What is the freezing-point depression of water in a solution of 17.1 g of sucrose,  $C_{12}H_{22}O_{11}$ , in 200. g of water? What is the actual freezing point of the solution?

## **SOLUTION**

**1 ANALYZE** Given: solute mass and chemical formula =  $17.1 \text{ g C}_{12}H_{22}O_{11}$ 

solvent mass and identity = 200. g water

Unknown: a. freezing-point depression

**b.** freezing point of the solution

**2 PLAN** Find the molal freezing-point constant,  $K_f$ , for water in **Table 2.** To use the equation for freezing-point depression,  $\Delta t_f = K_f m$ , you need to determine the molality of the solution.

mass of solute (g) 
$$\times \frac{1 \text{ mol solute}}{\text{molar mass of solute (g)}} = \text{amount of solute (mol)}$$

$$\frac{\text{amount of solute (mol)}}{\text{mass of solvent (g)}} \times \frac{1000 \text{ g water}}{1 \text{ kg water}} = \text{molality}$$

$$\Delta t_f = K_f m$$
 f.p. solution = f.p. solvent +  $\Delta t_f$ 

**3 COMPUTE**  $17.1 \text{ g C}_{12}\text{H}_{22}\text{O}_{11} \times \frac{1 \text{ mol C}_{12}\text{H}_{22}\text{O}_{11}}{342.34 \text{ g C}_{12}\text{H}_{22}\text{O}_{11}} = 0.0500 \text{ mol C}_{12}\text{H}_{22}\text{O}_{11}$ 

$$\frac{0.0500 \text{ mol C}_{12}\text{H}_{22}\text{O}_{11}}{200.\text{ g water}} \times \frac{1000 \text{ g water}}{\text{kg water}} = \frac{0.250 \text{ mol C}_{12}\text{H}_{22}\text{O}_{11}}{\text{kg water}} = 0.250 \text{ m}$$

- a.  $\Delta t_f = 0.250 \ m \times (-1.86^{\circ} \text{C/m}) = -0.465^{\circ} \text{C}$
- **b.** f.p. solution =  $0.000^{\circ}$ C +  $(-0.465^{\circ}$ C) =  $-0.465^{\circ}$ C

## **SAMPLE PROBLEM D**

For more help, go to the *Math Tutor* at the end of this chapter.

A water solution containing an unknown quantity of a nonelectrolyte solute is found to have a freezing point of -0.23°C. What is the molal concentration of the solution?

## **SOLUTION**

**1 ANALYZE Given:** freezing point of solution =  $-0.23^{\circ}$ C

**Unknown:** molality of the solution

Water is the solvent, so you will need the value of  $K_f$ , the molal-freezing-point constant for water, from **Table 2.** The  $\Delta t_f$  for this solution is the difference between the f.p. of water and the f.p. of the solution. Use the equation for freezing-point depression to calculate molality.

$$\Delta t_f = \text{f.p. of solution} - \text{f.p. of pure solvent}$$
  
 $\Delta t_f = K_f m$  Solve for molality,  $m$ .

$$m = \frac{\Delta t_f}{K_f}$$