

EE5600Assignment01 Problem103 in Lines Planes

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1 Problem statement:

If the points $(1, 1, p)$ and $(-3, 0, 1)$ be equidistant from the plane $(3, 4, -12) \cdot \mathbf{x} = -13$, then find the value of p .

2 Procedure:

1. The perpendicular distance of point $P(x_1, y_1, z_1)$ from the given plane $ax + by + cz = 0$ is given by $\text{distance} = \frac{ax_1 + by_1 + cz_1}{\sqrt{a^2 + b^2 + c^2}}$
2. Point $P_1 = (1, 1, p)$
3. Point $P_2 = (-3, 0, 1)$
4. Plane : $3x + 4y - 12z + 13 = 0$ (as given in the problem statement)
5. Let the distance of P_1 from plane = D_1
6. Let the distance of P_2 from plane = D_2
7. As given in the problem statement, P_1 and P_2 are equidistant.
8. If D_1 and D_2 are made equal, in formula mentioned in (2-1) denominator gets cancelled.
9. That implies $\text{modulus}(ax_1 + by_1 + cz_1 + d) = \text{modulus}(ax_2 + by_2 + cz_2 + d)$
10. In the given problem
 $x_1 = 1; y_1 = 1; z_1 = p; \text{ and } x_2 = -3, y_2 = 0, z_2 = 1$
11. Therefore
$$z_1 = \frac{\text{modulus}(ax_2 + by_2 + cz_2 + d) - (ax_1 + by_1 + d)}{c}$$
12. In the above formula the values were substituted and value of z_1 is calculated.

2.1

code is made available in assignment01_e20resch14006.ipynb