11. If you apply the Koch curve construction to an equilateral triangle, you get the sequence of pre-fractals shown below. Calculate the area of each pre-fractal. If you can, calculate the area of the fractal. (*Hint*: Let the area of the original equilateral triangle be 1 square unit.)



## Dimension of Fractals

The dimension of a fractal is usually not an integer. Measuring the dimension of a fractal involves finding its *self-similarity dimension*, defined below.

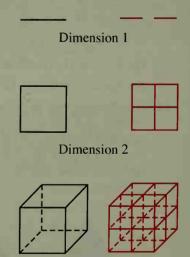
In general, if a shape can be replaced, or covered, by N shapes similar to itself with scale factor  $\frac{1}{R}$ , then it has self-similarity dimension D, where  $N = R^D$ .

The example below demonstrates the use of this definition with shapes whose dimensions you already know.

**Example 1** a. A *segment* can be replaced by 2 segments similar to itself with scale factor  $\frac{1}{2}$ . In this case, N = 2 and R = 2. Since  $2 = (2)^1$ , we will say that the segment has self-

similarity dimension 1.

- **b.** A square can be replaced by 4 squares similar to itself with scale factor  $\frac{1}{2}$ . In this case, N = 4 and R = 2. Since  $4 = 2^2$ , we will say that the square has self-similarity dimension 2.
- c. A *cube* can be replaced by 8 cubes similar to itself with scale factor  $\frac{1}{2}$ . In this case, N = 8 and R = 2. Since  $8 = 2^3$ , we will say that the cube has self-similarity dimension 3.



Dimension 3