

Research Note

Bermudan Swaptions – A Relative Value Framework

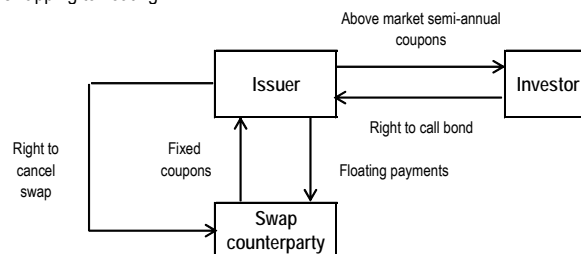
- Bermudan swaptions are very easy to describe, less easy to understand intuitively, and very hard to analyze—a relative value metric to answer the basic question of whether a Bermudan swaption is rich or cheap has been elusive
- A good relative value framework should not only provide a summary measure of richness/cheapness, but also provide an understanding of the sources of value, and be monetizable. In particular, any framework should specify exposures to correlations and implied vol curves in a hedge-able way
- In this paper, we develop such a framework. Our approach relies on the observation that Canary swaptions are the simplest structures that are complex enough to provide stable approximations to a Bermudan swaption. Since Canaries have exactly 2 exercise dates, they are specified by vanilla swaption implied volatilities and one implied correlation. This can be useful in the risk-management of Bermudan swaptions and in monetizing relative value
- A report based on the framework outlined in this paper may be found in the daily analytics packages on Morganmarkets

Introduction¹

Bermudan swaptions are relatively simple to describe, but can be quite difficult to analyze from a relative value standpoint. Quite simply, a Bermudan receiver (payer) swaption is an option that gives the owner the right—but not the obligation—to receive (pay) fixed at a pre-determined rate (the strike) in a swap to a given final maturity, with the option being exercisable once at any one of a given set of dates prior to the final maturity of the swap. This is in contrast to European swaptions, which can only be exercised on

Exhibit 1: Investor demand for the higher coupons that characterize callable bonds can spur issuance of such structures, which are often swapped to yield a lower synthetic funding rate for the issuer

A schematic illustrating the flows involved in issuing callable bonds and swapping to floating



a single exercise date. At the other extreme, an option that can be exercised at any point before the predetermined final maturity of the swap would be an American swaption.

The Bermudan as well as American swaptions markets are closely linked to the callable bond market. Investors frequently are willing to absorb reinvestment risk in search of higher current yield—i.e., they are willing to earn an above-market coupon for some minimum period of time that is less than their target investment horizon, in exchange for possibly being forced to accept lower reinvestment rates in the future. In other words, these investors are willing to own bonds with an embedded short call position, providing a higher coupon until the bond is called; should the bond be called, however, reinvestment rates will be lower by definition.

To accommodate this desire for higher current yield, issuers often find it attractive to issue callable bonds, even if they would prefer to have—say—floating rate liabilities without any call features. For instance, such an issuer might issue a Bermudan-style callable bond (typically callable on any coupon date) with a higher

Srini Ramaswamy^{AC}
(1-212) 834-4573
srini.ramaswamy@jpmorgan.com
J.P. Morgan Securities LLC

Alberto Iglesias
(1-212) 834-5116
alberto.d.iglesias@jpmorgan.com
J.P. Morgan Securities LLC

Praveen Korapaty
(1-212) 834-3092
praveen.korapaty@jpmorgan.com
J.P. Morgan Securities LLC

¹ The authors gratefully acknowledge the contributions of their colleagues Hui Fang and Feng Deng to this research.

Srinivas Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

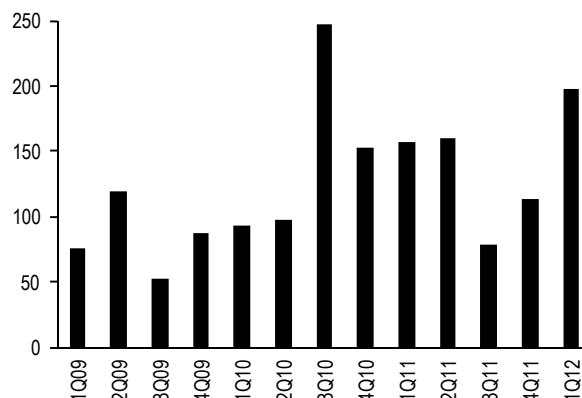
coupon, and then enter into a cancellable swap with a dealer. Effectively, the issuer would be selling the embedded call to the dealer and switching their liability into a synthetic floating rate note. Such a transaction is likely to occur when investor demand for callables is strong, allowing the issuer to synthetically obtain better funding costs through the callable market than might be possible directly. A schematic outlining this is shown in **Exhibit 1**.

One consequence of such transactions is that dealer desks are left warehousing long vol (often Bermudan) positions. Indeed, this is a key source of vol supply to swaption dealers; as seen in **Exhibit 2**, gross issuance of callables can be significant over time. Such issuance is also frequently in Bermudan or American form, given the greater yield enhancement possible by selling embedded calls with more than one exercise date. Thus, dealer desks tend to structurally warehouse long Bermudan swaptions positions, which are risk-managed using the more liquid European swaptions market.

This type of market structure makes it likely that Bermudan swaptions will offer a cheaper (albeit less liquid) source of interest rate optionality for investors needing structural hedges such as MBS portfolio hedgers. Indeed, the risk characteristics of Bermudan receiver swaptions (as opposed to European swaptions) are likely to be a better match for the risk characteristics of MBS, given that the embedded prepayment option is American in nature, and a properly structured Bermudan or American style swaption should represent a more stable hedge for MBS across a broader range of market environments. Despite these advantages, European swaptions remain by far the preferred hedging instrument. This is likely driven by three main factors. First, Bermudan swaptions are less liquid than their European-style counterparts. Second, Bermudan swaptions are more complex instruments and are simply less well understood. Third, and on a somewhat related note, a simple metric that quantifies the relative value in Bermudan swaptions versus European swaptions in a monetizable way has proven elusive. While investors can of course use a well-calibrated Bermudan pricing model to determine the fair price of an instrument and compare it to the market price, this is not a satisfactory way to assess mispricings in Bermudan swaptions. A good relative value framework for Bermudan

Exhibit 2: Issuance of swapped callables is a key source of vol supply

Quarterly vega supply from zero coupon callable issuance;
\$mn per 1 bp/day move in implied vol



swaptions should do more than merely deliver a rich/cheap number. It should:

- Be **decomposable** into its constituent parts. I.e., where does the mispricing come from? How much of the mispricing is idiosyncratic to the Bermudan swaptions market? How much reflects other market variables, such as mispriced implied vol curves or correlations?
- Be **monetizable**. Relative to European swaptions, Bermudans result in additional exposure to numerous other market variables, such as implied vol curves and implied correlations. Only a portion of the aggregate richness/cheapness of a Bermudan swaption is idiosyncratic to the instrument itself; some portion of it will derive from views on the mispricing of these market variables themselves. However, an investor might not wish to buy a “cheap” Bermudan swaption if most of its cheapness derives from a view on the implied vol curve, for instance, since vol curve views are more easily expressed via European swaptions. Thus, a proper relative value framework should allow an investor to determine the proper vol curve and correlation hedges, if those risks are deemed undesirable.

Finally, a useful metric of relative value should be demonstrably successful as a trading signal.

In previous research, we have attempted to make Bermudan swaptions easier to understand via

Srini Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

European-swaption-based approximations (see *Introduction to Bermudan Swaptions and a Framework for Analysis*, J.P.Morgan Derivatives Strategy Research Note, 7/1/2003). In that paper, we built on some fairly simple observations to develop intuition regarding Bermudans. Specifically, we noted that each Bermudan swaption (say, a 1Yx10Y receiver struck at 3%, exercisable semiannually after the first exercise date) may be thought of as spanning a basket of European swaptions (including the 1Yx10Y, the 1Y6Mx9Y6M, the 2Yx9Y, and so on, with all these European swaptions also being receivers struck at 3%). Depending on the current optimal exercise date of the Bermudan swaption, it would most closely resemble one of these European swaptions. It is also straightforward that the Bermudan swaption's premium must be at least as much as the highest premium of all the swaptions in this basket. Moreover, the European swaption in the basket with the highest premium may be thought of as the locally best European approximation to the more complex Bermudan swaption. Inspired by the analogy with the Treasury futures market, we call this European swaption as the CTD (even though the term "cheapest" is of course incorrect in this context). And much like the CTD into a Treasury futures contract can change as market conditions change, so too can the CTD for a Bermudan swaption. For instance, in a sharp rally, a 1Yx10Y Bermudan receiver swaption's CTD would likely become the 1Yx10Y European swaption as the Bermudan becomes highly exercisable at the earliest possible date. In contrast, as rates rise and near-term exercise becomes less rewarding, the CTD would shift towards longer expiries, perhaps the 5Yx6Y.

This analogy with futures baskets allows an investor to develop some intuition regarding Bermudans. However, it doesn't easily translate into a relative value metric, because the European swaption CTD is generally not stable enough to use the "basis" between the Bermudan swaption and its CTD as a relative value metric. We also considered a slightly modified approach to developing a relative value metric in our earlier research, based upon the basis between a Bermudan swaption and a "replicating portfolio" of spanned European swaptions from its basket. While more stable than a single CTD based approach, replicating portfolios proved not to be stable enough to translate into a meaningful relative value metric.

This, then, is the objective of this research note—to develop a simple relative value metric for Bermudan swaptions, and test its effectiveness in a trading strategy using Bermudan swaptions versus European swaptions. To do this, we build on the basic ideas explored in our earlier research, but extend them in a slightly different direction. Specifically, rather than attempting to replicate Bermudans with a portfolio of European swaptions, we instead seek to find a "Canary" or a 2-exercise swaption that best approximates a given Bermudan. Put simply, if our earlier research was based on finding each Bermudan swaption's European CTD, this paper explores the usefulness of considering each Bermudan swaption's Canary CTD. We demonstrate that a Bermudan swaption's Canary CTD is stable enough for it to serve as an approximation of the Bermudan itself; in addition, it is also simple enough to analyze, given that Canary pricing is determined by vanilla swaption implied volatilities and one implied correlation. In the rest of this paper, we develop a monetizable metric of relative value that builds on this observation.

Bermudan swaptions as a basket of Canary swaptions

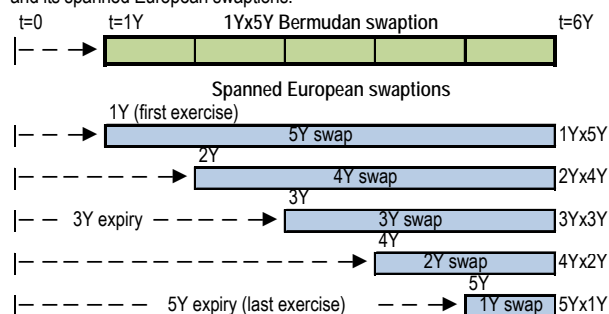
A Canary swaption is simply a Bermudan with exactly two possible exercise dates; in other words, it is the simplest possible Bermudan-style option that is not "too simple" (i.e., a European swaption). Albert Einstein famously said that everything must be made "as simple as possible, but not simpler". In our context, it turns out that approximating Bermudans with European swaptions is too simple to be useful; Canary-based approximations, on the other hand, strike the right balance between simplicity and usefulness.

We introduce the following notation for Canary swaptions: by a 1Y(4Y)x10y Canary we mean a 1Yx10Y European with an additional exercise possibility 4 years from now, with the final maturity of the underlying swap being 11 years from now, regardless of when the option is exercised. Similar to the description of Bermudans in terms of their European basket, Bermudans can also be thought of as baskets of Canary swaptions with a single exercise. For example, a 1Yx5Y Bermudan, with annual exercise dates (for the sake of simplicity in illustration) after the first exercise date at the 1y point, can be thought of as spanning a basket of 5 Europeans with exercises 1 year

Srini Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

Exhibit 3: A Bermudan swaption may be thought of as spanning numerous European swaptions, corresponding to each of the various possible exercise dates

Graphic representation of a 1Yx5Y Bermudan swaption with annual exercise points, and its spanned European swaptions.



from now (to enter into a 5 year swap), 2 years from now (to enter into a 4 year swap) and so on (see illustration in **Exhibit 3**).

It is straightforward to generalize this idea, and to think of a Bermudan swaption as spanning a set of Canary swaptions. Specifically, the same Bermudan mentioned earlier can also be thought of as spanning a basket of 10 Canary swaptions (one for each possible pair of allowable exercise dates). These possibilities are enumerated for the above example of a 1x5 Bermudan with annual exercise in **Exhibit 4**.

For each Canary swaption spanned by a Bermudan, we can also define the Bermudan/Canary or BC basis as the premium of the Bermudan minus the Canary's premium. The highest-premium Canary in the basket (that is, the "CTD" in our terminology), therefore, has the smallest basis in the basket.

The real value in analyzing Bermudans by using their Canary baskets stems from the greater stability of the Canary CTD. As seen in **Exhibit 5**, the Canary CTD's BC basis is not only narrower (in comparison to the BE basis of the European CTD), but also much more stable across different rate regimes. In addition, Canaries also mirror the risk characteristics of a Bermudan swaption more closely than European swaptions. In order to match the risk profile of a Bermudan swaption using Europeans alone, typically two-to-three or more are needed, and the replicating portfolio is typically only stable under a narrow range of market moves. For example, a 1Yx5Y Bermudan receiver might combine the risk characteristics of a 1Yx5Y European receiver in a rally and a 2.5Yx3.5Y European in a selloff

Exhibit 4: It is straightforward to generalize this idea and to think of Bermudans as spanning a set of Canary swaptions

Graphic representation of a 1Yx5Y Bermudan with annual exercise points, and its 10 spanned Canary swaptions

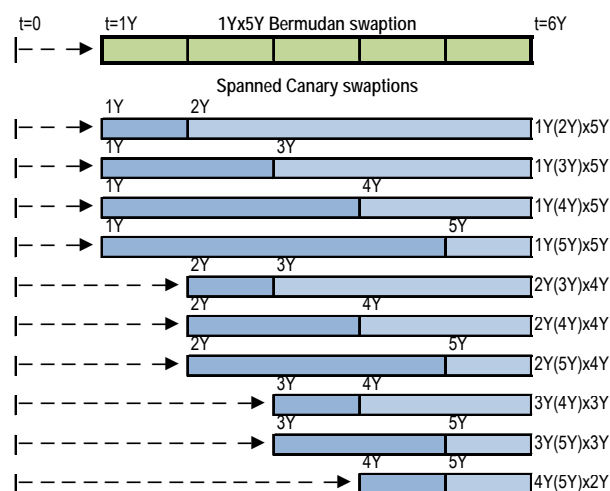
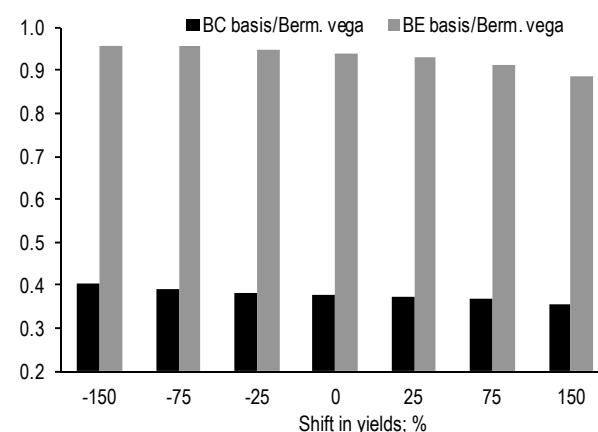


Exhibit 5: The BC basis is consistently narrower than the BE basis under different yield scenarios

1Yx5Y ATM receiver Bermudan/Canary basis and Bermudan/European basis for the CTD divided by the Bermudan vega* for various parallel shifts of the yield curve**, %



* Bermudan vega in bp of notional per bp shift in daily vol.

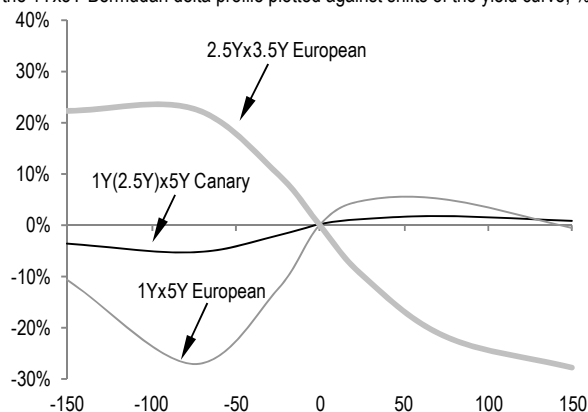
** COB 5/22/2012

(**Exhibits 6 & 7**). Over the same scenarios, a single Canary swaption (the CTD, in fact) provides a better match than any of the individual Europeans. Intuitively, this result is not surprising. Under most circumstances the Bermudan may either be exercised early on or somewhere near the midpoint of the exercise period. Exercising much closer to the final

Srinivas Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

Exhibit 6: The Canary CTD mimics its parent's risk characteristics better than individual European counterparts, as seen in the deviation profiles for delta ...

Deviation of the delta profile of selected European and Canary swaptions from the 1Yx5Y Bermudan delta profile plotted against shifts of the yield curve; %



The delta profile is obtained as a % of the original delta (that is, for no change in the yield curve). Each curve is obtained by subtracting the European or Canary delta profile from the Bermudan delta profile. The 1Y(2.5Y)x5Y Canary and the 1Yx5Y European are the CTDs. COB 5/22/2012

maturity of the option tends not to be advantageous due to the lower annuity factors of the residual swap.

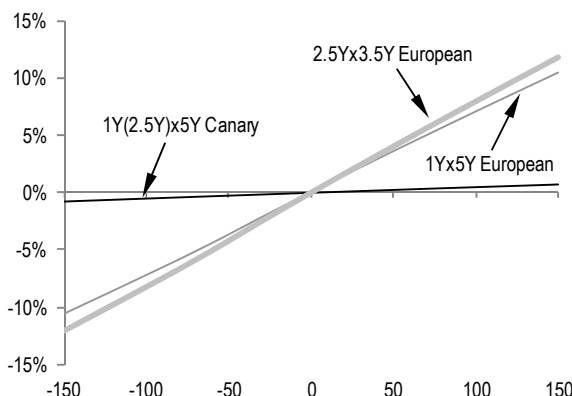
Thus, a Bermudan swaption's Canary CTD is in fact likely to be a very good approximation to the Bermudan swaption. But why is this useful? After all, the more exercise dates one is willing to allow in the approximating structure, the better one can approximate the characteristics of a Bermudan swaption.

The answer lies in the greater tractability of Canaries. Since—as discussed above—Canaries do indeed serve as reasonable approximations to the more complex Bermudan structures, the problem of developing a relative value metric for the more complex Bermudans can be simplified to that of developing relative value views on its Canary CTD. Also, Canary swaption premia are determined by vanilla swaption pricing inputs plus one implied correlation input, meaning that relative value metrics based on Canary approximations can be estimated from (and monetized through) the vanilla swaptions and correlation markets.

As an example, consider a 1Y(4Y)x5Y Canary receiver. At the 1-year horizon, this option will be exercised if and only if the exercise value (the forward value of the 5-year swap with fixed coupon equal to the

Exhibit 7: ... and vega

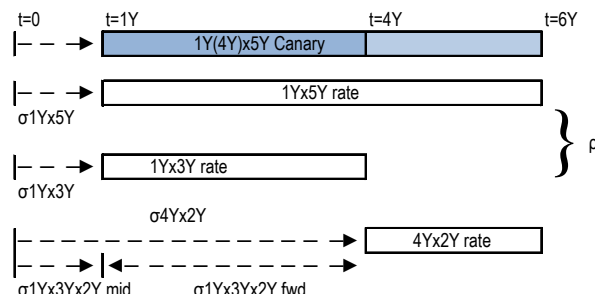
Deviation of the vega profile of selected European and Canary swaptions from the 1Yx5Y Bermudan vega profile plotted against shifts of the yield curve; %



The vega profile is obtained as a % of the original vega (that is, for no change in the yield curve). Each curve is obtained by subtracting the European or Canary vega profile from the Bermudan vega profile. The 1Y(2.5Y)x5Y Canary and the 1Yx5Y European are the CTDs. COB 5/22/2012

Exhibit 8: Pricing a 1Y(4Y)x5Y Canary swaption

Symbolic representation of a 1y (4y) x 5y Canary swaption and the minimal components needed to price it



strike) is greater than residual option value (the value of a 3Yx2Y receiver swaption at that point in time). Thus, the value of the right to defer exercise at the 1Y point depends on the then spot 3Yx2Y swaption volatility, which we approximate by the *forward* volatility, in addition to the 1Yx5Y spot swaption volatility. Moreover, as illustrated in the grey box below, 1-year forward 3Yx2Y implied volatility is itself determined by 3 vanilla swaption implied vols and a correlation: in this example, one would require 1Yx3Y, 1Yx5Y and 4Yx2Y swaption implieds, as well as an implied correlation input that represents the 1-year correlation between the 1Yx3Y and 1Yx5Y forward swap yields (see the schematic in **Exhibit 8**). This means that we may derive a fair price for the

Srinivas Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

Introduction to forward volatility

Forward volatility exposure in the USD swaptions market is typically created via forward option agreements. This generally involves an agreement that enables one counterparty to buy an ATM straddle at a future point in time, at a price (i.e., the forward premium) agreed to on the trade date. For instance, a 1Yx2Yx5Y forward option agreement would allow a client to purchase a 2Yx5Y then-at-the-money straddle 1-year from trade date, at the pre-determined price. Note that the strike on the 2Yx5Y would be set at the completion of the 1-year forward term; indeed, it is this characteristic that makes it a forward volatility instrument, since the absence of strike results in no delta or gamma exposure for the first 1-year period in this example. This can be a desirable characteristic indeed; for instance, this allows an investor to create vega exposure without having to manage delta or gamma exposures. Alternatively, an investor looking to put on vol positions with desirable implied vol slide characteristics can simply buy or sell a forward option agreement, with no subsequent dynamic position management as would be necessitated if the investor were to trade swaption calendar spreads.

The pricing of any given forward option structure is determined by 3 different swaption implied volatilities, and one correlation input. The discussion below clarifies this in the context of the example mentioned above. Consider a 3Yx5Y plain vanilla swaption; its implied volatility may be thought of as a weighted average of the volatility of the underlying forward yield over the 1st year of the option (which we can call the midcurve volatility, since the underlying forward rolls down from being 3-years forward to only 2-years forward as opposed to spot), and the volatility of the same underlying yield over the last 2 years of the options life (over which period the underlying yield rolls from being 2-years forward to spot).

More precisely, we can write:

$$1 * \sigma_{M,1 \times 2 \times 5}^2 + 2 * \sigma_{F,1 \times 2 \times 5}^2 = 3 * \sigma_{E,3 \times 5}^2$$

where $\sigma_{M,1 \times 2 \times 5}^2$ denotes the implied volatility of a midcurve that expires in 1 year, but with the same underlying swap as the 3Yx5Y - i.e., upon expiry, the midcurve swaption, if exercised, would result in a 2Yx5Y forward swap position. $\sigma_{F,1 \times 2 \times 5}^2$ denotes 1-year forward volatility on the 2Yx5Y volatility while $\sigma_{E,3 \times 5}^2$ refers to the

3Yx5Y European swaption volatility.

If a sufficiently deep and liquid market existed in midcurve options, nothing further would be necessary.

However, in practice, dealers will likely need to synthetically create exposure to midcurve volatility, via more liquid plain vanilla swaption instruments. This is done by viewing forward swap rates as linear combinations of spot swap rates. For instance, if we suppose that:

$$\Delta s_{2 \times 5} = b1 * \Delta s_2 + b2 * \Delta s_7,$$

Then, we may approximately infer the 1Yx2Yx5Y midcurve volatility from 1Yx2Y and 1Yx7Y volatilities, as well as the 1-year average correlation between 2- and 7-year swaps, via the following equation:

$$\sigma_{M,1 \times 2 \times 5}^2 = b1^2 \sigma_{E,1 \times 2}^2 + b2^2 \sigma_{E,1 \times 7}^2 - 2\rho * b1 * b2 * \sigma_{E,1 \times 7} \sigma_{E,1 \times 2},$$

where ρ is the 1-year correlation between 2-year and 7-year swap yields

Combining our expression for midcurve volatility with our earlier expression, we may write:

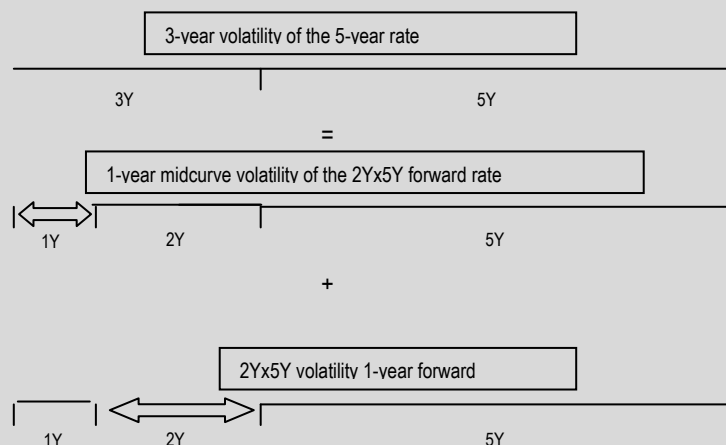
$$\sigma_{F,1 \times 2 \times 5}^2 = \frac{1}{2} (3 * \sigma_{E,3 \times 5}^2 - (b1^2 \sigma_{E,1 \times 2}^2 + b2^2 \sigma_{E,1 \times 7}^2 - 2\rho * b1 * b2 * \sigma_{E,1 \times 7} \sigma_{E,1 \times 2}))$$

Thus, the pricing of a 1Yx2Yx5Y forward vol contract, for instance, is determined by the implied volatilities of the 3Yx5Y, 1Yx2Y and 1Yx7Y swaptions, as well as the 1 year implied correlation between 2- and 7-year swap yield changes. Equivalently, the risk exposure in a long 1Yx2Yx5Y forward option agreement position typically decomposes into:

- a long position in 3Yx5Y swaptions
- a long position in 1Yx2Y swaptions,
- a short position in 1Yx7Y swaptions, and
- long exposure to the 1-year correlation between 2- and 7-year swaps.

Canary using vanilla swaption implied volatilities and implied correlations.

Moreover, the recent growth and development of a correlation market, thanks to rising activity in bivariate options such as YCSOs as well as increased trading



Srini Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

Exhibit 9: An illustration of the sources of value in a sample Bermudan receiver swaption

An illustration of the components driving the richness/cheapness of a 6Mx30Y Bermudan receiver swaption, based upon its Canary CTD*

Premiums from a Bermudan model	
6Mx30Y Berm receiver	1409.5 bp
3Y6M(14Y)x30Y Canary	1176.6 bp
Vega	32.5 bp of notl per 0.1 bp/day
Alternate fair values for Canary based on:	
Implied correlation	1191.8 bp
Mispricing of Canary (& Berm)	
In price terms	-15.3 bp of notional
In vol units	-0.05 bp/day
plus	
Mispricing in correlation markets	
Canary price using implied correlation	1191.8 bp
Canary price using realized correlation	1192.0 bp
Correlation driven mispricing of Berm	
In price units	-0.11 bp of notional
In vol units	0.00 bp/day
plus	
Mispricing of 3.5x27/14x16.5 vol curve	
Canary price using realized correlation	1192.0 bp
Canary price under tweaked vol curve	1202.3 bp
Vol curve driven mispricing of Berm	
In price terms	-10.3 bp of notional
In vol units	-0.03 bp/day
equals	
Total mispricing	
	-0.08 bp/day

* Premia quoted in bp of notional. Data as of COB 5/14/2012

activity in forward and midcurve volatility, means that relative value metrics for Bermudan swaptions that are based on the idea of approximating Bermudans via Canaries, can likely be monetized by buying or selling Bermudan swaptions versus offsetting positions in vanilla volatility and correlation. These ideas are explored further in the next section.

A relative value measure

We may now develop a relative value metric. In doing so, we note that there are three possible sources of value. First, any cheapness/richness in a Bermudan swaption would likely extend into its Canary CTD, meaning that the “Bermudan market price” of its canary CTD (which can be inferred from a suitably

Exhibit 10: Indicative mispricings for various Bermudan receiver structures

Components* of our relative value metric for Bermudan receiver swaptions and the total richness/cheapness in various sectors expressed in price terms (bp of notional) and Bermudan implied volatility terms (bp/day)

Sector	Bermudan swaption mispricing*		Correlation mispricing**		Total	
	Price	Vol	Price	Vol	Price	Vol
6Mx5Y	-5.7	-0.16	-0.7	-0.02	-6.4	-0.18
6Mx10Y	-10.2	-0.11	-2.8	-0.03	-13.0	-0.15
6Mx2Y	-1.5	-0.14	0.4	0.03	-1.2	-0.11
6Mx3Y	-1.5	-0.08	-0.1	-0.01	-1.6	-0.09
1Yx10Y	-2.6	-0.03	-3.4	-0.04	-6.1	-0.06
1Yx5Y	-0.7	-0.02	-1.2	-0.03	-1.9	-0.05
6Mx30Y	-13.3	-0.04	-0.1	0.00	-13.4	-0.04
1Yx30Y	-6.1	-0.02	-0.2	0.00	-6.4	-0.02
2Yx30Y	7.0	0.02	-0.6	0.00	6.3	0.02
2Yx10Y	8.2	0.07	-2.6	-0.02	5.6	0.05
3Yx30Y	21.5	0.06	-1.2	0.00	20.3	0.06
5Yx30Y	25.5	0.07	-1.8	0.00	23.7	0.06
3Yx5Y	7.3	0.13	-3.5	-0.06	3.7	0.06
3Yx10Y	13.2	0.11	-3.3	-0.03	10.0	0.08
5Yx7Y	16.5	0.17	-2.9	-0.03	13.6	0.14
5Yx10Y	23.2	0.16	-3.2	-0.02	20.0	0.14

* The price of the Canary CTD from a Bermudan swaption pricing model, minus its fair value estimated from vanilla swaption inputs and implied correlations from the YCSO market. Estimate based on Bermudan pricing model, may not represent tradable prices. As of COB 5/29/2012.

** Canary CTD premium using 6M realized correlation minus premium using implied correlation.

calibrated Bermudan swaption pricing model) may differ from the price of the same Canary that can independently be calculated from vanilla implied volatilities and implied correlations from the YCSO market. Second, using an empirical framework, we may conclude that implied correlations in the YCSO market are themselves rich or cheap, based on comparisons to realized correlations over time. Third, since Bermudans are often traded as BE switches with respect to the European swaption corresponding to the first exercise date, the implied vol curve could be another source of value (more on this later). Again using an empirical framework, we may take a view on the volatility curve corresponding to a given canary (i.e., the implied volatility differential between the longer and short expiries for the Canary). By repricing the Canary using the estimated fair level for the vol curve, we may back out the contribution of any potential vol curve mispricing to the richness/cheapness of the Bermudan swaption being

Srinivas Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

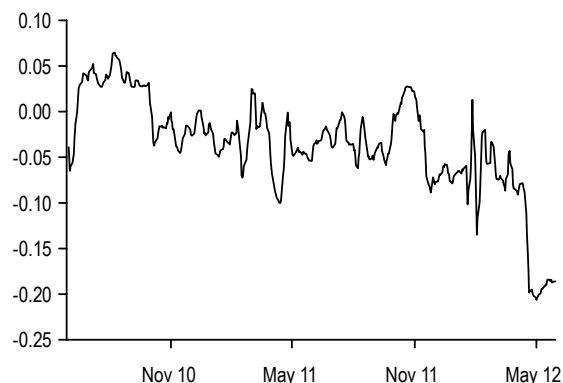
analyzed. Last, we may total up the mispricing from all three sources, and divide by the vega of the Bermudan swaption to compute the richness or cheapness of the Bermudan swaption, expressed in basis points per day. This is illustrated in detail for the case of the 6Mx30Y Bermudan receiver swaption in **Exhibit 9**.

In practice, we prefer to use the sum of the first two contributing factors as our metric for the Bermudan swaption's mispricing, ignoring the impact of any mispricing in the implied vol curve. We included this contributing factor in Exhibit 9 to showcase all the sources of value in a Bermudan swaption. However, while correlation risk can be viewed as an intrinsic part of Bermudan swaptions, views on the implied volatility curve are more easily expressed via vanilla European swaptions, making it less useful to include it in a summary measure of mispricing for Bermudan swaptions. Therefore, going forward, any references to the richness/cheapness of Bermudan swaptions can be understood to mean the sum of the first two components—the current indicative mispricing for several benchmark Bermudan swaption structures is illustrated in **Exhibit 10**, along with a breakdown. A time series of the R/C values for a sample Bermudan receiver swaption is also shown in **Exhibit 11**; similar charts for a wide range of structures can be found in the *J.P.Morgan Bermudan Receiver Swaption Relative Value Report*, which can be found in daily analytics packages and available via <http://mm.jpmorgan.com>.

Having developed a metric for the richness/cheapness of Bermudan swaptions, the last remaining question is: does it work in practice as a trading signal? To assess the usefulness of our metric in this regard, we examined rolling 3-month total returns from a reasonably practical strategy—buying a Bermudan receiver swaption versus selling its European CTD. Both swaptions were assumed to be delta-hedged daily with their underlying forward swaps in order to isolate the vol effects. As seen in **Exhibit 12**, and as one would expect, returns from this strategy (expressed in implied vol units) are inversely correlated to the richness of Bermudans. In particular, when Bermudan swaptions are sufficiently cheap (say, cheaper by 0.3bp/day or more), our results suggest that the value in Bermudans can be monetized via a relatively simple strategy of buying Bermudan swaptions versus selling its European CTD on a delta-hedged basis.

Exhibit 11: 6Mx5Y Bermudan receiver swaptions are currently the cheapest they have been in recent years

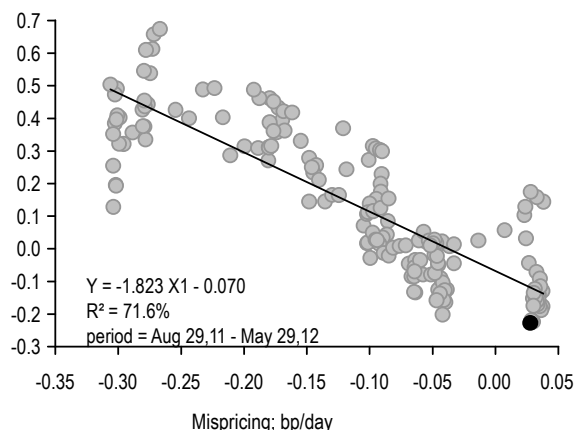
Total mispricing* in the 6Mx5Y Bermudan receiver swaption; bp/day



* Negative values indicate cheapness of Bermudan swaptions. As of COB 5/29/2012. Estimate from Bermudan pricing model, may not represent tradable values.

Exhibit 12: Returns on delta and vega hedged Bermudan longs appear inversely correlated to its richness estimated by our relative value metric

Rolling 3M total returns from buying 5Yx30Y Bermudan receiver swaptions versus selling its European CTD swaption*, regressed against ex-ante mispricing**, bp/day



* Both the Bermudan swaption and its European CTD swaption are assumed to be delta hedged daily using the underlying forward swap. Options are re-struck at the end of each month.

** As estimated by our relative value framework, as of the start of the rolling 3-month period

Conclusions

In any market, one of the most basic questions that investors ask is whether a particular financial instrument is rich or cheap. With regards to the Bermudan swaptions market, this question has been easier asked than answered. Moreover, it is equally important that any framework that attempts to quantify relative value be monetizable.

In this paper, we have addressed this basic question for Bermudan swaptions. Our approach draws on the

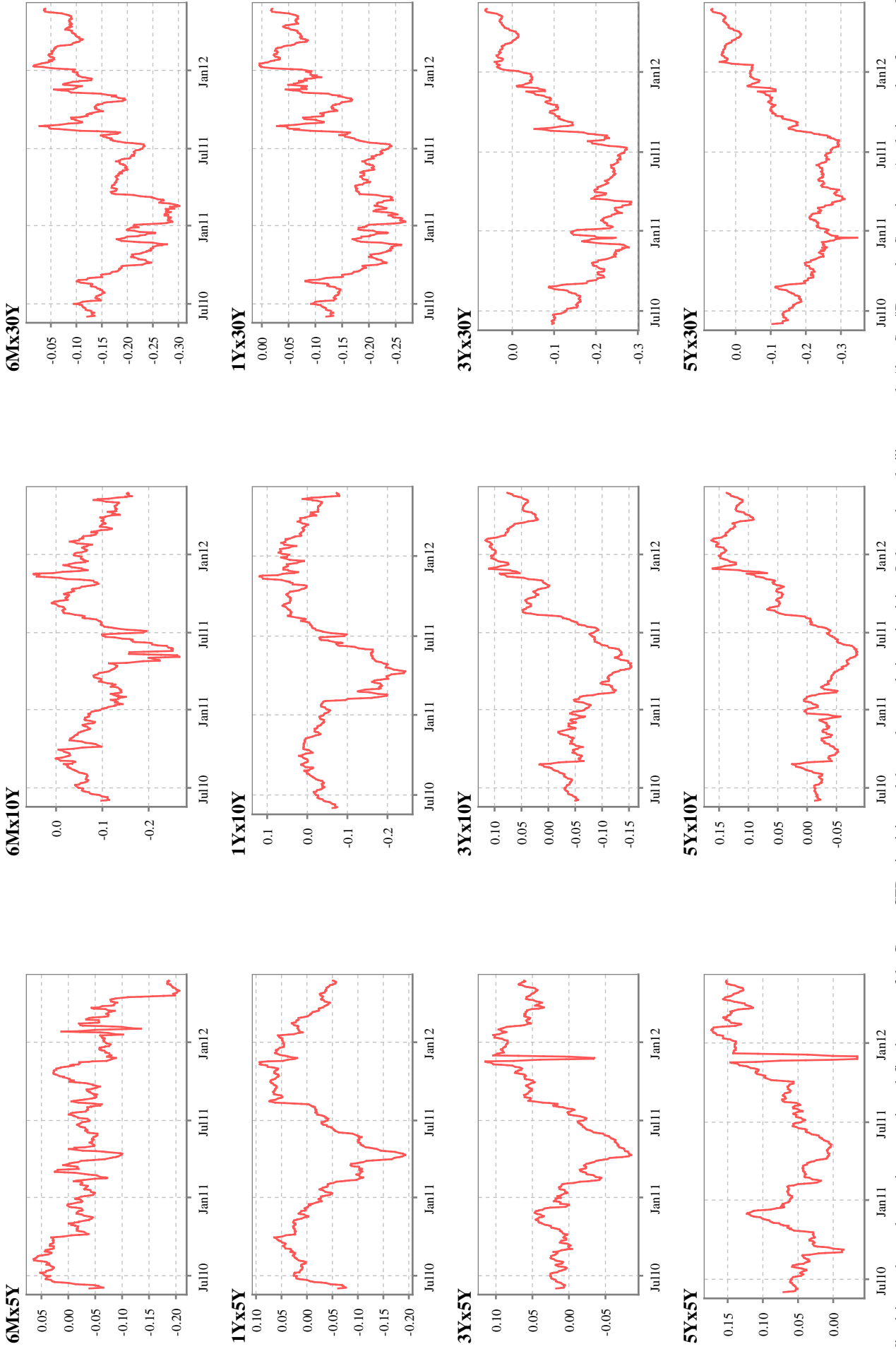
Srini Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

observation that Canary swaptions—options with precisely two exercise dates—are rich enough to provide a stable approximation of Bermudans while also being simple enough to analyze. Moreover, while Bermudan swaptions have always been understood to include risk exposure to implied volatility levels, the implied volatility curve, as well as correlations, these exposures have always been rather amorphous and difficult to break down. Which vol curves are the ones that matter, and to what extent? Which correlations are most relevant to a given Bermudan swaption's pricing? What are the sensitivities? These are all important questions to answer in order to truly understand the risks in a Bermudan swaption position. The beauty of using approximating Canaries is that all of these questions are answerable—since the Canary CTD is a decent approximation of the more complex Bermudan swaption, the implied volatility curves and implied correlations that are relevant to the Canary's pricing are also the relevant market variables that the Bermudan is most exposed to. Quantifying the sensitivities is also rather straightforward once one has determined the best Canary approximation.

Our approach also leads to a rich/cheap value metric that is monetizable, via a relatively straightforward trading strategy involving the Bermudan swaption versus its European swaption CTD. A daily Bermudan Receiver Swaption Relative Value Report, based on the framework discussed in this paper, is attached here and will be included in J.P.Morgan's daily analytics packages.

Derivatives Strategy

Bermudan Receiver Swaption Relative Value



Mispricing on bermudan receiver swaptions defined as sum of the Canary CTD mispricing and the market correlation mispricing. In bermudan volatility terms; bp/day. See "Bermudan Swaptions - A relative value framework" for details.

Srini Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

Analyst Certification:

The research analyst(s) denoted by an "AC" on the cover of this report certifies (or, where multiple research analysts are primarily responsible for this report, the research analyst denoted by an "AC" on the cover or within the document individually certifies, with respect to each security or issuer that the research analyst covers in this research) that: (1) all of the views expressed in this report accurately reflect his or her personal views about any and all of the subject securities or issuers; and (2) no part of any of the research analyst's compensation was, is, or will be directly or indirectly related to the specific recommendations or views expressed by the research analyst(s) in this report.

Conflict of Interest:

This research contains the views, opinions and recommendations of J.P. Morgan research analysts. Research analysts routinely consult with J.P. Morgan trading desk personnel in formulating views, opinions and recommendations in preparing research. Trading desks may trade, or have traded, as principal on the basis of the research analyst(s) views and report(s). Therefore, this research may not be independent from the proprietary interests of J.P. Morgan trading desks which may conflict with your interests. In addition, research analysts receive compensation based, in part, on the quality and accuracy of their analysis, client feedback, trading desk and firm revenues and competitive factors. As a general matter, J.P. Morgan and/or its affiliates normally make a market and trade as principal in fixed income securities discussed in research reports.

Other Disclosures

J.P. Morgan ("JPM") is the global brand name for J.P. Morgan Securities LLC ("JPMS") and its affiliates worldwide. J.P. Morgan Cazenove is a marketing name for the U.K. investment banking businesses and EMEA cash equities and equity research businesses of JPMorgan Chase & Co. and its subsidiaries.

Options related research: If the information contained herein regards options related research, such information is available only to persons who have received the proper option risk disclosure documents. For a copy of the Option Clearing Corporation's Characteristics and Risks of Standardized Options, please contact your J.P. Morgan Representative or visit the OCC's website at <http://www.optionsclearing.com/publications/risks/riskstoc.pdf>.

Legal Entities Disclosures

U.S.: JPMS is a member of NYSE, FINRA and SIPC. J.P. Morgan Futures Inc. is a member of the NFA. JPMorgan Chase Bank, N.A. is a member of FDIC and is authorized and regulated in the UK by the Financial Services Authority. **U.K.:** J.P. Morgan Securities Ltd. (JPMSL) is a member of the London Stock Exchange and is authorized and regulated by the Financial Services Authority. Registered in England & Wales No. 2711006. Registered Office 125 London Wall, London EC2Y 5AJ. **South Africa:** J.P. Morgan Equities Limited is a member of the Johannesburg Securities Exchange and is regulated by the FSB. **Hong Kong:** J.P. Morgan Securities (Asia Pacific) Limited (CE number AAJ321) is regulated by the Hong Kong Monetary Authority and the Securities and Futures Commission in Hong Kong. **Korea:** J.P. Morgan Securities (Far East) Ltd, Seoul Branch, is regulated by the Korea Financial Supervisory Service. **Australia:** J.P. Morgan Australia Limited (ABN 52 002 888 011/AFS Licence No: 238188) is regulated by ASIC and J.P. Morgan Securities Australia Limited (ABN 61 003 245 234/AFS Licence No: 238066) is a Market Participant with the ASX and regulated by ASIC. **Taiwan:** J.P.Morgan Securities (Taiwan) Limited is a participant of the Taiwan Stock Exchange (company-type) and regulated by the Taiwan Securities and Futures Bureau. **India:** J.P. Morgan India Private Limited, having its registered office at J.P. Morgan Tower, Off. C.S.T. Road, Kalina, Santacruz East, Mumbai - 400098, is a member of the National Stock Exchange of India Limited (SEBI Registration Number - INB 230675231/INF 230675231/INE 230675231) and Bombay Stock Exchange Limited (SEBI Registration Number - INB010675237/INB010675237) and is regulated by Securities and Exchange Board of India. **Thailand:** JPMorgan Securities (Thailand) Limited is a member of the Stock Exchange of Thailand and is regulated by the Ministry of Finance and the Securities and Exchange Commission. **Indonesia:** PT J.P. Morgan Securities Indonesia is a member of the Indonesia Stock Exchange and is regulated by the BAPEPAM LK. **Philippines:** J.P. Morgan Securities Philippines Inc. is a member of the Philippine Stock Exchange and is regulated by the Securities and Exchange Commission. **Brazil:** Banco J.P. Morgan S.A. is regulated by the Comissao de Valores Mobiliarios (CVM) and by the Central Bank of Brazil. **Mexico:** J.P. Morgan Casa de Bolsa, S.A. de C.V., J.P. Morgan Grupo Financiero is a member of the Mexican Stock Exchange and authorized to act as a broker dealer by the National Banking and Securities Exchange Commission. **Singapore:** This material is issued and distributed in Singapore by J.P. Morgan Securities Singapore Private Limited (JPMSS) [MICA (P) 032/01/2012 and Co. Reg. No.: 199405335R] which is a member of the Singapore Exchange Securities Trading Limited and is regulated by the Monetary Authority of Singapore (MAS) and/or JPMorgan Chase Bank, N.A., Singapore branch (JPMCB Singapore) which is regulated by the MAS. **Malaysia:** This material is issued and distributed in Malaysia by JPMorgan Securities (Malaysia) Sdn Bhd (18146-X) which is a Participating Organization of Bursa Malaysia Berhad and a holder of Capital Markets Services License issued by the Securities Commission in Malaysia. **Pakistan:** J. P. Morgan Pakistan Broking (Pvt.) Ltd is a member of the Karachi Stock Exchange and regulated by the Securities and Exchange Commission of Pakistan. **Saudi Arabia:** J.P. Morgan Saudi Arabia Ltd. is authorized by the Capital Market Authority of the Kingdom of Saudi Arabia (CMA) to carry out dealing as an agent, arranging, advising and custody, with respect to securities business under licence number 35-07079 and its registered address is at 8th Floor, Al-Faisaliyah Tower, King Fahad Road, P.O. Box 51907, Riyadh 11553, Kingdom of Saudi Arabia. **Dubai:** JPMorgan Chase Bank, N.A., Dubai Branch is regulated by the Dubai Financial Services Authority (DFSA) and its registered address is Dubai International Financial Centre - Building 3, Level 7, PO Box 506551, Dubai, UAE.

Srini Ramaswamy^{AC} (1-212) 834-4573
Alberto Iglesias (1-212) 834-5116
Praveen Korapaty (1-212) 834-3092
J.P. Morgan Securities LLC

Country and Region Specific Disclosures

U.K. and European Economic Area (EEA): Unless specified to the contrary, issued and approved for distribution in the U.K. and the EEA by JPMSL. Investment research issued by JPMSL has been prepared in accordance with JPMSL's policies for managing conflicts of interest arising as a result of publication and distribution of investment research. Many European regulators require a firm to establish, implement and maintain such a policy. This report has been issued in the U.K. only to persons of a kind described in Article 19 (5), 38, 47 and 49 of the Financial Services and Markets Act 2000 (Financial Promotion) Order 2005 (all such persons being referred to as "relevant persons"). This document must not be acted on or relied on by persons who are not relevant persons. Any investment or investment activity to which this document relates is only available to relevant persons and will be engaged in only with relevant persons. In other EEA countries, the report has been issued to persons regarded as professional investors (or equivalent) in their home jurisdiction. **Australia:** This material is issued and distributed by JPMSAL in Australia to "wholesale clients" only. JPMSAL does not issue or distribute this material to "retail clients." The recipient of this material must not distribute it to any third party or outside Australia without the prior written consent of JPMSAL. For the purposes of this paragraph the terms "wholesale client" and "retail client" have the meanings given to them in section 761G of the Corporations Act 2001. **Germany:** This material is distributed in Germany by J.P. Morgan Securities Ltd., Frankfurt Branch and J.P.Morgan Chase Bank, N.A., Frankfurt Branch which are regulated by the Bundesanstalt für Finanzdienstleistungsaufsicht. **Hong Kong:** The 1% ownership disclosure as of the previous month end satisfies the requirements under Paragraph 16.5(a) of the Hong Kong Code of Conduct for Persons Licensed by or Registered with the Securities and Futures Commission. (For research published within the first ten days of the month, the disclosure may be based on the month end data from two months' prior.) J.P. Morgan Broking (Hong Kong) Limited is the liquidity provider/market maker for derivative warrants, callable bull bear contracts and stock options listed on the Stock Exchange of Hong Kong Limited. An updated list can be found on HKEx website: <http://www.hkex.com.hk>. **Japan:** There is a risk that a loss may occur due to a change in the price of the shares in the case of share trading, and that a loss may occur due to the exchange rate in the case of foreign share trading. In the case of share trading, JPMorgan Securities Japan Co., Ltd., will be receiving a brokerage fee and consumption tax (shouhizei) calculated by multiplying the executed price by the commission rate which was individually agreed between JPMorgan Securities Japan Co., Ltd., and the customer in advance. Financial Instruments Firms: JPMorgan Securities Japan Co., Ltd., Kanto Local Finance Bureau (kinsho) No. 82 Participating Association / Japan Securities Dealers Association, The Financial Futures Association of Japan. **Korea:** This report may have been edited or contributed to from time to time by affiliates of J.P. Morgan Securities (Far East) Ltd, Seoul Branch. **Singapore:** JPMS and/or its affiliates may have a holding in any of the securities discussed in this report; for securities where the holding is 1% or greater, the specific holding is disclosed in the Important Disclosures section above. **India:** For private circulation only, not for sale. **Pakistan:** For private circulation only, not for sale. **New Zealand:** This material is issued and distributed by JPMSAL in New Zealand only to persons whose principal business is the investment of money or who, in the course of and for the purposes of their business, habitually invest money. JPMSAL does not issue or distribute this material to members of "the public" as determined in accordance with section 3 of the Securities Act 1978. The recipient of this material must not distribute it to any third party or outside New Zealand without the prior written consent of JPMSAL. **Canada:** The information contained herein is not, and under no circumstances is to be construed as, a prospectus, an advertisement, a public offering, an offer to sell securities described herein, or solicitation of an offer to buy securities described herein, in Canada or any province or territory thereof. Any offer or sale of the securities described herein in Canada will be made only under an exemption from the requirements to file a prospectus with the relevant Canadian securities regulators and only by a dealer properly registered under applicable securities laws or, alternatively, pursuant to an exemption from the dealer registration requirement in the relevant province or territory of Canada in which such offer or sale is made. The information contained herein is under no circumstances to be construed as investment advice in any province or territory of Canada and is not tailored to the needs of the recipient. To the extent that the information contained herein references securities of an issuer incorporated, formed or created under the laws of Canada or a province or territory of Canada, any trades in such securities must be conducted through a dealer registered in Canada. No securities commission or similar regulatory authority in Canada has reviewed or in any way passed judgment upon these materials, the information contained herein or the merits of the securities described herein, and any representation to the contrary is an offence. **Dubai:** This report has been issued to persons regarded as professional clients as defined under the DFSA rules.

General: Additional information is available upon request. Information has been obtained from sources believed to be reliable but JPMorgan Chase & Co. or its affiliates and/or subsidiaries (collectively J.P. Morgan) do not warrant its completeness or accuracy except with respect to any disclosures relative to JPMS and/or its affiliates and the analyst's involvement with the issuer that is the subject of the research. All pricing is as of the close of market for the securities discussed, unless otherwise stated. Opinions and estimates constitute our judgment as of the date of this material and are subject to change without notice. Past performance is not indicative of future results. This material is not intended as an offer or solicitation for the purchase or sale of any financial instrument. The opinions and recommendations herein do not take into account individual client circumstances, objectives, or needs and are not intended as recommendations of particular securities, financial instruments or strategies to particular clients. The recipient of this report must make its own independent decisions regarding any securities or financial instruments mentioned herein. JPMS distributes in the U.S. research published by non-U.S. affiliates and accepts responsibility for its contents. Periodic updates may be provided on companies/industries based on company specific developments or announcements, market conditions or any other publicly available information. Clients should contact analysts and execute transactions through a J.P. Morgan subsidiary or affiliate in their home jurisdiction unless governing law permits otherwise.

"Other Disclosures" last revised January 6, 2012.

Copyright 2012 JPMorgan Chase & Co. All rights reserved. This report or any portion hereof may not be reprinted, sold or redistributed without the written consent of J.P. Morgan.