



Energy systems modelling

Tutorial 6

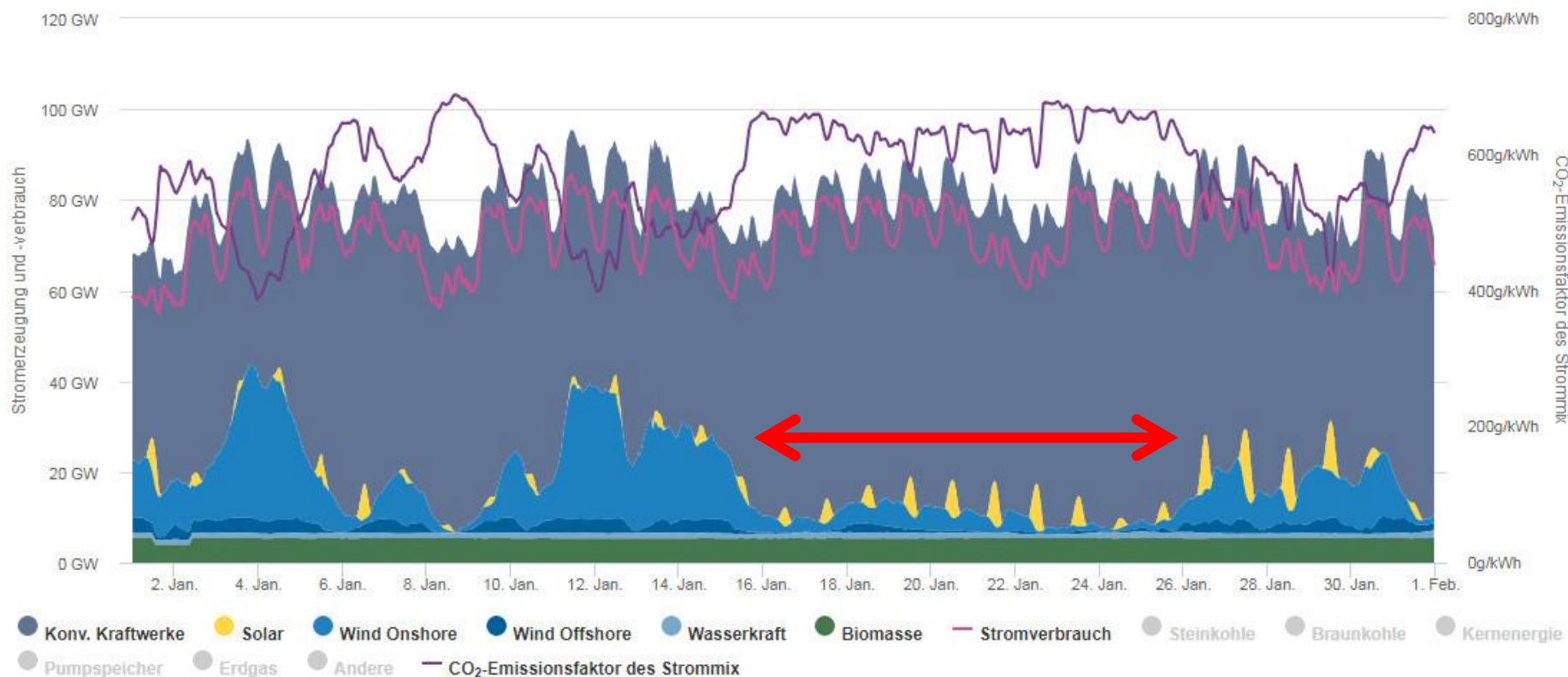
Iegor Riepin

Intertemporal dynamics

Intertemporal dynamics - a decision made at one time step has an effect on the optimal decisions in other time steps

- ♦ Q: What are the causes of intertemporal dynamics in electricity markets?
 - **Energy storages**
 - Investment decisions
 - Start-up constraints
 - Partial-load costs
 - Start-up costs

“Dunkelflaute”: German term for the co-occurrence of ‘Dunkelheit’ (darkness) and ‘Windflaute’ (windlessness)



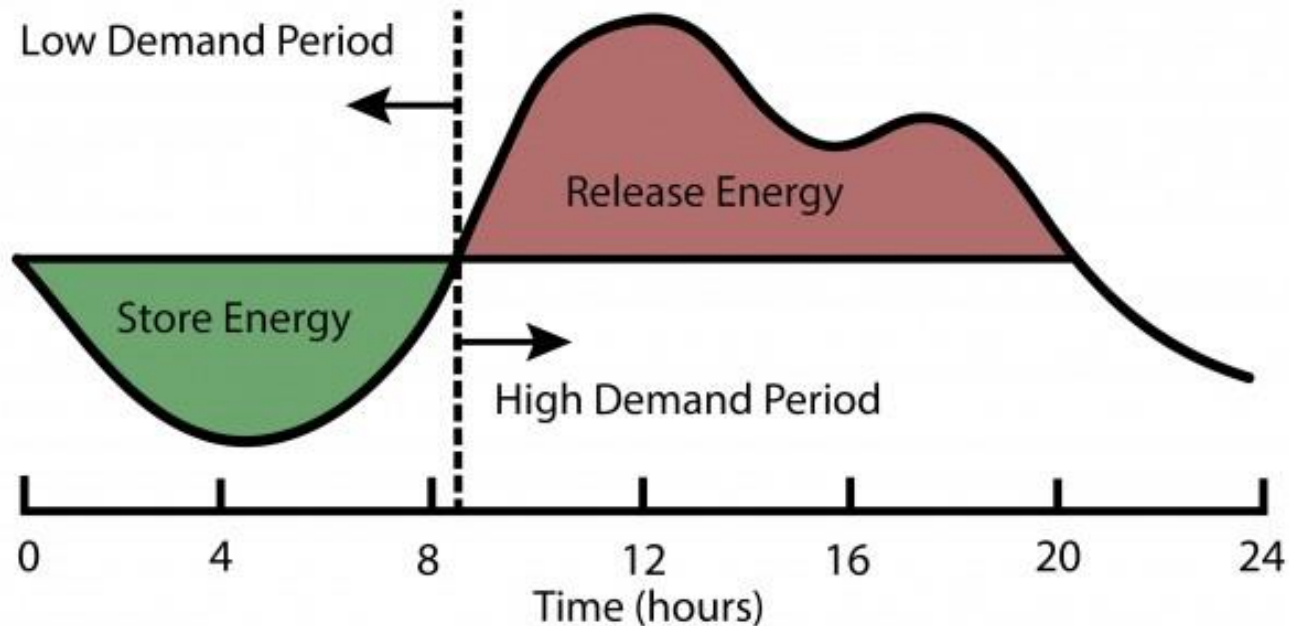
January 2017, 10 days of “Dunkelflaute”

source: Agora Energiewende

https://www.agora-energiewende.de/service/agorameter/chart/power_generation/01.01.2017/31.01.2017/

Illustration of storage activity

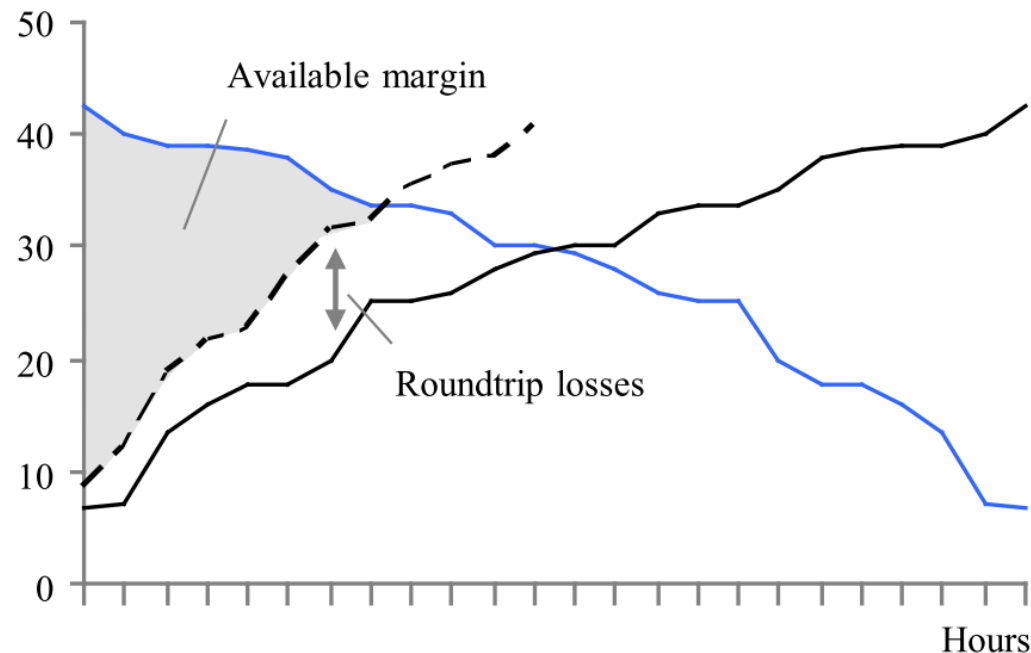
- Storing energy during low demand (off-peak periods) and using that energy during high demand (on-peak periods)



Source: U.S. Grid energy storage factsheet
<http://css.umich.edu/factsheets/us-grid-energy-storage-factsheet>

Illustration of time spread margin

Price duration curves EPEX Spot, 01/08/2010
€/MWh



- (a) Hourly prices in decreasing order = **generation revenues**
- (b) Hourly prices in increasing order
- - (c) Prices (b) after 20% roundtrip losses = **pumping costs**

Discussion: What are the other revenue sources (in addition to energy arbitrage at a spot market) for energy storage?

Source: Steffen, Bjarne, Prospects for Pumped-Hydro Storage in Germany (December 8, 2011). EWL Working Paper No. 07/2011.

<http://dx.doi.org/10.2139/ssrn.1969767>

Implementing energy storage

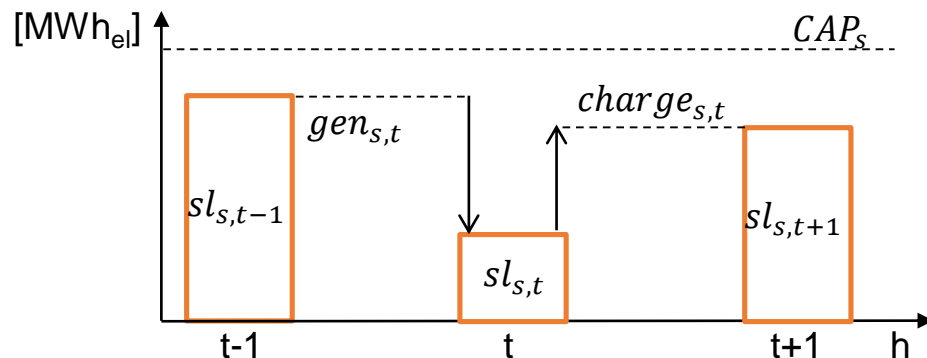
Storages – mathematical description on the electricity market

Defining a storage level of a storage s at time t :

$$sl_{s,t} = sl_{s,t-1} + charge_{s,t} - gen_{s,t} \quad \forall s, t$$

Defining maximum storage capacity:

$$sl_{s,t} \leq CAP_s \quad \forall s, t$$



New index:

s index for storage technologies

New parameters:

CAP_s storage capacity [MWh]

$POWER_X_s$ generation/charging power [MW]

New variables:

$sl_{s,t}$ storage level [MWh]

$charge_{s,t}$ charging storage [MW]

$gen_{s,t}$ generation by storage [MW]

Implementing energy storage

Storages – mathematical description on the electricity market

Constraint for the charging/generation power:

$$charge_{s,t} \leq POWER_PUMP_s \quad \forall s, t$$

$$gen_{s,t} \leq POWER_TURB_s \quad \forall s, t$$

Constraint for the generation quantity:

$$gen_{s,t} \leq sl_{s,t-1} \quad \forall s, t$$

Non-negativity constraints:

$$0 \leq sl_{s,t}, gen_{s,t}, charge_{s,t} \quad \forall t$$

New index:

s index for storage technologies

New parameters:

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New variables:

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Implementing energy storage

Storages – mathematical description on the electricity market

2) Effects on the energy balance

$$\sum_c g_{c,t} + \sum_r g_{r,t} = DEMAND_t + \sum_s (charge_{s,t} - gen_{s,t} * (1 - LOSS_s)) \quad \forall t$$

Charging the storage increases demand for electricity

Losses in storage cycle
 (here: LOSS parameter represents the losses of the entire storage cycle)

See you next class!