

Specifying and synthesizing Shield logically using DCSYNTH

Amol Wakankar, Paritosh K. Pandya and Raj Mohan Matteplackel

1 Formalization

Different notions of shield synthesis can be specified using hard and soft goals in DCSYNTH. We give several such definitions below. In the following, given a set of variables

- Conservative burst error shield.
 - Input: $I \cup O$. Output: $O1$
 - Hard requirement: $\text{REQ}[0/01]$
 - Soft requirement: $\bigwedge_{o \in O} (\text{true} \wedge \langle o=01 \rangle)$
- Conservative k -shield-V1
 - Input: $I \cup O$. Output: $O1$
 - Hard requirement: $\text{REQ}[0/01] \&\& [] ([[\bigvee_{o \in O} (o \neq 01)]] \Rightarrow \text{slen} < k)$.
- Conservative k -shield-V2.
 - Input: $I \cup O$. Output: $O1$
 - Hard requirement: $\text{REQ}[0/01] \&\& [] ([[\text{ind} \ \&\& \ \bigvee_{o \in O} (o \neq 01)]] \Rightarrow \text{slen} < k)$.
 - Indicator $\text{ind} : \text{REQ}(I, O)$
- Conservative k -shield-V3.
 - Input: $I \cup O$. Output: $O1$
 - Hard requirement: $\text{REQ}[0/01] \&\& [] ([[\text{ind} \ \&\& \ \bigvee_{o \in O} (o \neq 01)]] \Rightarrow \text{slen} < k)$.
 - Indicator $\text{ind} : \text{exists } O2. ((([O2=01] \ || \ \text{pt}) \wedge \langle O2=0 \rangle) \ \&\& \ \text{REQ}(I, O2))$

2 Experiments

In this section we give the time and the states for the following formulas for each shield.

- $\varphi_0 = \mathcal{G} \neg q \vee \mathcal{F}_{<=n}(q \wedge \mathcal{F}_{<=n} p)$. The corresponding QDDC formula is given by $[[!q]] \ || \ (\text{slen} \leq n) \wedge \langle q \rangle \wedge (\text{slen} \leq n) \wedge \langle p \rangle \wedge \text{true}$.
- $\varphi_1 = \mathcal{G} \neg q \vee \mathcal{F}_{<=n}(q \wedge \mathcal{F}_{<=n} p)$. The corresponding QDDC formula is given by $[[!q]] \ || \ \text{pref}((\text{slen} \leq n) \wedge \langle q \rangle \wedge (\text{slen} \leq n) \wedge \langle p \rangle \wedge \text{true})$.

- $\varphi_2 = \mathcal{G}((q \wedge \neg r) \Rightarrow \neg r \mathcal{U}_{\leq n}(p \wedge \neg r))$. The corresponding QDDC formula is $\Box((\langle q \rangle \ \&\& \ !r \rangle \wedge \text{true}) \Rightarrow ((([\![r]\!] \mid \text{pt}) \ \&\& \ \text{slen} \leq n) \wedge \langle p \ \&\& \ !r \rangle \wedge \text{true}) \mid ([\![r]\!] \ \&\& \ \text{slen} < n))$.
- $\varphi_3 = \mathcal{G}((x \Rightarrow y \vee z) \wedge ((z \wedge \mathcal{X}^n \text{true}) \Rightarrow \mathcal{X} \mathcal{G}_{=n}!z))$. The corresponding QDDC formula is $\Box((\langle x \rangle \Rightarrow \langle y \mid z \rangle) \ \&\& \ (\{\{z\}\} \wedge (\text{slen} == n) \Rightarrow (\text{slen} == 1) \wedge [\![z]\!])))$.
- $\varphi_4 = G_1 \wedge G_2 \wedge G_3$ where
 - $G_1 = \mathcal{G}(HREADY \Rightarrow \mathcal{X} START)$.
QDDC equivalent of G_1 is $\Box(\{\{!HREADY\}\} \Rightarrow (\text{slen} == 1) \wedge \langle !START \rangle)$.
 - $G_2 = \mathcal{G}((HMASTLOCK \wedge (HBURST = INCR) \wedge START \wedge HMASTERi) \Rightarrow \mathcal{X}(\neg START \text{ Unless } \neg HBUSREQi))$.
QDDC formula of G_2 is roughly $\forall i \in \{0, 1\} : \Box(\{\{HMASTLOCK \ \&\& \ INCR \ \&\& \ START \ \&\& \ HMASTERi\}\} \wedge \text{true} \Rightarrow (\text{slen} == 1) \wedge ([\![START]\!] \mid [\![!START]\!] \wedge \langle !HBUSREQi \rangle \wedge \text{true}))$.
 - $G_3 = \mathcal{G}((HMASTLOCK \wedge HBURST = BURST4 \wedge START) \Rightarrow ((HREADY \wedge \mathcal{X}(\neg START \mathcal{U}_3 HREADY)) \wedge (\neg HREADY \wedge \mathcal{X}(\neg START \mathcal{U}_4 HREADY))))$.
QDDC formula is $\Box(\langle HMASTLOCK \ \&\& \ BURST4 \ \&\& \ START \rangle \wedge \text{true} \Rightarrow (\{\{HREADY\}\} \wedge ([\![HREADY]\!] \mid ([\![!START]\!] \ \&\& \ (\text{scount HREADY} == 3)) \wedge \text{true})) \mid (\{\{!HREADY\}\} \wedge ([\![HREADY]\!] \mid ([\![!START]\!] \ \&\& \ (\text{scount HREADY} == 4)) \wedge \text{true})))$.

| Shield | Formula | n | k | States | Time |
|-------------|-------------|-----|-----|--------------|-------|
| burst error | φ_0 | 16 | - | 36 | 1.404 |
| | φ_1 | 16 | - | 4 | 1.372 |
| | φ_2 | 12 | - | 14 | 0.064 |
| | φ_3 | 4 | - | 7 | 0.012 |
| | φ_4 | - | - | 6 | 0.056 |
| K-Shield V1 | φ_0 | 16 | 1 | 19 | 1.428 |
| | φ_1 | 16 | 1 | 3 | 1.424 |
| | φ_2 | 12 | 1 | 14 | 0.068 |
| | φ_3 | 4 | 4 | Unrealizable | 0.016 |
| | φ_4 | - | 1 | Unrealizable | 0.016 |
| K-Shield V2 | φ_0 | 16 | 1 | 174 | 1.516 |
| | φ_1 | 16 | 1 | 6 | 1.512 |
| | φ_2 | 12 | 1 | 27 | 0.160 |
| | φ_3 | 4 | 4 | 16 | 0.052 |
| | φ_4 | - | 1 | 24 | 0.460 |
| K-Shield V3 | φ_0 | 16 | 1 | 20 | 2.736 |
| | φ_1 | 16 | 1 | 4 | 2.636 |
| | φ_2 | 12 | 1 | 14 | 0.108 |
| | φ_3 | 4 | 4 | 7 | 0.036 |
| | φ_4 | - | 1 | 12 | 0.132 |

Table 1: Experiments for various shield synthesis notions.