

Example 2 Find an equation of each line described.

- The line through $(1, 2)$ and parallel to the line $y = 3x - 7$
- The line through $(1, 2)$ and perpendicular to the line $y = 3x - 7$
- The line through the points $(-3, 0)$ and $(1, 8)$

Solution

- If the line is parallel to the line $y = 3x - 7$, its slope must be 3. Substituting in $y - y_1 = m(x - x_1)$ gives $y - 2 = 3(x - 1)$, or $y = 3x - 1$.
- The required line has slope $-\frac{1}{3}$. (Why?) Thus an equation in point-slope form is $y - 2 = -\frac{1}{3}(x - 1)$, or $y = -\frac{1}{3}x + \frac{7}{3}$, or $x + 3y = 7$.
- First find the slope: $m = \frac{8 - 0}{1 - (-3)} = 2$
Then use the point-slope form with *either* given point.
Using $(-3, 0)$, the equation is $y - 0 = 2[x - (-3)]$, or $y = 2x + 6$.
Using $(1, 8)$, the equation is $y - 8 = 2(x - 1)$, or $y = 2x + 6$.

Classroom Exercises

Give an equation of each line described.

- Slope $= -\frac{1}{2}$; y-intercept $= 5$
- Slope $= \frac{3}{7}$; y-intercept $= 8$
- x-intercept $= 2$; y-intercept $= 4$
- x-intercept $= 2$; y-intercept $= -6$
- The x-axis
- The y-axis
- y-intercept $= -3$; parallel to $y = -\frac{4}{5}x + 2$
- y-intercept $= 0$; perpendicular to $y = -\frac{7}{4}x + 9$
- Slope $= \frac{5}{8}$; passes through $(3, 4)$
- Slope $= -2$; passes through $(8, 6)$

State the slope of the line and name two points on the line.

- $y = -(x + 7)$
- $y + 2 = \frac{1}{2}(x - 5)$
- $y - c = \frac{a}{b}(x - d)$
- Line l is tangent to $\odot O$ at point $P(3, 4)$.
 - Find the radius of the circle.
 - Give an equation of the circle.
 - Find the slope of line l .
 - Give an equation of line l .

