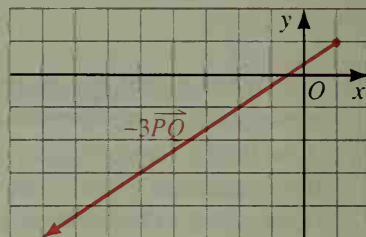
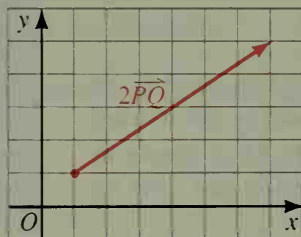
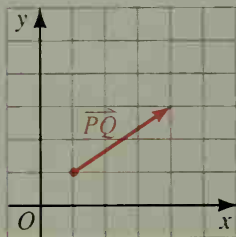
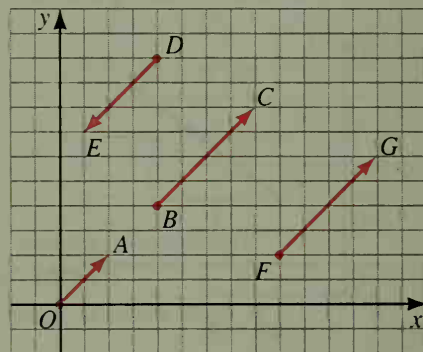


The symbol  $2\vec{PQ}$  represents a vector that has twice the magnitude of  $\vec{PQ}$  and has the same direction. If  $\vec{PQ} = (3, 2)$ , it should not surprise you that  $2\vec{PQ} = (2 \cdot 3, 2 \cdot 2) = (6, 4)$ . In general, if the vector  $\vec{PQ} = (a, b)$ , then  $k\vec{PQ} = (ka, kb)$ ;  $k\vec{PQ}$  is called a **scalar multiple** of  $\vec{PQ}$ . Multiplying a vector by a real number  $k$  multiplies the length of the vector by  $|k|$ . If  $k < 0$ , the direction of the vector reverses as well. This is illustrated in the diagrams below. What ordered pair represents  $-3\vec{PQ}$ ?



Two vectors are *perpendicular* if the arrows representing them have perpendicular directions. Two vectors are *parallel* if the arrows representing them have the same direction or opposite directions. All the vectors shown at the right are parallel. Notice that  $\vec{OA}$  and  $\vec{BC}$  are parallel even though the points  $O$ ,  $A$ ,  $B$ , and  $C$  are collinear.

Two vectors are **equal** if they have the same magnitude and the same direction. In the diagram,  $\vec{BC} = \vec{FG}$ .



You can tell by using slopes whether nonvertical vectors are parallel or perpendicular. Example 2 shows how.

- Example 2**
- Show that  $(9, -6)$  and  $(-6, 4)$  are parallel.
  - Show that  $(9, -6)$  and  $(2, 3)$  are perpendicular.

**Solution**

- Slope of  $(9, -6)$  is  $\frac{-6}{9} = -\frac{2}{3}$ .

$$\text{Slope of } (-6, 4) = \frac{4}{-6} = -\frac{2}{3}.$$

Since the slopes are equal, the vectors are parallel.

- Slope of  $(9, -6)$  is  $\frac{-6}{9} = -\frac{2}{3}$ .

$$\text{Slope of } (2, 3) \text{ is } \frac{3}{2}.$$

Since  $\frac{-2}{3} \cdot \frac{3}{2} = -1$ , the vectors are perpendicular.