f C 38. Given: Parallel lines l and k and point A.

**a.** Construct an equilateral  $\triangle ABC$  with B on k and C on l using the following method.

Step 2. Let point C on l be the preimage of B.

Step 1. Rotate l through 60° about A and let B be the point on k where the image of l intersects k. (The diagram for Exercise 35 may be helpful in rotating l.)

k

A

Exs. 38, 39

**b.** Explain why  $\triangle ABC$  is equilateral.

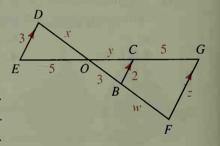
c. Are there other equilateral triangles with vertices at A and on l and k?

39. Given the figure for Exercise 38, construct a square AXYZ with X on k and Z on l.

## **Mixed Review Exercises**

Given  $\overline{ED} \parallel \overline{BC} \parallel \overline{FG}$ . Complete the statements.

- 1.  $\triangle OBC$  is similar to  $\triangle$ ? and  $\triangle$ ?
- **2.** The scale factor of  $\triangle OBC$  to  $\triangle ODE$  is =?
- 3. Find the values of x, y, z, and w.
- **4.** The scale factor of  $\triangle ODE$  to  $\triangle OFG$  is  $\frac{?}{}$ .
- **5.** The ratio of the areas of  $\triangle OBC$  and  $\triangle ODE$  is  $\frac{?}{}$ .
- **6.** The ratio of the areas of  $\triangle ODE$  and  $\triangle OFG$  is  $\frac{?}{}$
- 7. The ratio of the areas of  $\triangle OBC$  and  $\triangle OFG$  is  $\frac{?}{}$



## 14-5 Dilations

Reflections, translations, glide reflections, and rotations are isometries, or congruence mappings. In this section we consider a transformation related to similarity rather than congruence. It is called a **dilation**. The dilation  $D_{O,k}$ 

has center O and nonzero scale factor k.  $D_{O, k}$  maps any point P to a point P' determined as follows:

- (1) If k > 0, P' lies on  $\overrightarrow{OP}$  and  $OP' = k \cdot OP$ .
- (2) If k < 0, P' lies on the ray opposite  $\overrightarrow{OP}$  and  $OP' = |k| \cdot OP$ .
- (3) The center O is its own image.

If |k| > 1, the dilation is called an **expansion**. If |k| < 1, the dilation is called a **contraction**.

A developing leaf undergoes an expansion, keeping approximately the same shape as it grows in size.

