by using coordinates and transformations. Before studying the example below, you should understand how the equation of a circle is used in Examples 3 and 4 of Lesson 13-1.

- Example**
- a. Sketch the circle  $x^2 + y^2 = 10$  and the line  $y = 3x + 10$ .
  - b. Solve the two equations simultaneously and show that there is just one solution for  $x$ .
  - c. Find the corresponding value for  $y$ . Label the solution point,  $T$ , on your sketch. What does this tell you about the line and the circle?
  - d. Use the slopes to show that  $\overline{OT}$  is perpendicular to the line  $y = 3x + 10$ .

**Solution** a. The circle has center  $O$  and radius  $\sqrt{10}$ .

$$\begin{aligned}
 \text{b.} \quad & x^2 + y^2 = 10 \\
 & x^2 + (3x + 10)^2 = 10 \\
 & x^2 + 9x^2 + 60x + 100 = 10 \\
 & 10x^2 + 60x + 90 = 0 \\
 & x^2 + 6x + 9 = 0 \\
 & (x + 3)(x + 3) = 0 \\
 & x + 3 = 0 \\
 & x = -3
 \end{aligned}$$

- c.  $y = 3x + 10$ ;  $y = 3(-3) + 10$ ;  $y = 1$ .  
Point  $T$  is  $(-3, 1)$ . The line is tangent to the circle at point  $T$ .

- d. The slope of  $\overline{OT}$  is  $\frac{1 - 0}{-3 - 0} = -\frac{1}{3}$ . The slope of  $y = 3x + 10$  is 3. Since the slopes are negative reciprocals, the lines are perpendicular.

