
MPC Model

$$x_{t+1} = x_t + v_t \cdot \cos(\psi_t) \cdot dt \tag{1}$$

$$y_{t+1} = y_t + v_t \cdot \sin(\psi_t) \cdot dt \tag{2}$$

$$\psi_{t+1} = \psi_t + \frac{v_t}{L_f} \cdot \delta_t \cdot dt \tag{3}$$

$$v_{t+1} = v_t + a_t \cdot dt \tag{4}$$

$$cte_{t+1} = f(x_t) - y_t + v_t \cdot \sin(e\psi_t) \cdot dt \tag{5}$$

$$e\psi_{t+1} = \psi_t - \psi_{des_t} + \frac{v_t}{L_f} \cdot \delta_t \cdot dt \tag{6}$$

Constraints

$$\delta \in [-25^\circ, +25^\circ] \tag{7}$$

$$a \in [-1.0, +1.0] \tag{8}$$

Cost

$$J = \sum_{t=1}^N (cte_t - cte_{ref})^2 + (e\psi_t - e\psi_{ref})^2 + ... \tag{9}$$

MPC state feedback loop:
Pass the current state to the MPC.
Call the optimization solver. The solver uses the state, model, constraints and cost function to return a control vector that minimizes the cost function.