

6-2 Inverses and Contrapositives

You have already studied the converse of an if-then statement. Now we consider two other related conditionals called the *inverse* and the *contrapositive*.

Statement: If p , then q .

Inverse: If not p , then not q .

Contrapositive: If not q , then not p .

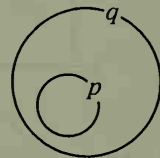
Example Write (a) the inverse and (b) the contrapositive of the true conditional: If two lines are not coplanar, then they do not intersect.

Solution a. Inverse: If two lines are coplanar, then they intersect. (False)

b. Contrapositive: If two lines intersect, then they are coplanar. (True)

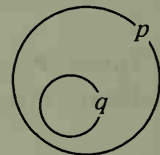
As you can see, the inverse of a true conditional is *not* necessarily true.

You can use a **Venn diagram** to represent a conditional. Since any point inside circle p is also inside circle q , this diagram represents “If p , then q .” Similarly, if a point is *not* inside circle q , then it *can't* be inside circle p . Therefore, the same diagram also represents “If not q , then not p .” Since the same diagram represents both a conditional and its contrapositive, these statements are either both true or both false. They are called **logically equivalent** statements.



Since a conditional and its contrapositive are logically equivalent, you may prove a conditional by proving its contrapositive. Sometimes this is easier, as you will see in Written Exercises 21 and 22.

The Venn diagram at the right represents both the converse “If q , then p ” and the inverse “If not p , then not q .” Therefore, the converse and the inverse of a conditional are also logically equivalent statements.



Summary of Related If-Then Statements

Given statement:	If p , then q .
Contrapositive:	If not q , then not p .
Converse:	If q , then p .
Inverse:	If not p , then not q .

A statement and its contrapositive are logically equivalent.

A statement is *not* logically equivalent to its converse or to its inverse.