

Answer all questions briefly and to the point. **Untidy answers will not be evaluated.** All necessary charts/tables will be provided. There are three parts- A, B and C. For ease of checking, please do not mix answers of one part with those of others.

PART A: Each question carries 1 mark.

Q1. In the context of hypothesis testing, what is a type I error?

Q2. What is the t_{critical} value with 10 degrees of freedom at 5% level of significance? Consider a situation of a one-tailed test.

Q3. The mean weight of a sample of 200 painkiller tablets manufactured in a pharmaceutical company is 50 mg with a standard deviation of 5 mg. Find the 95% confidence interval for the mean weight of the painkillers.

PART B: Each question carries two marks.

Q4. A multiple choice type question had four choices for an answer. A student either knows the answer with a probability of 0.3, or guesses by choosing an option at random. Given that the student answers the question correctly, what is the probability that the student guessed it.

Q5. The owner of a casino starts a game in which the player has to pay Rs 50 per game. The player is asked to toss an unfair coin [$p(H) = 0.25$] two times. If both show up heads then the owner gives the player Rs 200. Else, the player gets nothing. What is the average profit or loss made by the owner per game?

Q6. The cumulative distribution for a discrete random variable (X) is provided in the table below

X	0	1	2	3	4
CDF(X)	0.05	0.45	0.5	0.8	1

Find the expectation value Y, where $Y = 2X + 1$

$$E(Y) = E(2X+1) = 2E(X) + E(1) \\ = 2(1) + 1.$$

PART C: Each question carries 4 marks. Your responses should be accompanied by proper arguments and calculations.

Q7. Healthy mice (60-70 day old) have a distribution of serum uric acid which is approximately normal with a mean of 300 micromoles/liter. 9 mice of the same age group were treated with a drug for a period of 5 days and their serum uric acid levels were found to have a mean of 250 micromoles/litre with a standard deviation of 80 micromoles/litre.

a) Does the treatment significantly "reduce" the serum uric acid in the mice? Your answer should be supported by appropriate test statistic and its cutoff value. Consider that you would do the analysis at 5% level of significance.

b) What is the 95% confidence interval for the mean uric acid in drug treated mice?

Q8. Laboratory animals were administered with various concentrations of a drug (independent variable; X) and the activity of a serum enzyme (dependent variable, Y) was determined. The data is provided below. If the researcher chose to test a linear relationship between Y and X using simple linear regression, what would be the equation of the regression line?

Conc (μM)	0	1	2	3	4
Activity(units/ml)	42	38	29	17	10

Q9. Consider the following ANOVA table that was obtained after analysis of experimental data. In this experiment animals were divided into different groups and treated with three drugs to study the levels of a serum marker.

Source	Sum of Squares	df
Groups (Treatments)	665.2	2
Error	697.7	12

- How many observations are there in each group?
- Calculate the F-statistic.
- Is there any significant difference in the group means at 5% level of significance?

Q10. A researcher hypothesizes that it is possible to detect membrane proteins by looking at the fraction of the hydrophobic residues alone. To test this model, the researcher creates a library of 7500 proteins and scores each of them based on their fraction of hydrophobic residues and whether they are membrane proteins. The results are shown below.

	Majority hydrophobic	Majority hydrophilic
Membrane bound	2911	961
Cytosolic	713	2915

- A novel protein is identified. Majority of residues were found to be hydrophobic. What is the probability that this protein is cytosolic?
- If the researcher uses a Chi squared test to test whether there is any association between the content of hydrophobic residues and membrane localization, what would be the value of the Chi squared statistic?

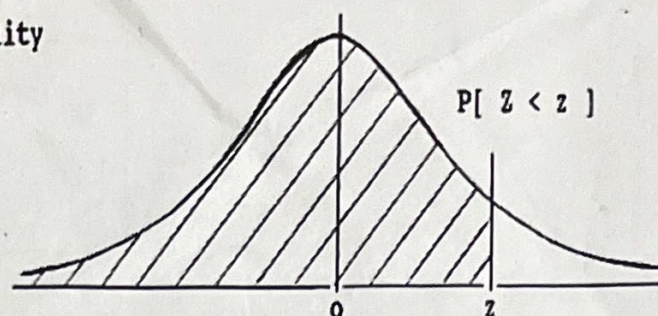
STANDARD STATISTICAL TABLES

1. Areas under the Normal Distribution

The table gives the cumulative probability up to the standardised normal value z

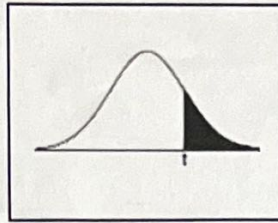
i.e.

$$P[Z < z] = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp(-\frac{1}{2}z^2) dz$$



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5159	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7854
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8804	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9773	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9865	0.9868	0.9871	0.9874	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
z	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
P	0.9986	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000

t-Distribution Table



The shaded area is equal to α for $t = t_{\alpha}$.

df	$t_{.100}$	$t_{.050}$	$t_{.025}$	$t_{.010}$	$t_{.005}$
1	3.078	6.314	12.706	31.821	63.657
2	1.886	2.920	4.303	6.965	9.925
3	1.638	2.353	3.182	4.541	5.841
4	1.533	2.132	2.776	3.747	4.604
5	1.476	2.015	2.571	3.365	4.032
6	1.440	1.943	2.447	3.143	3.707
7	1.415	1.895	2.365	2.998	3.499
8	1.397	1.860	2.306	2.896	3.355
9	1.383	1.833	2.262	2.821	3.250
10	1.372	1.812	2.228	2.764	3.169
11	1.363	1.796	2.201	2.718	3.106
12	1.356	1.782	2.179	2.681	3.055
13	1.350	1.771	2.160	2.650	3.012
14	1.345	1.761	2.145	2.624	2.977
15	1.341	1.753	2.131	2.602	2.947
16	1.337	1.746	2.120	2.583	2.921
17	1.333	1.740	2.110	2.567	2.898
18	1.330	1.734	2.101	2.552	2.878
19	1.328	1.729	2.093	2.539	2.861
20	1.325	1.725	2.086	2.528	2.845

Table showing critical values of F at 5% level of significance

Numerator df

Denominator df	1	2	3	4	5	6	7	8	9	10
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35