Plots for Assignment 2

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Question 1

All plots are for the exoplanet V830~Tau~b. The parameters used are $K_* = 75.0~\text{m/s}$, a = 0.057~AU, $t_p = 0.0$, P = 4.93~days. The true anomaly was calculated from the eccentric and mean anomalies by solving Kepler's equation iteratively. The plots are as below:

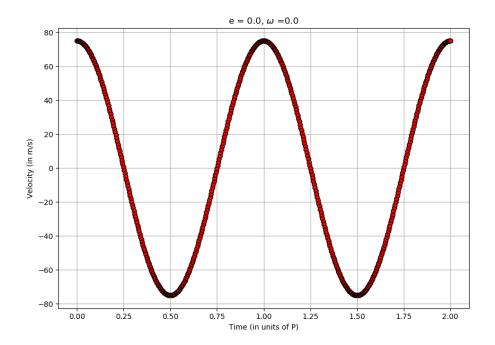


Figure 1: Plot of radial velocity curve for $e=0.0,\,\omega=0.0$

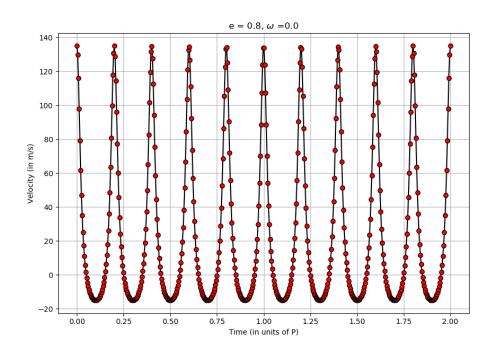


Figure 2: Plot of radial velocity curve for e = 0.8, $\omega = 0.0$

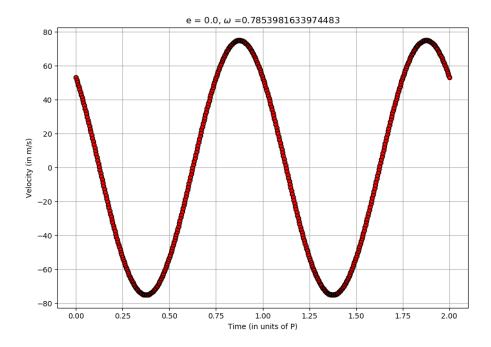


Figure 3: Plot of radial velocity curve for e = 0.0, $\omega = 45^{\circ}$

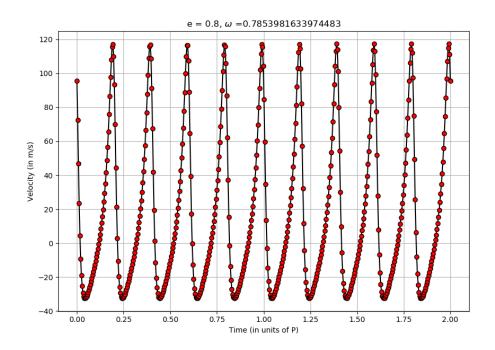


Figure 4: Plot of radial velocity curve for e = 0.8, $\omega = 45^{\circ}$

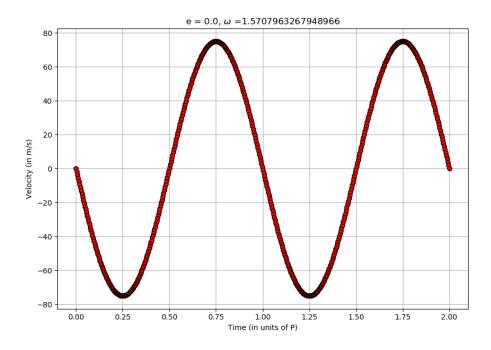


Figure 5: Plot of radial velocity curve for e = 0.0, $\omega = 90^{\circ}$

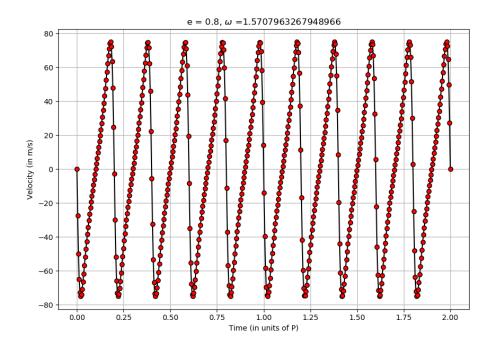


Figure 6: Plot of radial velocity curve for e = 0.8, $\omega = 90^{\circ}$

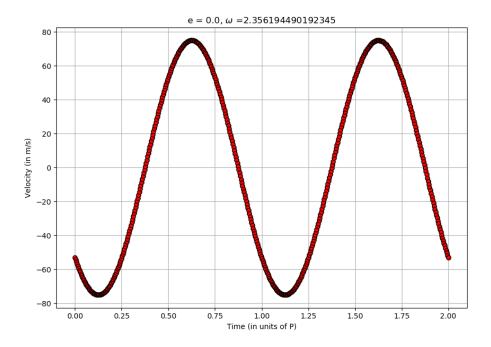


Figure 7: Plot of radial velocity curve for e = 0.0, $\omega = 135^\circ$

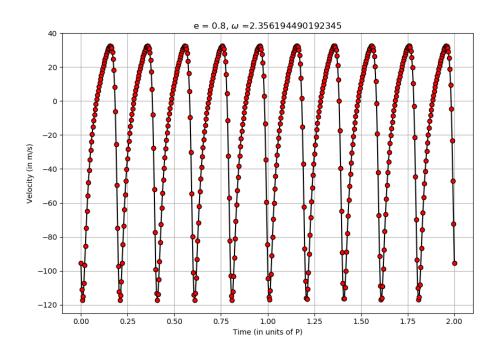


Figure 8: Plot of radial velocity curve for e = 0.8, $\omega = 135^\circ$

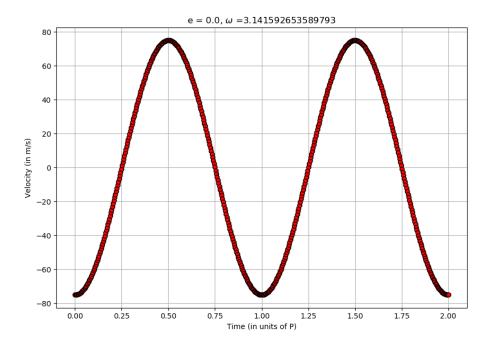


Figure 9: Plot of radial velocity curve for e = 0.0, $\omega = 180^{\circ}$

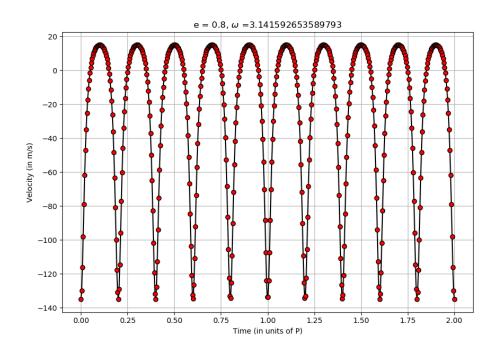


Figure 10: Plot of radial velocity curve for e = 0.8, $\omega = 180^{\circ}$

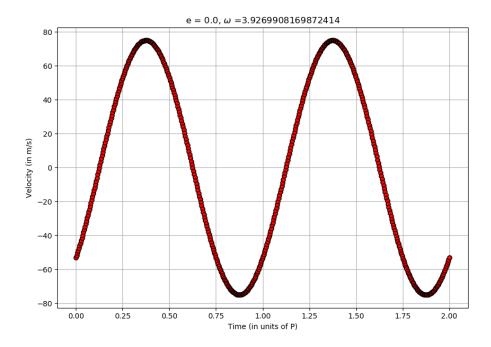


Figure 11: Plot of radial velocity curve for e = 0.0, $\omega = 225^{\circ}$

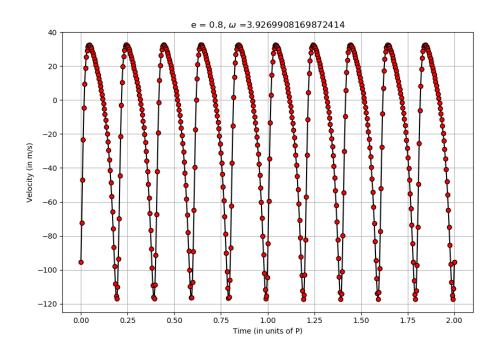


Figure 12: Plot of radial velocity curve for e = 0.8, $\omega = 225^\circ$

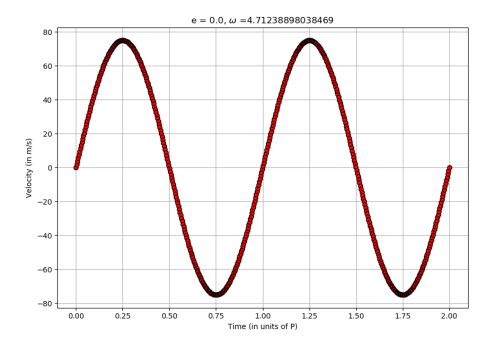


Figure 13: Plot of radial velocity curve for e = 0.0, $\omega = 270^{\circ}$

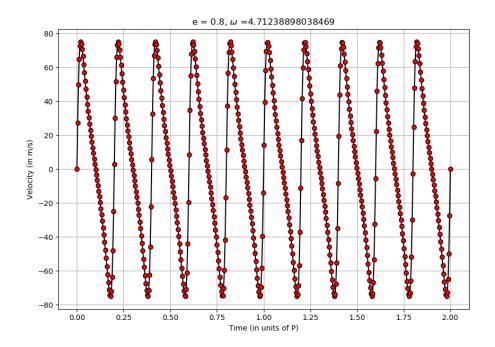


Figure 14: Plot of radial velocity curve for e = 0.8, $\omega = 270^{\circ}$

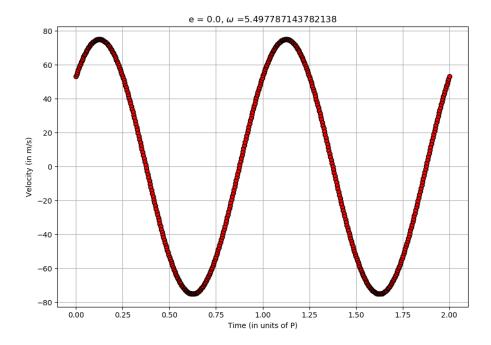


Figure 15: Plot of radial velocity curve for e = 0.0, $\omega=315^\circ$

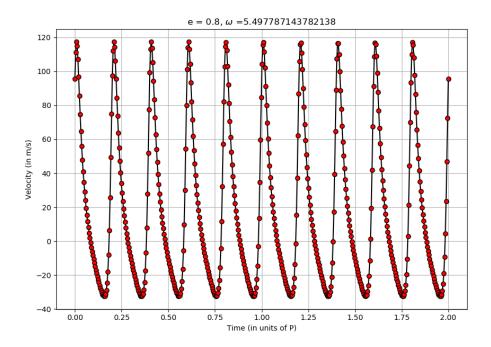


Figure 16: Plot of radial velocity curve for e = 0.8, $\omega = 315^{\circ}$

As seen from [1] and [2], the radial velocity of the actual exoplanet V830 Tau b corresponds to an eccentricity of 0.0, upon filtering. This agrees with the value given in the Exoplanet database, and also the behaviour as seen in the plots above.

Question 2

The plots are as given below. In the plots, the angle $i_{min} = \arccos\left(\frac{R_{star} + R_{planet}}{a}\right)$

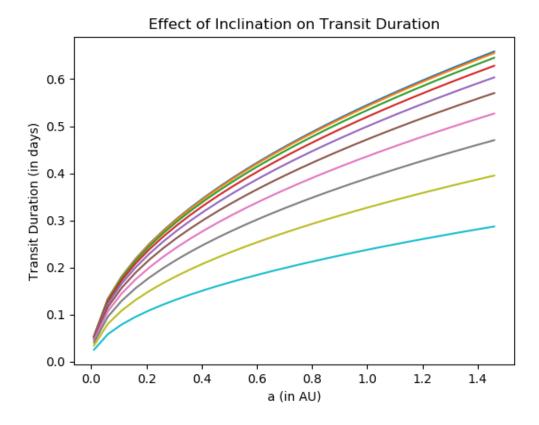


Figure 17: Variation of Transit Duration with the semi-major axis, for an Earth-sized planet around a Sun-type star. Note that the inclination, for a given a, varies from i_{min} to 90° , along increasing y.

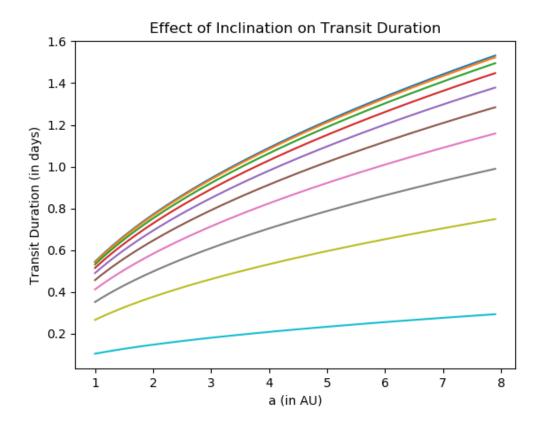


Figure 18: Variation of Transit Duration with the semi-major axis, for an Jupiter-sized planet around a Sun-type star. Note that the inclination, for a given a, varies from i_{min} to 90°, along increasing y.

We see that the curves for the Earth-sized planet around a Sun-type star bunch together at smaller semi-major axis values, and thus determining the inclination is tougher. This is not the case for the Jupiter-sized planet around a Sun-type star. Further, as expected, the largest transit durations are obtained for inclinations close to 90 deg, and the maximum possible transit duration (given best inclination, semi-major axis etc.) increases when the mass of the planet increases. Hence, finding Jupiter-sized planets via the transit method is easier than as compared to Earth-sized planets around a similar Sun-type star.

References

- Donati, J.-F., et al. "The Hot Jupiter of the Magnetically Active Weak-Line T Tauri Star V830 Tau." Monthly Notices of the Royal Astronomical Society, vol. 465, no. 3, 10 Nov. 2016, pp. 3343–3360, 10.1093/mnras/stw2904. Accessed 20 Sept. 2019.
- Donati, J. F., et al. "A Hot Jupiter Orbiting a 2-Million-Year-Old Solar-Mass T Tauri Star." Nature, vol. 534, no. 7609, June 2016, pp. 662–666, 10.1038/nature18305. Accessed 20 Sept. 2019.