

BT209

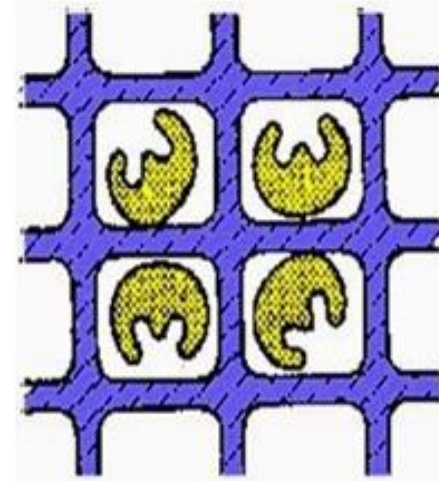
Bioreaction Engineering

12/04/2023

**Heterogeneous reaction:
immobilized enzyme , immobilized cell**

Heterogeneous reaction

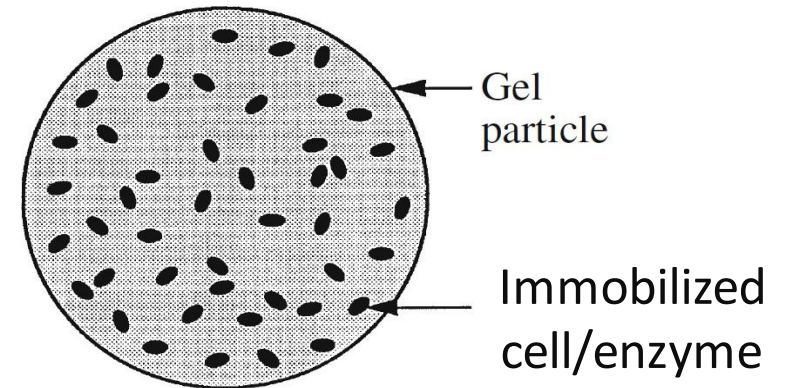
- ❑ Heterogeneous reactions occur in solid catalysts, not all reactive molecules are available for immediate conversion. Reaction takes place only after the reactants are transported to the site of reaction.
- ❑ Thus, mass transfer processes can have a considerable influence on the overall conversion rate.
- ❑ Reactions occurring in the presence of significant concentration or temperature gradients are called heterogeneous reactions.
- ❑ Here consider only concentration effect as biological reactions are not typically associated with large temperature gradients



entrapped in a matrix



encapsulate into
semipermeable membrane



Heterogeneous reaction in bioprocessing

□ Natural process

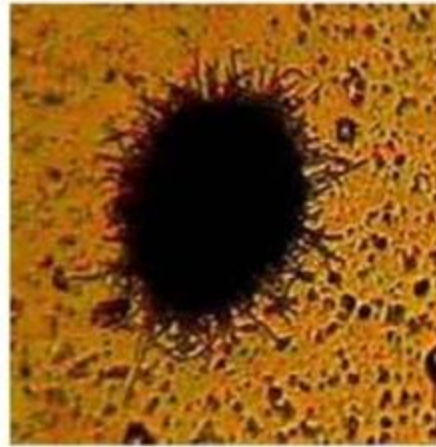
- Macroscopic flocs, clumps and pellets by certain filamentous bacteria and fungi
 - Mycelial pellets are common in antibiotic production



Free dispersed
mycelium cell



clump formation



Pellet formation

- Cells grow as biofilm on reactor walls
- Used in waste treatment process

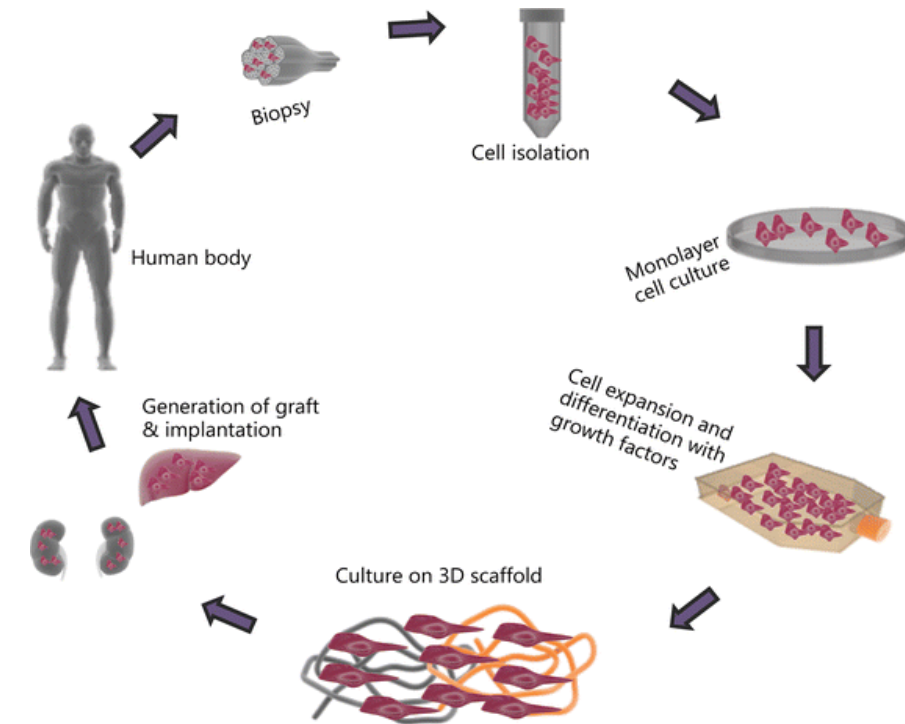


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❑ Natural process

- Plant cells tend to form aggregates in suspension culture and their growth results in the change in cell aggregate sizes
 - The aggregation of the plant cells can also stimulate the secondary metabolite production (therapeutic product)
- In tissue engineering animal cell are culture in a 3D scaffolds for surgical transplantation and organ repair

- ✓ Rate of reaction depends on the rate of reactant mass transfer outside and within the solid catalyst

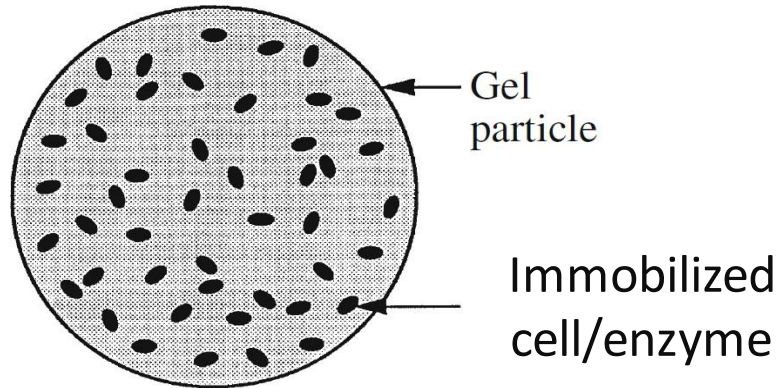


Artificial immobilization: Heterogeneous reaction in bio-processing

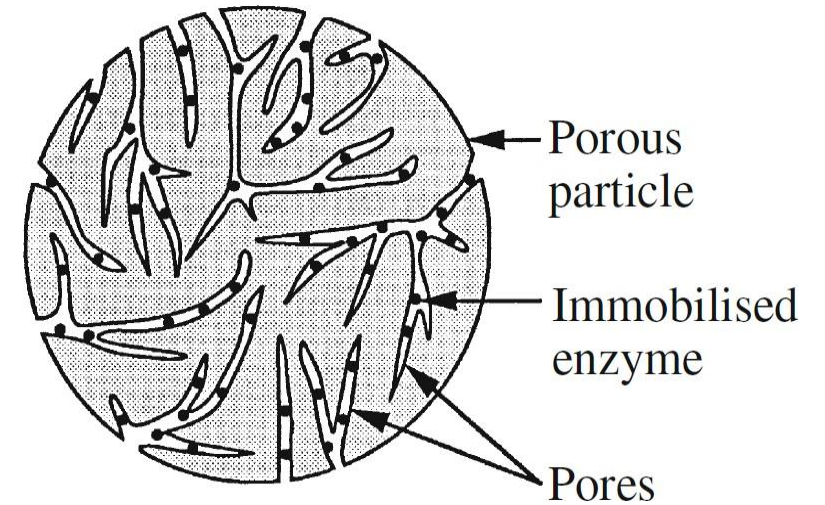
❑ Induced to heterogeneous system (artificial immobilization)

○ Cell/enzyme immobilization

➤ To reuse the enzyme or biocatalyst



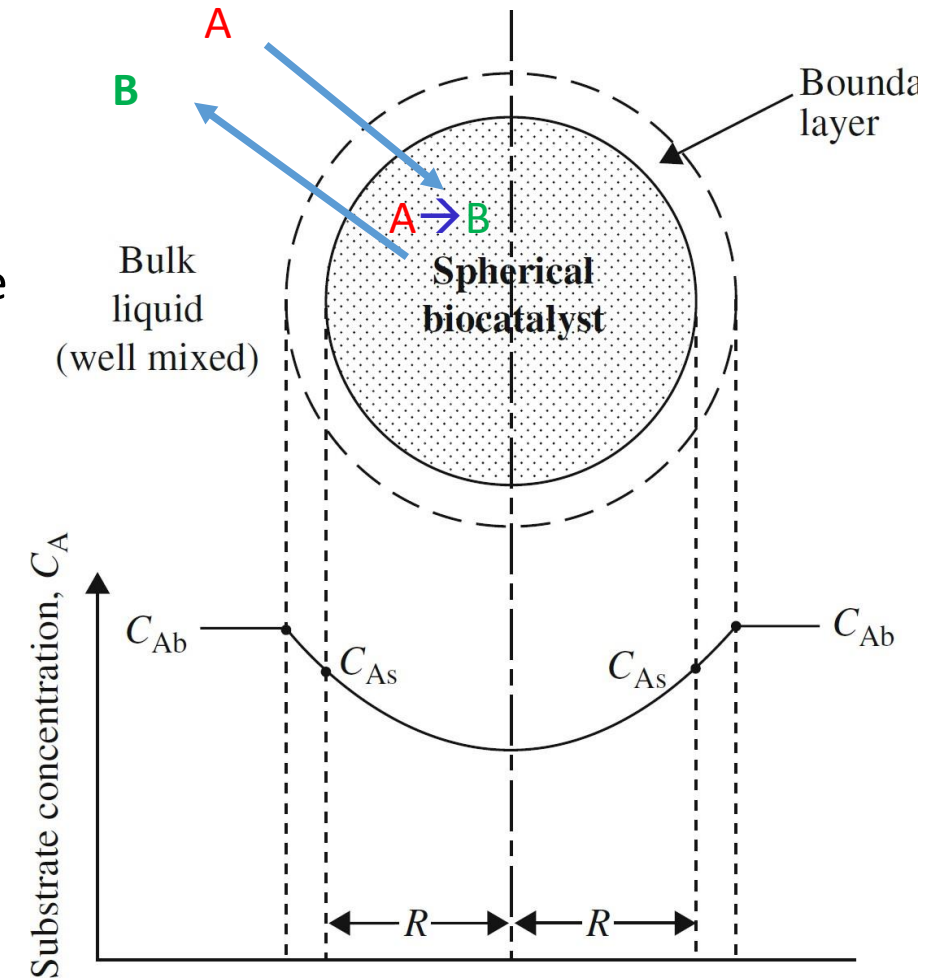
- Entrapment within **gel such** as alginate, agarose (crossed linked)
- ❑ Gel polymer must be porous and relatively soft to allow diffusion of reactants and products



- Entrapment **within porous solids** such as ceramics, porous glass, and resin bed
- ❑ Enzyme or cells migrate into the pores of these particles and attach to the internal beads (**Adsorption**)

Concentration gradient and reaction in solid catalyst

- ❑ A **spherical biocatalyst** immersed in **well mixed liquid** (contain substrate/**reactant A**)
- ❑ In **bulk** (away from particle) uniform concentration, C_{Ab}
- ❑ If **particle inactive** (no enzyme or cell), no consumption of A. the concentration of **substrate inside the solid would reach a constant value in equilibrium** with C_{Ab}
- ❑ If **active** (with enzyme/cell), C_A **decreases within the particle**.
- ❑ If **uniform distribution of enzyme or cell**, **symmetric concentration profile** with minimum at **centre**.
- ❑ Convective transport in bulk (NOT INSIDE SOLID)
- ❑ External diffusion through stagnant boundary layer (liquid film)
- ❑ Internal diffusion through internal pores



Cont.

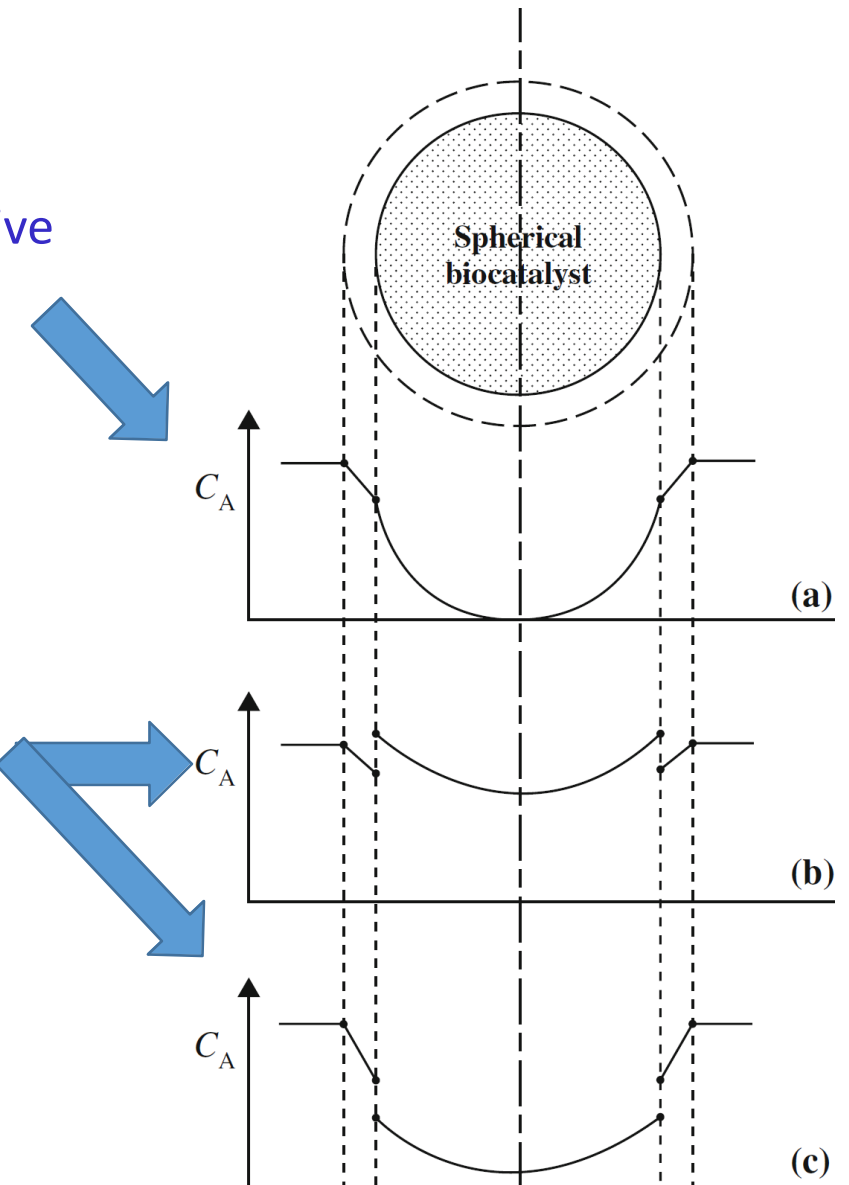
- ❑ If **mass transfer is much slower than** reaction:
 - all the substrate entering the particle may be consumed before reaching the center. The concentration falls zero within the particle and the core of particle become inactive

- ❑ **Partition coefficient** or **distribution coefficient is not equal to one**

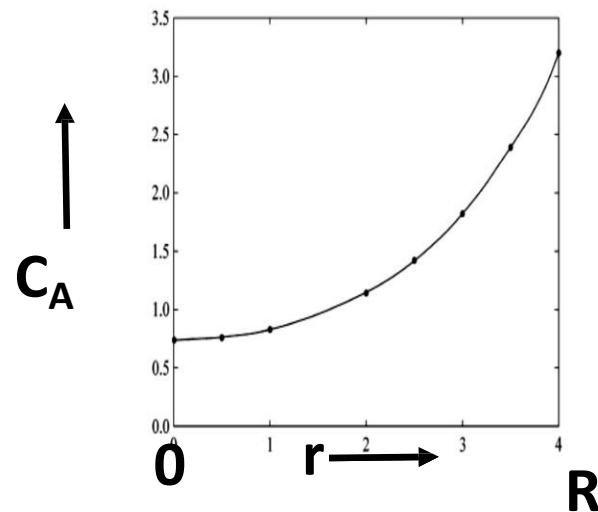
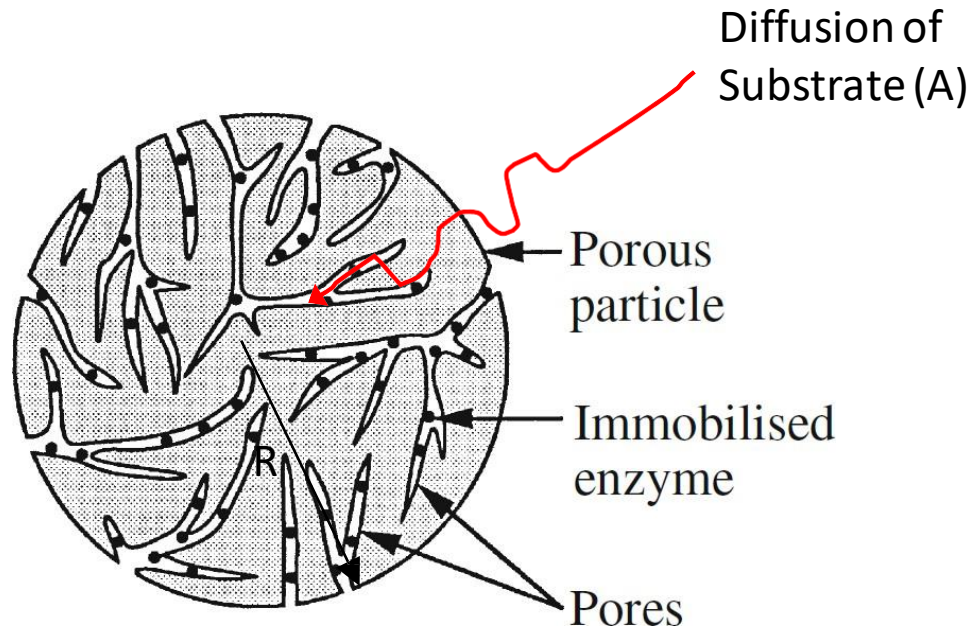
- at equilibrium and in the absence of reaction the concentration of A in the solid is higher or lower than in the liquid

- ❑ **Partitioning is important when A and solid are charged** or if strong hydrophobic interaction cause repulsion or attraction.

- ❑ Most materials used for immobilization are **very porous and contain high % water**, partition effect can be neglected



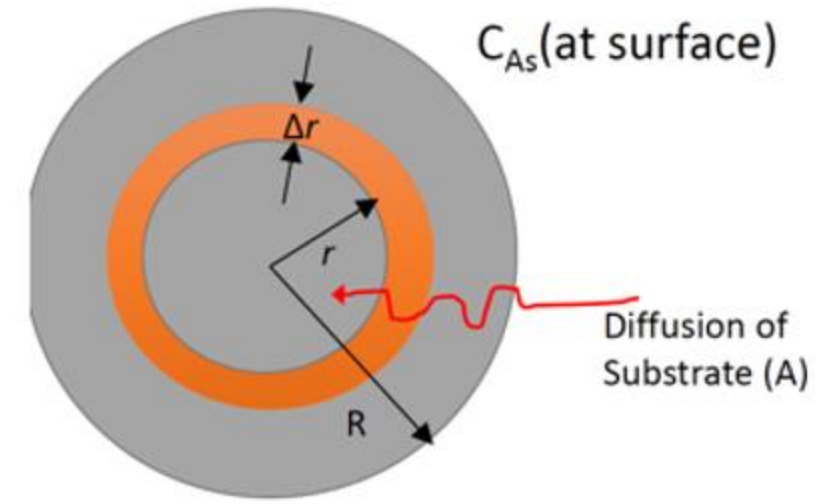
True and observed reaction rate



- Rate of reaction $= f(C_A, T)$
- Assume T (temperature) is not changing significantly here
- Rate of reaction depends on local C_A
- Normal rate expression can be used for **local rate of reaction (true reaction rate)** in each point) like homogeneous reaction
$$r_A = kC_A^n \qquad r_A = \frac{v_{max} C_A}{K_m + C_A}$$
- Very difficult to measure rate of reaction in each point (difficult to know local C_A)
- Measure overall reaction (observed) rate

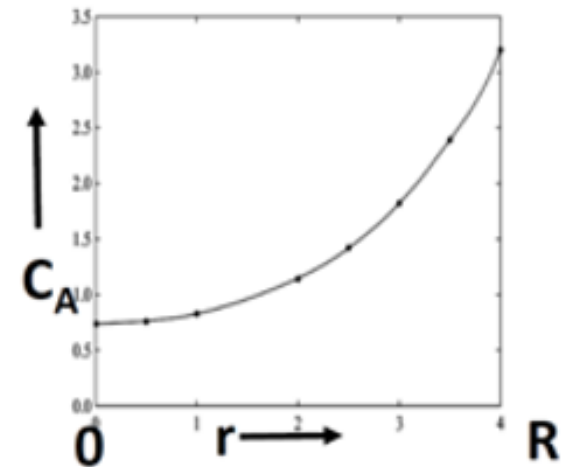
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- Concentration is changes across radius (r), $C_A=f(r)$
- Rate, $r_A=K f(C_A)$ is different in different radial position



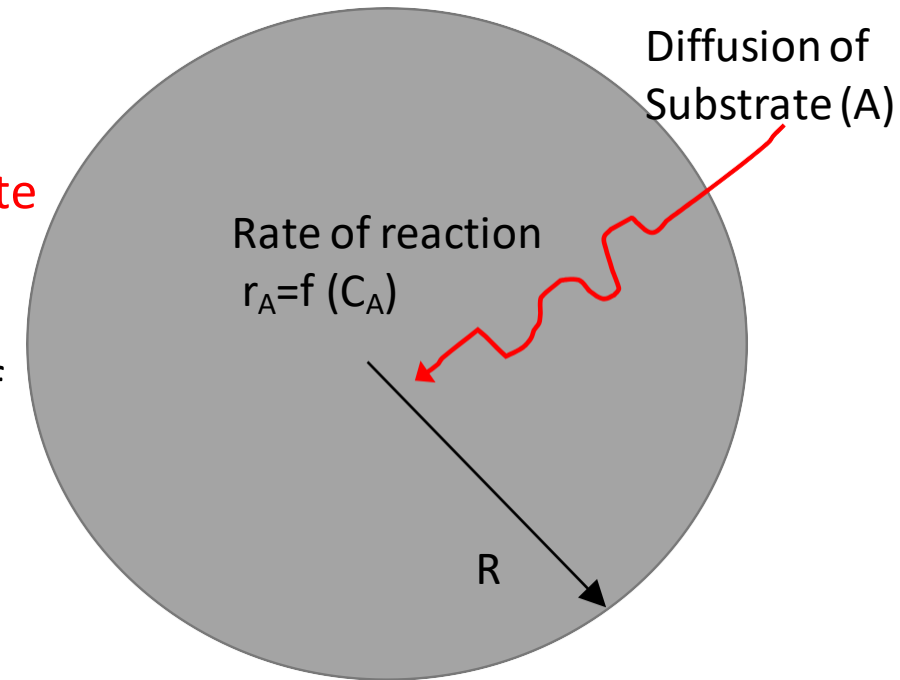
$$r_{A,obs} = \frac{4}{3}\pi R^3 \frac{\int_0^R r_A dV}{V - 0}$$

V: volume

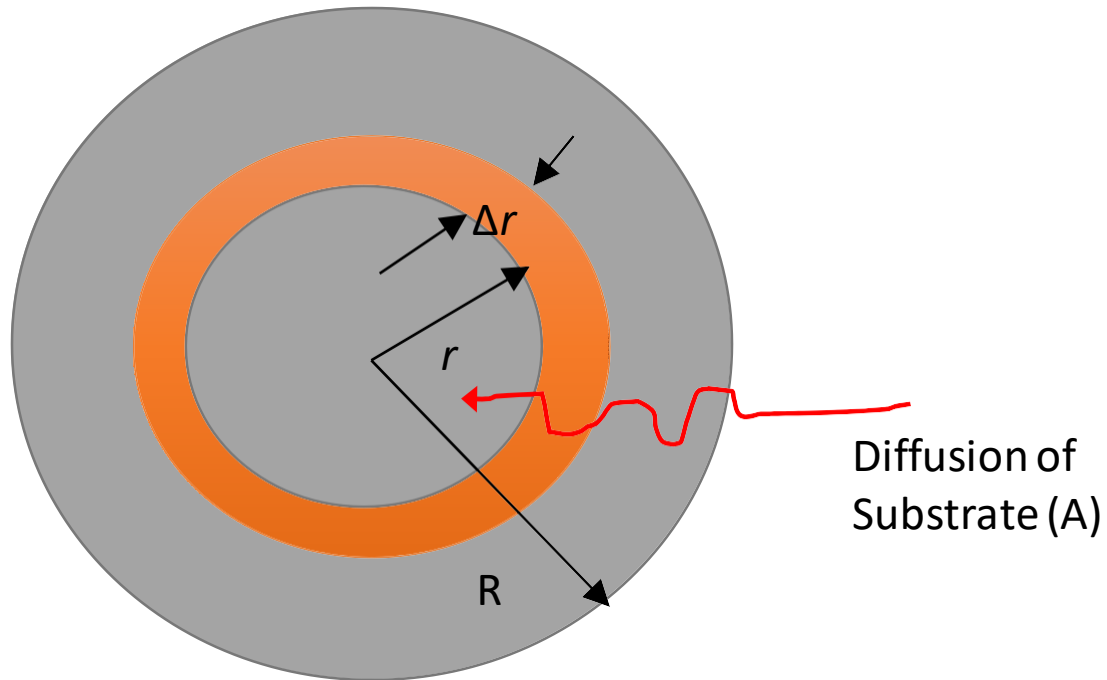


Internal mass transfer and reaction in heterogeneous systems

- ❑ Rates of reaction and substrate mass transfer are **not independent**
- ❑ The **rate of mass transfer depends on the concentration gradient** established in the system; this in **turn depends on** the rate of **substrate depletion by reaction**.
- ❑ On the other hand, the **rate of reaction depends** on the availability of **substrate**, which depends on the rate of mass transfer.
- ❑ Possible to **determine the relative influences** of mass transfer and reaction **on observed reaction** rates.
- ❑ If a **reaction proceeds slowly even in the presence of adequate substrate**, it is likely that mass transfer will be rapid enough to meet the demands of the reaction. In this case, the **observed rate would reflect more directly the reaction process** rather than mass transfer.
- ❑ Conversely, **if the reaction tends to be very rapid**, it is likely that **mass transfer will be too slow to supply substrate** at the rate required. The **observed rate would then reflect strongly the rate of mass transfer**.
- ❑ **Improving mass transfer and eliminating mass transfer restrictions** are desired objectives



Internal mass transfer and reaction



Assumption

- ✓ The particle is isothermal
- ✓ The particle is homogeneous
- ✓ Mass transfer occurs by diffusion only
- ✓ Diffusion can be described using Fick's law with constant effective diffusivity
- ✓ The substrate partition coefficient is unity
- ✓ The particle is at steady state

For a shell mass balance on substrate A

Rate of mass accumulation

= Rate of mass in - rate of mass out + rate mass of generation - rate of mass consumption

$$\left(\mathcal{D}_{Ae} \frac{dC_A}{dr} 4\pi r^2 \right) \Big|_{r+\Delta r} - \left(\mathcal{D}_{Ae} \frac{dC_A}{dr} 4\pi r^2 \right) \Big|_r + 0 - r_A 4\pi r^2 \Delta r = 0$$

\mathcal{D}_{Ae} is the effective diffusivity of substrate A in the particle

Internal mass transfer and reaction

$$\Rightarrow \left(\mathcal{D}_{Ae} \frac{dC_A}{dr} 4\pi r^2 \right) \Big|_{r+\Delta r} - \left(\mathcal{D}_{Ae} \frac{dC_A}{dr} 4\pi r^2 \right) \Big|_r + 0 - r_A 4\pi r^2 \Delta r$$

$$\Rightarrow \lim_{\Delta r \rightarrow 0} \frac{\left(\mathcal{D}_{Ae} \frac{dC_A}{dr} 4\pi r^2 \right) \Big|_{r+\Delta r} - \left(\mathcal{D}_{Ae} \frac{dC_A}{dr} 4\pi r^2 \right) \Big|_r}{\Delta r} - r_A r^2 = 0$$

$$\Rightarrow \frac{d}{dr} \left(r^2 \frac{dC_A}{dr} \right) - r_A r^2 = 0$$

$$\Rightarrow \mathcal{D}_{Ae} \left(\frac{d^2 C_A}{dr^2} r^2 + 2r \frac{dC_A}{dr} \right) - r_A r^2 = 0$$