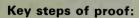
Theorem 14-4

A rotation is an isometry.

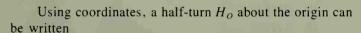
Given: \mathcal{R}_{Q} maps P to P' and Q to Q'.

Prove: $\overline{PO} \cong \overline{P'O'}$

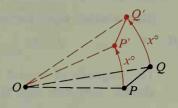


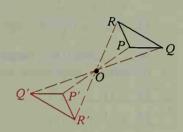
- 1. OP = OP', OQ = OQ' (Definition of rotation)
- 2. $m \angle POP' = m \angle QOQ' = x$ (Definition of rotation)
- 3. $m \angle POQ = m \angle P'OQ'$ (Subtraction Property of =: subtract $m \angle QOP'$.)
- 4. $\triangle POQ \cong \triangle P'OQ'$ (SAS Postulate)
- 5. $\overline{PO} \cong \overline{P'O'}$ (Corr. parts of $\cong \mathbb{A}$ are \cong .)

A rotation about point O through 180° is called a halfturn about O and is usually denoted by H_0 . The diagram shows $\triangle PQR$ and its image $\triangle P'Q'R'$ by H_Q . Notice that O is the midpoint of $\overline{PP'}$, $\overline{QQ'}$, and $\overline{RR'}$.



$$H_o:(x, y) \to (-x, -y).$$





Classroom Exercises

State another name for each rotation.

- 1. $\mathcal{R}_{0.50}$
- 2. $\mathcal{R}_{0} = 40$ 3. $\mathcal{R}_{0} = 90$ 4. $\mathcal{R}_{0} = 400$
- 5. Ro. 180

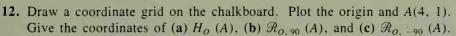
Exs. 6-11

In the diagram for Exercises 6-11, O is the center of equilateral $\triangle PST$. State the images of points P, S, and T for each rotation.

- 6. $\mathcal{R}_{0,120}$
- 7. $\mathcal{R}_{0} = 120$
- 8. Ro. 360

Name each image point.

- 9. $\mathcal{R}_{T, 60}(S)$
- 10. $\mathcal{R}_{T=-60}(P)$
- 11. $\mathcal{R}_{O, 240}(P)$



- 13. Repeat Exercise 12 if A has coordinates (-3, 5).
- 14. Is congruence invariant under a half-turn mapping? Explain.
- 15. Read each expression aloud.
 - a. $R_k(A) = A'$

- **b.** $H_0: (-2, 0) \to (2, 0)$
- **c.** $T:(x, y) \to (x 1, y + 3)$ **d.** $\mathcal{R}_{P \to 0}$