

FIGURE 7 This graph shows that there is an inverse relationship between volume and pressure.

Plotting the values of volume versus pressure for a gas at constant temperature gives a curve like that in **Figure 7.** The general volume-pressure relationship that is illustrated is called Boyle's law. **Boyle's law** states that the volume of a fixed mass of gas varies inversely with the pressure at constant temperature.

Mathematically, Boyle's law can be expressed as follows:

$$PV = k$$

In the equation above, P is the pressure, V is the volume, and k is a constant. Since P and V vary inversely, their product remains the same. Because two quantities that are equal to the same thing are equal to each other, the relationship between changes of pressure and volume can be expressed as shown below.

$$P_1V_1 = P_2V_2$$

 P_1 and V_1 represent initial conditions. P_2 and V_2 represent a different set of conditions. Given three of the four values P_1 , V_1 , P_2 , and V_2 , you can use this equation to calculate the fourth value for a system at constant temperature.

SAMPLE PROBLEM C

For more help, go to the *Math Tutor* at the end of this chapter.

A sample of oxygen gas has a volume of 150.0 mL when its pressure is 0.947 atm. What will the volume of the gas be at a pressure of 0.987 atm if the temperature remains constant?

SOLUTION

1 ANALYZE Given: V_1 of $O_2 = 150.0 \text{ mL}$; P_1 of $O_2 = 0.947 \text{ atm}$; P_2 of $O_2 = 0.987 \text{ atm}$

Unknown: V_2 of O_2 in mL

2 PLAN Rearrange the equation for Boyle's law $(P_1V_1 = P_2V_2)$ to obtain V_2 .

$$V_2 = \frac{P_1 V_1}{P_2}$$

3 COMPUTE Substitute values for P_1 , V_1 , and P_2 to obtain the new volume, V_2 .

$$V_2 = \frac{P_1 V_1}{P_2} = \frac{(0.947 \text{ atm})(150.0 \text{ mL O}_2)}{0.987 \text{ atm}} = 144 \text{ mL O}_2$$

4 EVALUATE When the pressure is increased slightly at constant temperature, the volume decreases slightly, as expected. Units cancel to give milliliters, a volume unit.

PRACTICE

Answers in Appendix E

1. A balloon filled with helium gas has a volume of 500 mL at a pressure of 1 atm. The balloon is released and reaches an altitude of 6.5 km, where the pressure is 0.5 atm. If the temperature has remained the same, what volume does the gas occupy at this height?

