$$F(x) = P(X \le x) = \sum_{t \le x} f(t)$$
, for $-\infty < x < \infty$

$$P(a \le X \le b) = F(b) - F(a)$$

$$F(x) = P(X \le x) = \int_{-\infty}^{x} f(t) dt$$
, for $-\infty < x < \infty$

$$\mu = E(X) = \sum_{x} xf(x)$$

$$\mu = \mathbf{E}(\mathbf{X}) = \int_{-\infty}^{\infty} \mathbf{x} \mathbf{f}(\mathbf{x}) \, d\mathbf{x}$$

$$f(x, y) \ge 0$$
 for all (x, y)

$$\sum_{x}\sum_{y}f(x,y)=\mathbf{1}$$

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) \, dx \, dy = 1$$

$$g(x) = \sum_{y} f(x, y)$$

$$\mathbf{h}(\mathbf{y}) = \sum_{x} f(x, y)$$

$$\mathbf{g}(\mathbf{x}) = \int_{y=-\infty}^{\infty} f(x, y) d\mathbf{y}$$

$$h(y) = \int_{x = -\infty}^{\infty} f(x, y) dx$$

$$P(X = x, Y = y) = P(X = x) \times P(Y = y)$$

$$f(x, y) = f(x)_X \times f(y)_Y$$

$$f(x, y) = g(x)h(y)$$

$$f(y|x) = \frac{P(X = x, Y = y)}{P(X = x)}$$

or

$$f(y|x) = \frac{f(x, y)}{g(x)}$$

$$P(X = x, Y = y) = P(X = x) \times P(Y = y)$$

$$f(x, y) = f(x)_X \times f(y)_Y$$

$$\mu_g(X,Y) = E[g(X,Y)] = \sum_x \sum_y g(x,y)f(x,y)$$

$$\mu_g(X,Y) = E[g(X,Y)] = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} g(x,y) f(x,y) dx dy$$

$$E(Y|X) = \int_{y=-\infty}^{y=+\infty} y f(y|x) dy$$

$$E(X|Y) = \int_{x=-\infty}^{x=+\infty} x f(x|y) dx$$

$$E(Y) = \sum_{y} \sum_{x} y f(x, y) = \sum_{y} y h(y)$$

$$E(Y) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} yf(x, y) dx dy = \int_{-\infty}^{+\infty} yh(y)$$

$$E(X) = \sum_{x} \sum_{y} xf(x, y) = \sum_{x} xg(x)$$

$$E(X) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} xf(x, y) dx dy = \int_{-\infty}^{+\infty} xg(x)$$

$$E(X) = \sum_{x} \sum_{y} x f(x, y) = \sum_{x} x g(x)$$

$$E(X) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} x f(x, y) dx dy = \int_{-\infty}^{+\infty} x g(x)$$

$$E(Y) = \sum_{y} \sum_{x} y f(x, y) = \sum_{y} y h(y)$$

$$E(Y) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} x f(x, y) dx dy = \int_{-\infty}^{+\infty} y h(y)$$

$$\mu_{\mathbf{g}}(\mathbf{X}) = \mathbf{E}[\mathbf{g}(\mathbf{X})] = \sum_{x} g(x) f(x)$$

$$\mu_{\mathbf{g}}(\mathbf{X}) = \mathbf{E}[\mathbf{g}(\mathbf{X})] = \int_{-\infty}^{+\infty} \mathbf{g}(\mathbf{x}) f(\mathbf{x})$$

$$\sigma^2 = \mathbf{E}[(\mathbf{X} - \boldsymbol{\mu})^2] = \boldsymbol{\Sigma} (\mathbf{x} - \boldsymbol{\mu})^2 \mathbf{f}(\mathbf{x})$$

$$\sigma^2 = E[(X - \mu)^2] = \int_{y - -\infty}^{x = +\infty} (x - \mu)^2 f(x) dx$$

$$\sigma^2 = E(X^2) - \mu^2 \text{ or } \sigma^2 = E(X^2) - \{E(X)\}^2$$

$$\begin{split} \sigma_{XY} &= \mathbf{E} \left[(\mathbf{X} - \mu_X)(\mathbf{Y} - \mu_Y) \right] \\ &= \sum_x \sum_y (\mathbf{x} - \mu_X)(\mathbf{y} - \mu_Y) \ \mathbf{f}(\mathbf{x}, \mathbf{y}) \end{split}$$

$$\sigma_{XY} = \mathbf{E}[(\mathbf{X} - \mu_X)(\mathbf{Y} - \mu_Y)]$$

=
$$\int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} (\mathbf{x} - \mu_X)(\mathbf{y} - \mu_Y) \mathbf{f}(\mathbf{x}, \mathbf{y}) d\mathbf{x} d\mathbf{y}$$

$$\sigma_{XY} = E(XY) - \mu_x \mu_Y$$

$$SST = \sum_{i=1}^{k} \sum_{j=1}^{n} (y_{ij} - \bar{y}_{i..})^2$$

$$SSA = n \sum_{i=1}^{k} (\overline{y}_{i,-} \overline{y}_{i,-})^2$$

$$SSE = \sum_{i=1}^{k} \sum_{i=1}^{n} (y_{ii} - \bar{y}_{i})^{2}$$

$$s_1^2 = \frac{SSA}{k-1}$$

$$s^2 = \frac{\text{SSE}}{k(n-1)}$$

$$f_{cal} = \frac{s_1^2}{s_2^2}$$

$$f_{tab} = f_a[k-1, k(n-1)]$$

$$r = \frac{n(\sum xy) - (\sum x)\left(\sum y\right)}{\sqrt{n(\sum x^2) - (\sum x)^2} \sqrt{n(\sum y^2) - (\sum y)^2}}$$

$$t_{cal} = \frac{r}{\sqrt{\frac{1-r^2}{r-2}}}$$

$$\hat{y} = b_0 + b_1 x$$

$$\mathbf{b_1} = \frac{\mathbf{n}(\sum xy) - (\sum x)(\sum y)}{\mathbf{n}(\sum x^2) - (\sum x)^2}$$

$$\mathbf{b_0} = \overline{\mathbf{y}} - \mathbf{b_1} \overline{\mathbf{x}}$$

$$\mathbf{b_0} = \frac{(\sum y)(\sum x^2) - (\sum x)(\sum xy)}{\mathrm{n}(\sum x^2) - (\sum x)^2}$$

$$t_{cal} = \frac{\overline{d} - \mu_d}{\frac{s_d}{\sqrt{n}}}$$