

Boseong Kim

Yonsei - IBM Qiskit User Meetup

About Me



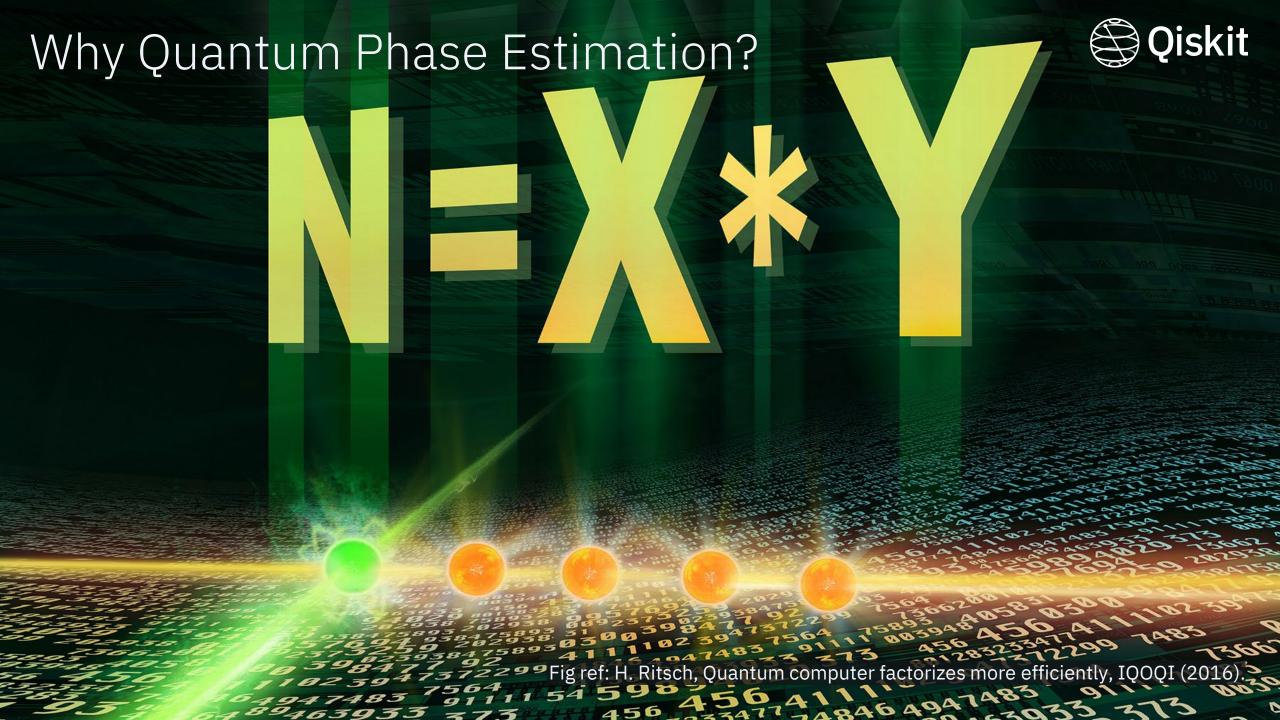


김보성 (boseong.kim.22@ucl.ac.uk)

- MSc in Quantum Technologies @ University College London
- BSc in Physics & Mathematics @ Yonsei University

 YouTube!
 - → Officer & Tutor of Yonsei Physics Society SCC -
- Qiskit Advocate
- Research Keywords: Quantum Advantage, Quantum Contextuality, Quantum Algorithms, Quantum Computation for High Energy Physics







Please visit!

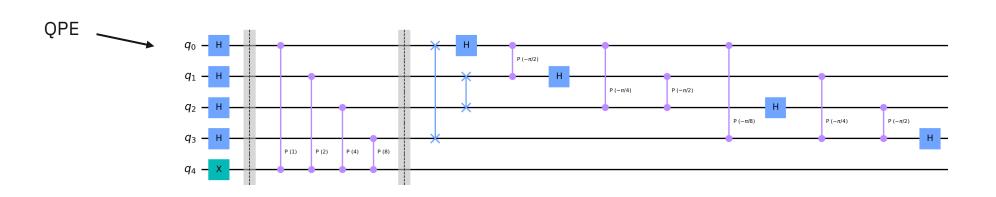
https://qiskit.org/textbook/

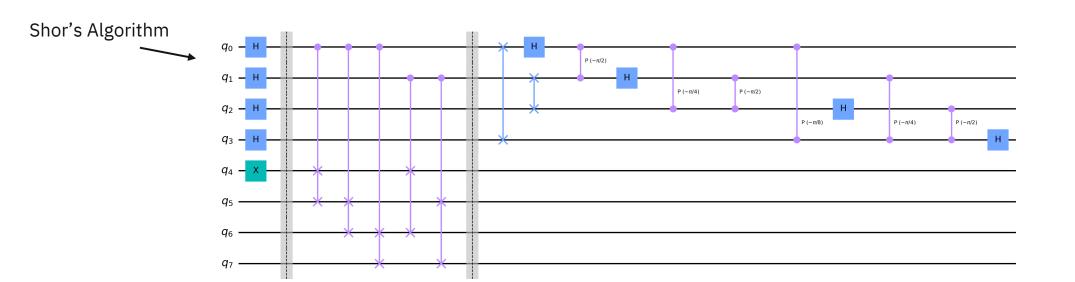
Deutsch-Jozsa Algorithm Bernstein-Vazirani Algorithm Simon's Algorithm

Shor's Algorithm

Quantum Phase Estimation vs Shor's Algorithm



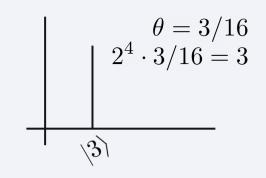


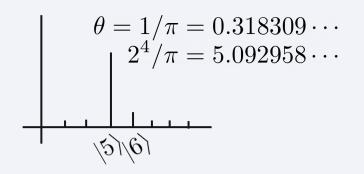


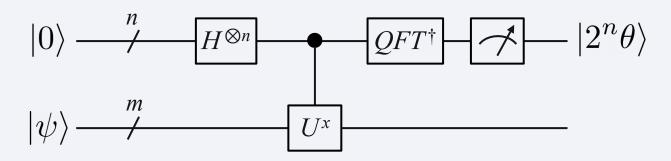


How can we measure the phase from a gate?

$$U|\psi\rangle = e^{2\pi i\theta} |\psi\rangle$$

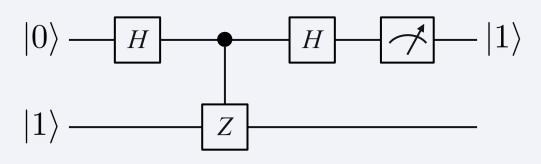






Phase Kickback



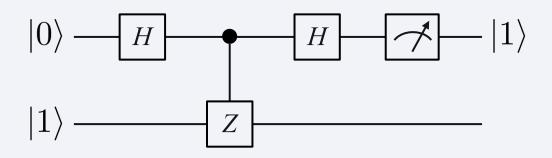


Gates in the Phase Kickback Circuit



$$H|0\rangle = \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

$$H\left|1\right\rangle = \frac{\left|0\right\rangle - \left|1\right\rangle}{\sqrt{2}}$$



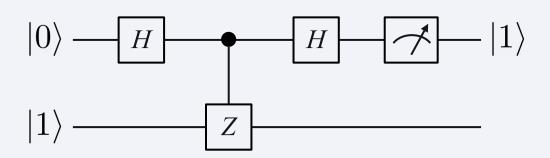
Gates in the Phase Kickback Circuit



$$Z$$
: Z gate

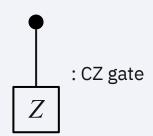
$$Z|0\rangle = |0\rangle$$

$$Z|1\rangle = -|1\rangle$$



Gates in the Phase Kickback Circuit

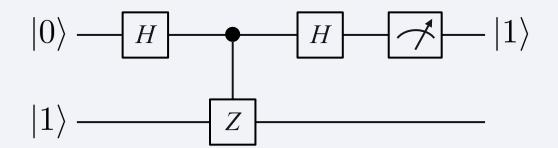




$$CZ |1\rangle |0\rangle = |1\rangle (Z |0\rangle) = |1\rangle |0\rangle$$

$$CZ |1\rangle |1\rangle = |1\rangle (Z |1\rangle)$$

= $|1\rangle (-|1\rangle) = -|1\rangle |1\rangle$



Phase Kickback

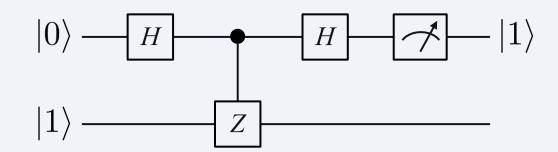


$$|0\rangle |1\rangle$$

$$\xrightarrow{H \otimes I} \left(\frac{|0\rangle + |1\rangle}{\sqrt{2}} \right) |1\rangle = \frac{|0\rangle |1\rangle + |1\rangle |1\rangle}{\sqrt{2}}$$

$$\xrightarrow{CZ} \frac{|0\rangle |1\rangle - |1\rangle |1\rangle}{\sqrt{2}} = \left(\frac{|0\rangle - |1\rangle}{\sqrt{2}}\right) |1\rangle \qquad |0\rangle - H$$

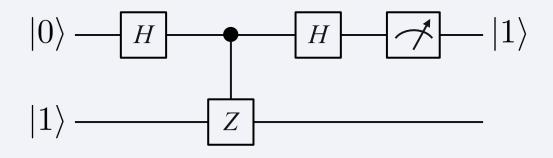
$$\xrightarrow{H\otimes I} |1\rangle |1\rangle$$

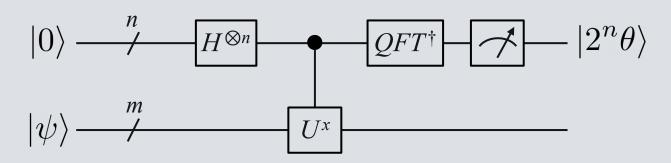


Phase Kickback



vs Quantum Phase Estimation

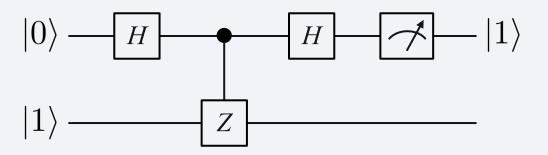






$$Z$$
: Z gate

$$Z|1\rangle = -|1\rangle = e^{2\pi i \frac{1}{2}}|1\rangle$$



$$oxedsymbol{U}$$
 : Some unitary gate giving phase

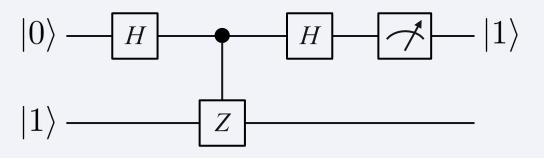
$$U|\psi\rangle = e^{2\pi i\theta} |\psi\rangle$$

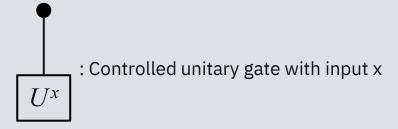
$$|0\rangle$$
 \xrightarrow{n} $|0\rangle$ $\xrightarrow{H\otimes n}$ $|0\rangle$ $|0\rangle$



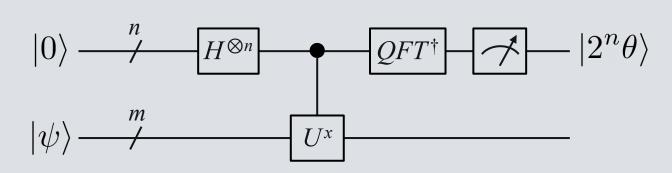
$$Z$$
: Z gate

$$Z|1\rangle = -|1\rangle = e^{2\pi i \frac{1}{2}}|1\rangle$$





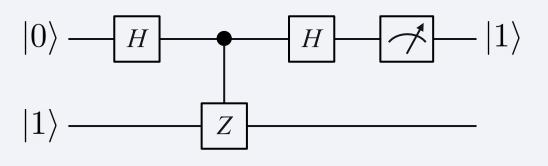
$$CU |x\rangle |\psi\rangle = |x\rangle (U^x |\psi\rangle)$$
$$= e^{2\pi i\theta x} |x\rangle |\psi\rangle$$





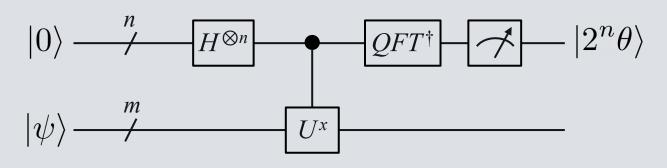
H : Hadamard gate

$$H\left(\frac{|0\rangle - |1\rangle}{\sqrt{2}}\right) = |1\rangle$$



 QFT^{\dagger} : Quantum Fourier Transform (inversed)

$$QFT^{\dagger} \left(\frac{1}{\sqrt{2^n}} \sum_{k=0}^{2^n - 1} e^{2\pi i \frac{2^n \theta}{2^n} k} |k\rangle \right) = |2^n \theta\rangle$$





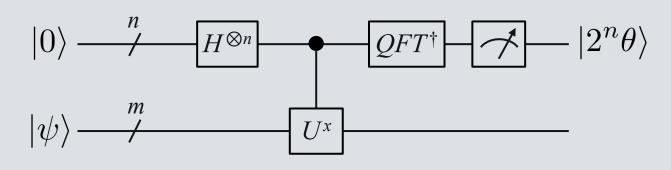
$$H$$
: Hadamard gate

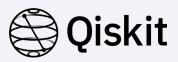
$$H\left(\frac{|0\rangle - |1\rangle}{\sqrt{2}}\right) = H\left(\frac{|0\rangle + e^{2\pi i \frac{1}{2}1} |1\rangle}{\sqrt{2}}\right) = \left|2^1 \cdot \frac{1}{2}\right\rangle = |1\rangle$$

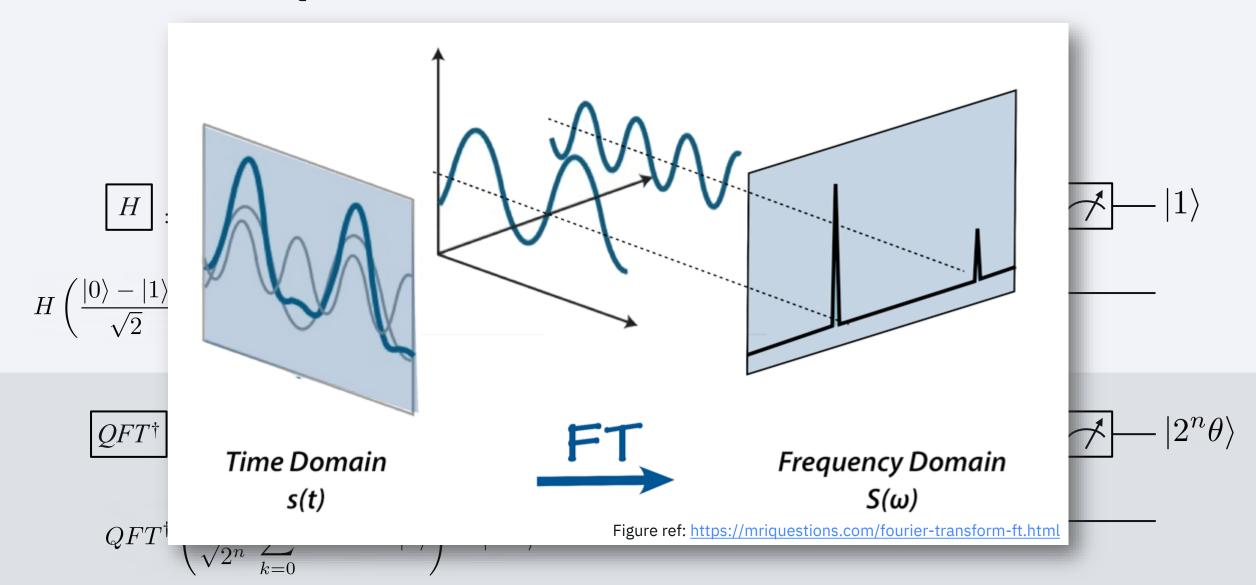
$$|0\rangle$$
 H H $|1\rangle$ $|1\rangle$

 QFT^{\dagger} : Quantum Fourier Transform (inversed)

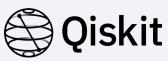
$$QFT^{\dagger} \left(\frac{1}{\sqrt{2^n}} \sum_{k=0}^{2^n - 1} e^{2\pi i \frac{2^n \theta}{2^n} k} |k\rangle \right) = |2^n \theta\rangle$$





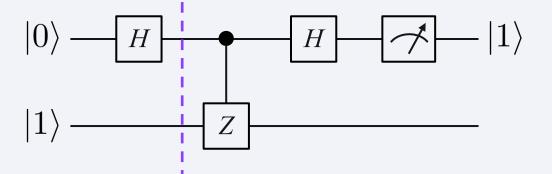


Superposition



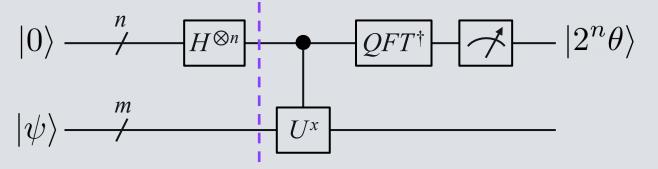
$$|0\rangle |1\rangle$$

$$\xrightarrow{H \otimes I} \left(\frac{|0\rangle + |1\rangle}{\sqrt{2}}\right) |1\rangle = \frac{|0\rangle |1\rangle + |1\rangle |1\rangle}{\sqrt{2}}$$

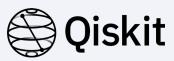


$$|0\rangle^{\otimes n} |\psi\rangle$$

$$\xrightarrow{H^{\otimes n} \otimes I} \frac{1}{\sqrt{2^n}} \left(\sum_{k=0}^{2^n - 1} |k\rangle \right) |\psi\rangle$$



Phase Kickback

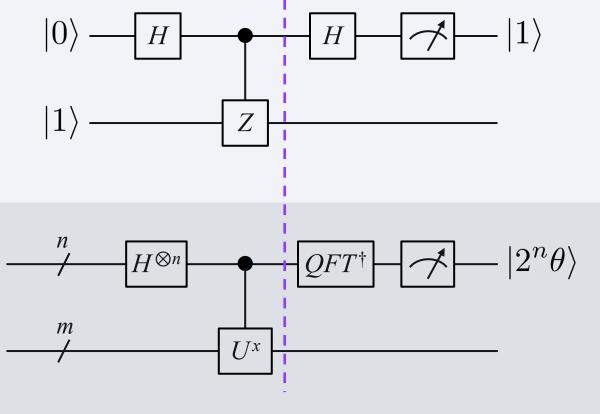


$$\left(\frac{|0\rangle + |1\rangle}{\sqrt{2}}\right)|1\rangle$$

$$\frac{CZ}{\sqrt{2}} \left(\frac{|0\rangle - |1\rangle}{\sqrt{2}}\right)|1\rangle$$

$$\frac{1}{\sqrt{2^n}} \left(\sum_{k=0}^{2^n - 1} |k\rangle \right) |\psi\rangle$$

$$\xrightarrow{CU} \frac{1}{\sqrt{2^n}} \left(\sum_{k=0}^{2^n - 1} e^{2\pi i \theta k} |k\rangle \right) |\psi\rangle$$



Quantum Fourier Transform



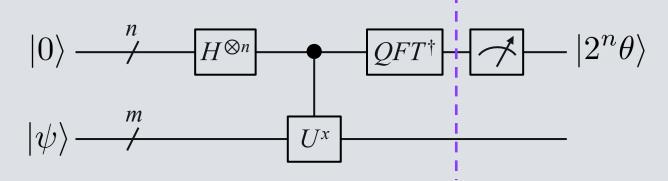
$$\left(\frac{|0\rangle - |1\rangle}{\sqrt{2}}\right)|1\rangle$$

$$\xrightarrow{H\otimes I} |1\rangle |1\rangle$$

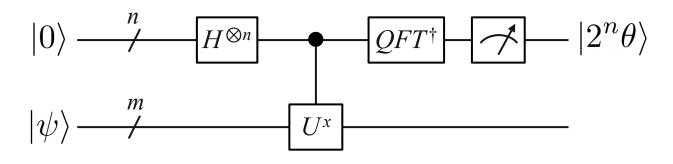
$$|0\rangle$$
 H $|1\rangle$ $|1\rangle$

$$\frac{1}{\sqrt{2^n}} \left(\sum_{k=0}^{2^n - 1} e^{2\pi i \theta k} |k\rangle \right) |\psi\rangle$$

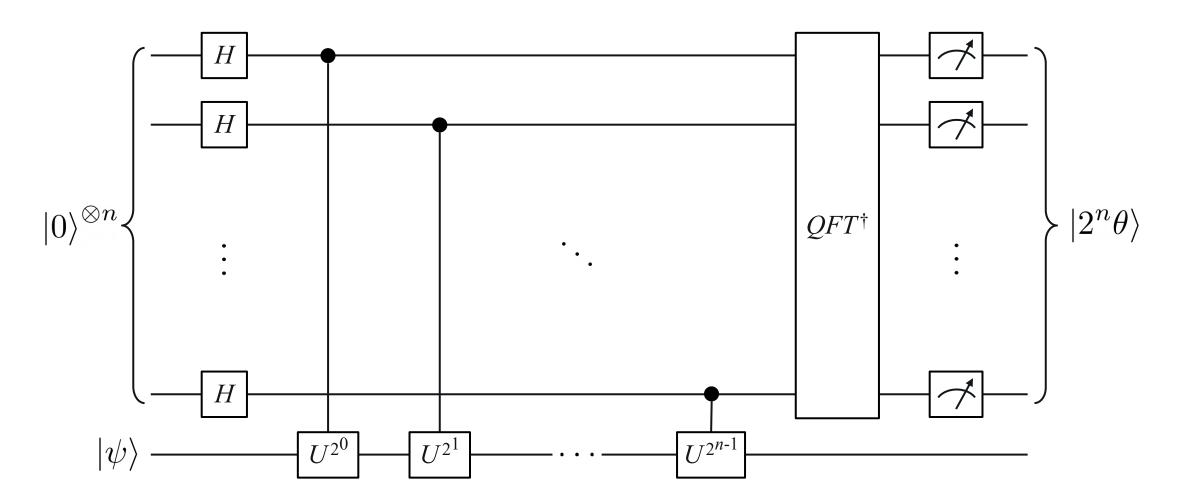
$$\xrightarrow{QFT^{\dagger}} \frac{1}{2^n} \left(\sum_{x,k=0}^{2^n - 1} e^{-\frac{2\pi i k}{2^n} (x - 2^n \theta)} |x\rangle \right) |\psi\rangle = |2^n \theta\rangle |\psi\rangle \qquad |\psi\rangle \xrightarrow{m}$$



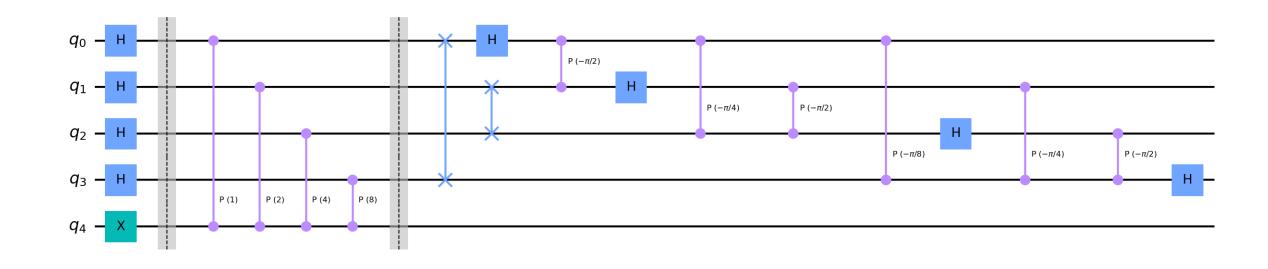










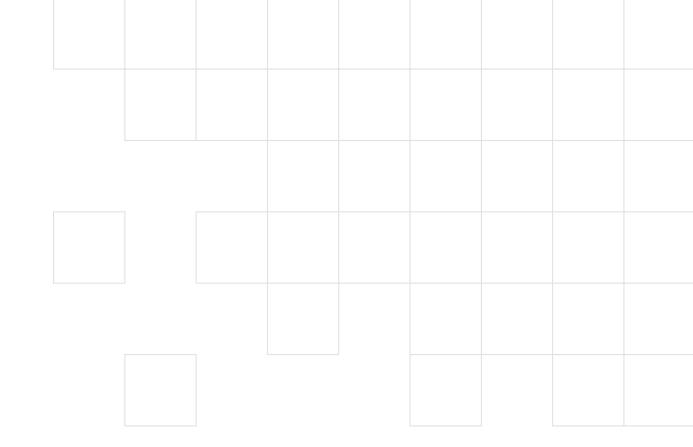


Thank you

Boseong Kim MSc Student, Dept of Physics, UCL

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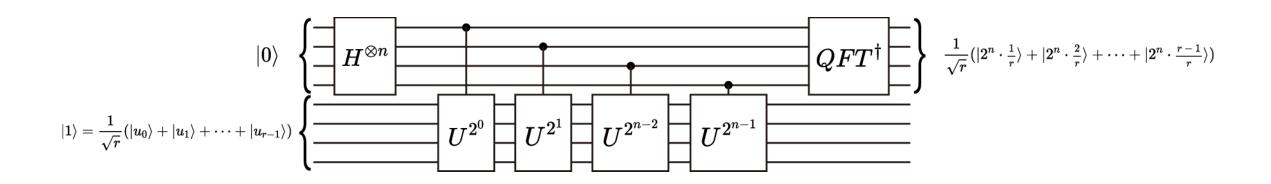
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Shor's Algorithm

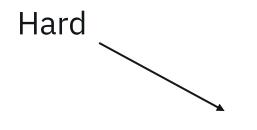




Answering question vs Building algorithm

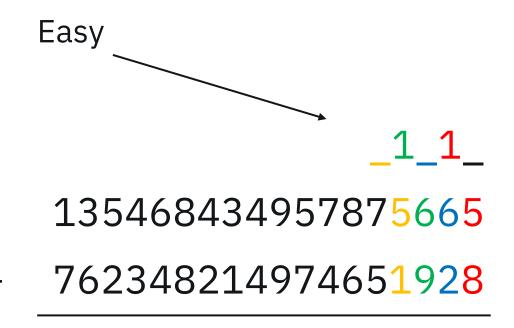


.7593



135468434957875665

+ 762348214974651348



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Quantum Fourier Transform



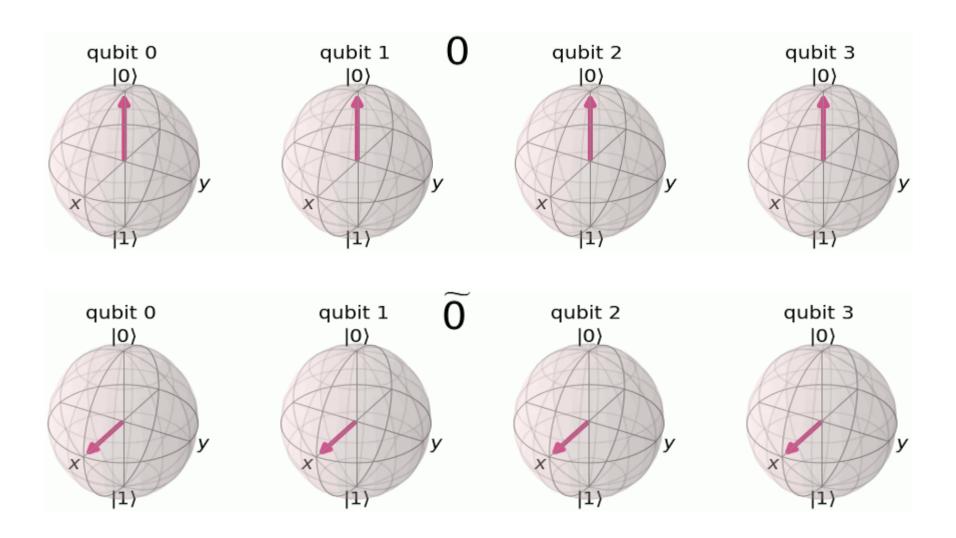


Figure ref: https://qiskit.org/textbook/ch-algorithms/quantum-fourier-transform.html