OCaml: The Basics

Concepts of Programming Languages Lecture 2

Practice Problem

None today, instead we'll do a demo of the one of the functions from assignment 0 in a moment

Outline

- >> Briefly outline the use of **Dune**
- >> Cover the **basic expressions** we need to start programming in OCaml, look at some examples
- » Define more carefully the notion of an inference rule

Learning Objectives

- >> Write basic OCaml programs on primitive types
- » Read inference rules, i.e., translate formal mathematical notation to English and English to mathematical notation

Recap

Recap: Functional vs. Imperative

OCaml is a **functional language**. This means a couple things:

- >> No state (which means no loops!)
- >> We don't think of a program as describing a
 procedure, but as defining a value using an
 expression

Recap: Expressions

Expressions are <u>syntactic</u> objects which describe values in a program

Mneumonic: Expressions are

EValuated to Values

They appear in both functional and imperative PLs, but in functional PLs we only have expressions

$$2 + (2 * 3)$$

if x = 3 then 3 else 4

In fact, we'll often think of an OCaml program as a *single* expression (more on that in a moment)

```
Syntax: What a well-formed program in your PL?
```

```
def f():
    return 3
```

```
define f():
    3 return
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Semantics (Dynamic Semantics): What is the output of a (valid) program?





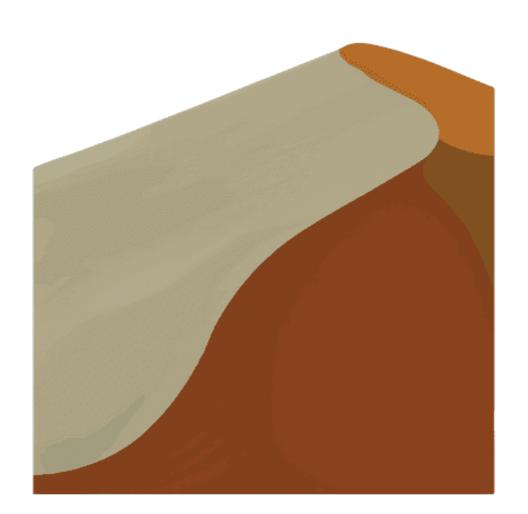


For every possible expression, we'll define the syntax rules, the typing rules, and the semantic rules

Working with OCaml



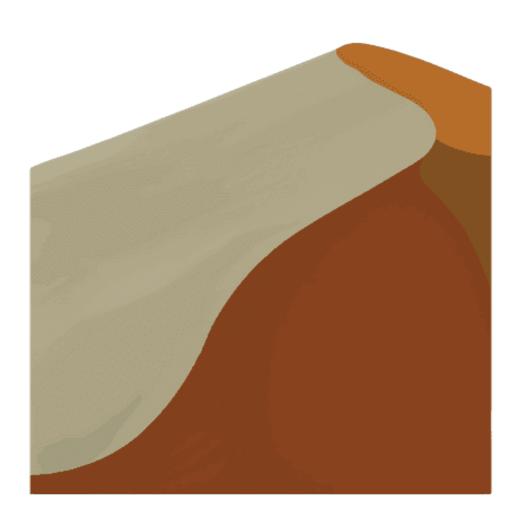
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DUNE

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It allows us to specify project-level dependencies and configurations

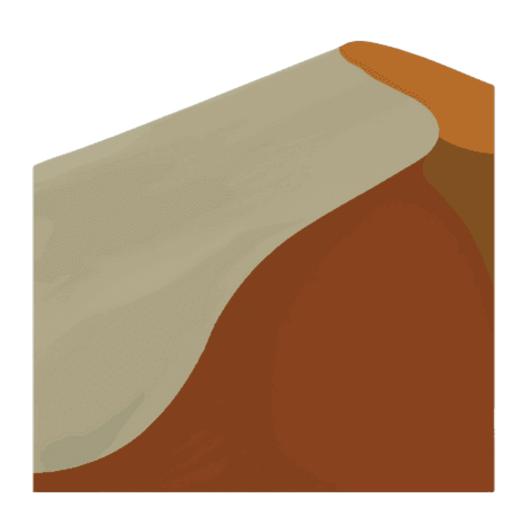




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We'll use it throughout the course for all assignments and projects

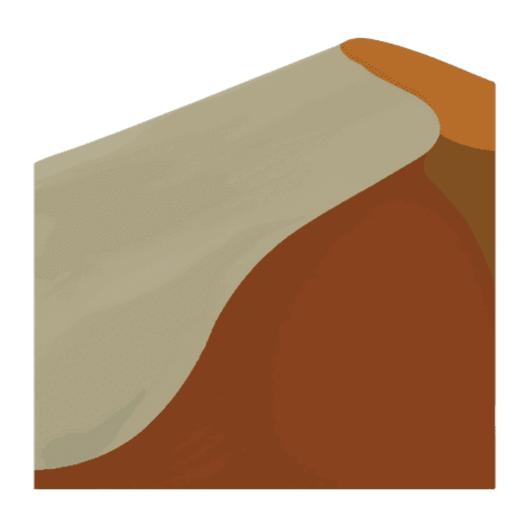




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Cheatsheet:



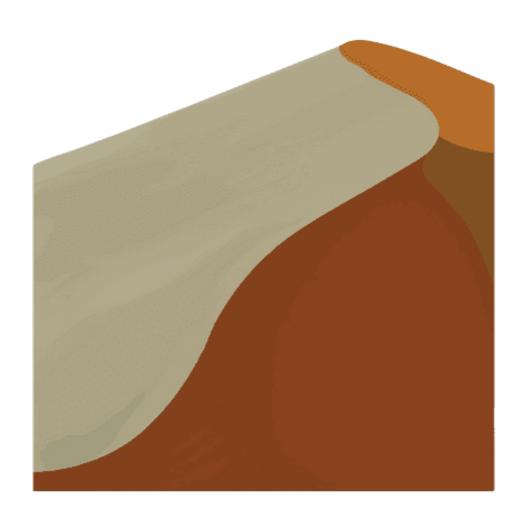


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>> dune build: type check your project



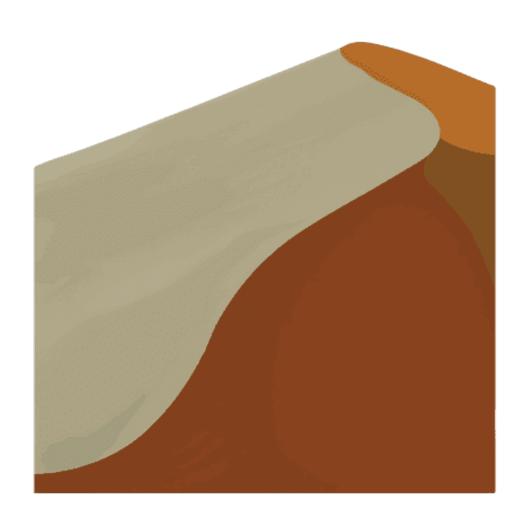


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- >> dune utop: open Utop in a project aware way



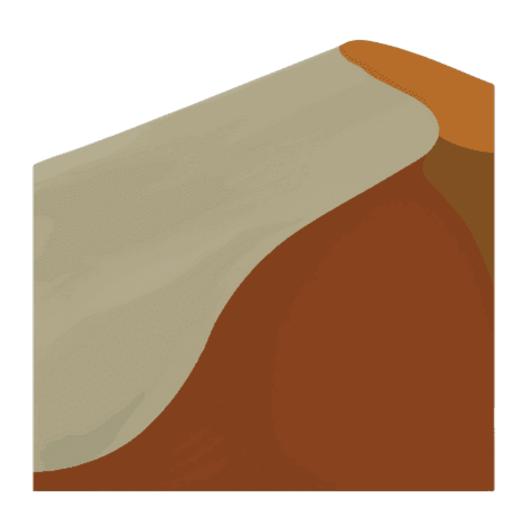
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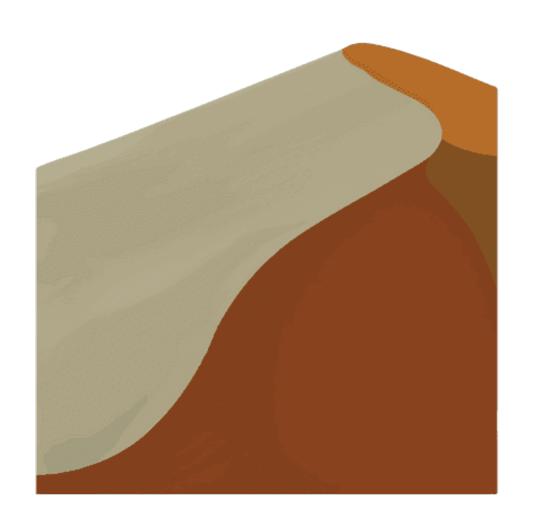


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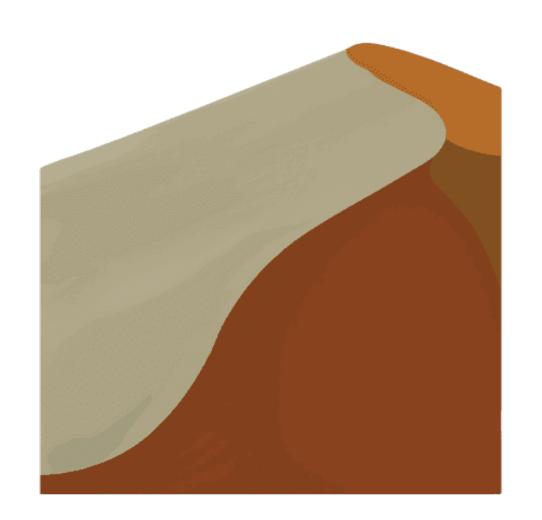
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- >> dune exec PROJ_NAME: run the executable of your project
- >> dune clean: removes files created by dune build (not so important but may come in handy)





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Findlib has been successfully loaded. Additional directi
 #require "package";;
                       to load a package
 #list;;
                       to list the available packag
 #camlp4o;;
                        to load camlp4 (standard syn
 #camlp4r;; to load camlp4 (revised synt
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                        to enable threads
Type #utop_help for help about using utop.
-( 23:00:06 )-< command 0
utop # 1 + 2;;
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- » #quit;; or (Ctl-D) leaves UTop

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We'll see how to do this much better later on...

demo

Expressions (Informally)

High Level View

<u>Values</u> are the things manipulated and output by programs, e.g., the integer 7 or the string "seven"

Expressions describe values (the values to which they evaluate

Example: The expression 2 + 7 "describes" the value 9

```
let x : int = 2
let y : string = "two"
let _ = x + y (* THIS IS NOT POSSIBLE *)
```

Error: This expression has type string but an expression was expected of type int

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Types restrict how expression can be constructed

Primitive Types and Literals

As with any PL, OCaml has a collection of standard types and literals

Type	Literals	Operators
int	0, -2, 13, -023	+, -, *, /, mod
float	3., -1.01	+.,, *., /.
bool	true, false	&&, , not
char	'b', 'c'	
string	"word", "@*&#"</th><th>^</th></tr></tbody></table>	

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Note that equality check is just = (not ==) and inequality is <> (not !=)

demo

A Note on Type Annotations

```
let rec fact (n : int) : int =
  if n <= 0
  then 1
  else n * fact (n - 1)</pre>
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Including type annotations can be useful for documentation and for code clarity (we will often do this to begin with)

let
$$x = 2$$
 in $x + x$

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Note that it reads like a sentence: let x stand for 2 in the expression x + x

Multiple Local Variables

```
def sum_of_squares(x, y):
    x_squared = x * x
    y_squared = y * y
    return x_squared + y_squared
```

Python

```
let sum_of_squares x y =
  let x_squared = x * x in
  let y_squared = y * y in
  x_squared + y_squared
```

0Cam1

It's very easy to use multiple local variables, we just nest local variables (If it helps, think of in as a semicolon;)

IMPORTANT: let x = e1 in e2 is an expression so it can be the body of a let expression.

Recall: Anatomy of an OCaml Program

```
let x = 3
let y = "string"

(* function definition *)
let square x = x * x

(* recursive function definition *)
let rec f x = if x = 0 then 0 else x + f (x - 1)

(* We can't just print , we assign to wildcard *)
let _ = print_endline("Hello world")
```

An OCaml Program consists of <u>top-level let-expressions</u>, i.e., it is a **collection of named expressions**

OCaml Programs are Expressions

```
let x = 3 in
let y = "string" in

(* function definition *)
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(* We can't just print , we assign to wildcard *)
let _ = print_endline("Hello world") in

0
```

This sequence of top-level let expressions is really shorthand for a **collection of nested local variables**

(This is a lie, but its a useful one for now)

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let x = 2 in x + x
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syntax: let VARIABLE = EXPRESSION in BODY

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semantics: the is the same as the value of BODY after substituting the VARIABLE in BODY

Example: III-Typed Let-Expression

An ill-typed expression will throw a type error when you try to evaluate it

Note that the body of a let-expression may be ill-typed depending on the value assigned to its variable

$$|et x = 2 in x + x| \longrightarrow 2 + 2$$

Formally, we write [v/x]e to mean "substitute v for x in e", e.g., [3/x](x+x) is the same as 3+3

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Intuitively, substitution is simple: replace the variable

Turns out, this is **very hard** to do correctly, it's subtle and a source of a lot of mistakes in PL implementations

demo

If-Expressions

```
let abs x = if x > 0 then x else -x
```

Note: OCaml is whitespace agnostic!

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As with any reasonable PL, OCaml has expressions for doing conditional reasoning

Note: The **else** case is required and the **then** and **else** cases must be the same type (why?)

If-Expressions

```
let foo x =
   if x < 0 then
      "negative"
   else if x = 0 then
      "zero"
   else
      "positive"</pre>
```

Answer: Remember, all we have is expressions. So every if-expression <u>must</u> have a value and a type (and therefore, an **else** case of the same type)

We can do **else if** just by nesting if-expressions! (neat)

Aside: If-Expressions in Python

```
if x < 0:
    return -1
else:
    return 1

if-stmt (Python)</pre>
```

```
return (-1 if x < 0 else 1)

if-expr (Python)
```

If-statements in Python are different from ifexpressions, but **both are available**

Statements don't have a value, expressions do

```
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Syntax: if CONDITION then TRUE-CASE else FALSE-CASE

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Syntax: if CONDITION then TRUE-CASE else FALSE-CASE

Typing: CONDITION must be a Boolean and TRUE-CASE and FALSE-CASE must be the same type. The type is then the same as that of TRUE-CASE and FALSE-CASE

Semantics: If CONDITION holds, then we get the TRUE-CASE, otherwise we get the FALSE-CASE

demo

Functions

```
let f x y z = x + y + z
let f (x : int) (y : int) (z : int) : int = x + y + z
```

There are a couple ways of defining functions in OCaml

So far, we've seen that let-expression can take arguments. How should we interpret this? If everything is an expression?

Anonymous Functions

let
$$f = fun x \rightarrow fun y \rightarrow fun z \rightarrow x + y + z$$

Answer: It must be that functions are expressions as well!

In OCaml, we can define anonymous functions, which are just **functions** without names

You should think of:

let
$$f x y z = x + y + z$$

as shorthand for the above

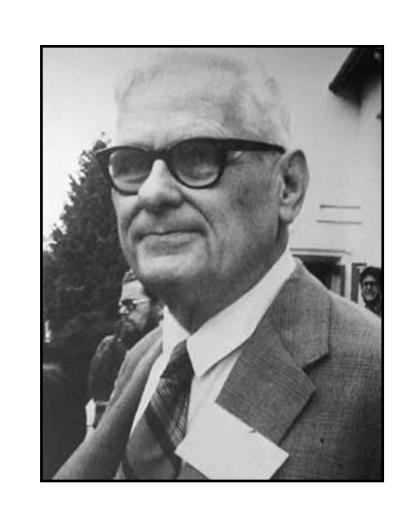
Aside: Anonymous Functions in Python

$$\lambda x \cdot x + 1$$
Math

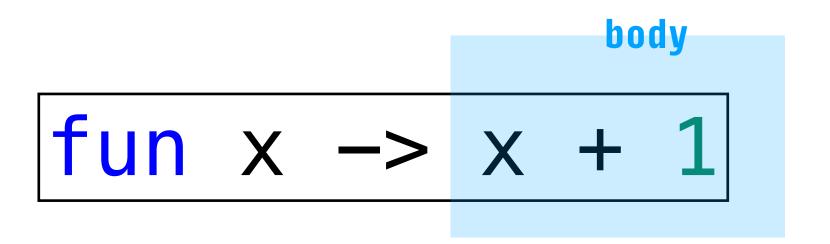
There are also anonymous function in Python!

They're called lambdas, based on the lambda calculus, a mathematical formulation of a functional PL that dates back to the 1930s, invented by Alonzo Church

(You'll find a lot of functional ideas hidden in languages like Python)



Functions (Informal)



Syntax: fun VAR-NAME -> EXPR

Typing: the type of a function is **T1 -> T2** where T1 is the type of the input and T2 is the type of the output

Semantics: A function will evaluate to special **function value** (printed as <fun> by UTop)

Important: Curried Functions

let
$$f = fun x \rightarrow fun y \rightarrow fun z \rightarrow x + y + z$$

The only kind of function we have is a single argument function

This seems restrictive, but ultimately it doesn't affect us at all

We can simulate multi-argument functions with nested functions. This is called **Currying** after Haskell Curry

Important: Curried Functions

```
let f = fun x \rightarrow fun y \rightarrow fun z \rightarrow x + y + z
```

We should think of the above function as something which takes an input and returns another function

In other words, we partially apply the function

Application

(fun x -> fun y -> x + y + 1) 3 2

Application is done by juxtaposition which means we put the arguments next to the function

Application is left-associative, which means we pass arguments from left to right

(fun x -> fun y -> x + y + 1) 3 2

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Syntax: FUNCTION-EXPR ARG-EXPR

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Typing: If FUNCTION-EXPR is of type T1 -> T2, and ARG-EXPR is of type T1, then the type is T2

Semantics: Substitute the value of ARG-EXPR into the body of FUNCTION-EXPR and evaluate that

(fun x -> fun y -> x + y + 1) 3 2

$$|(fun x -> fun y -> x + y + 1) 3 2|$$

Example:

Practice Problem

Implement a function **first digit** which takes an integer **n** as an input and returns the first digit of **n** (without converting to a string)

Expressions (Formally)

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<expr> ::= <expr> + <expr>
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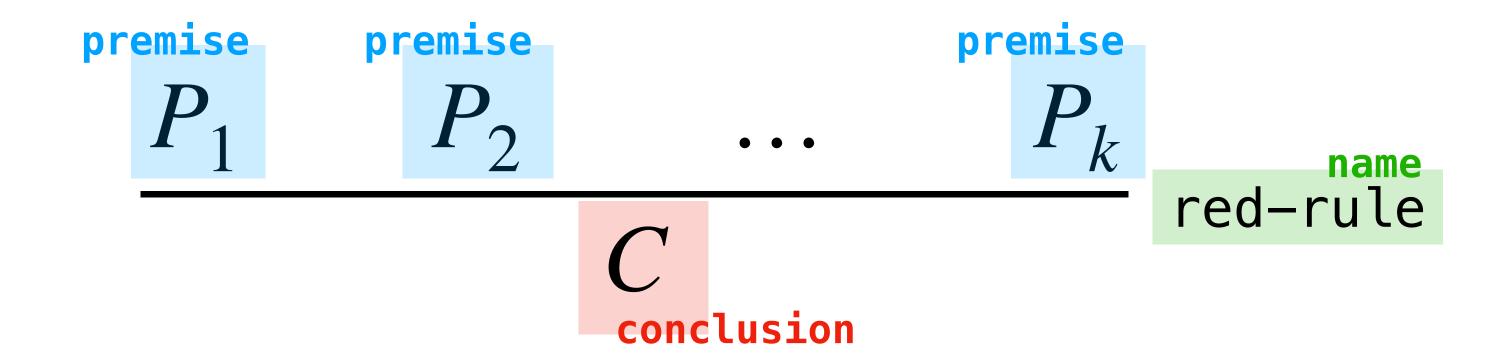
Reminder, this reads as: if e_1 is a well-formed expression and e_2 is a well-formed expression, then $e_1 + e_2$ is a well-formed expression

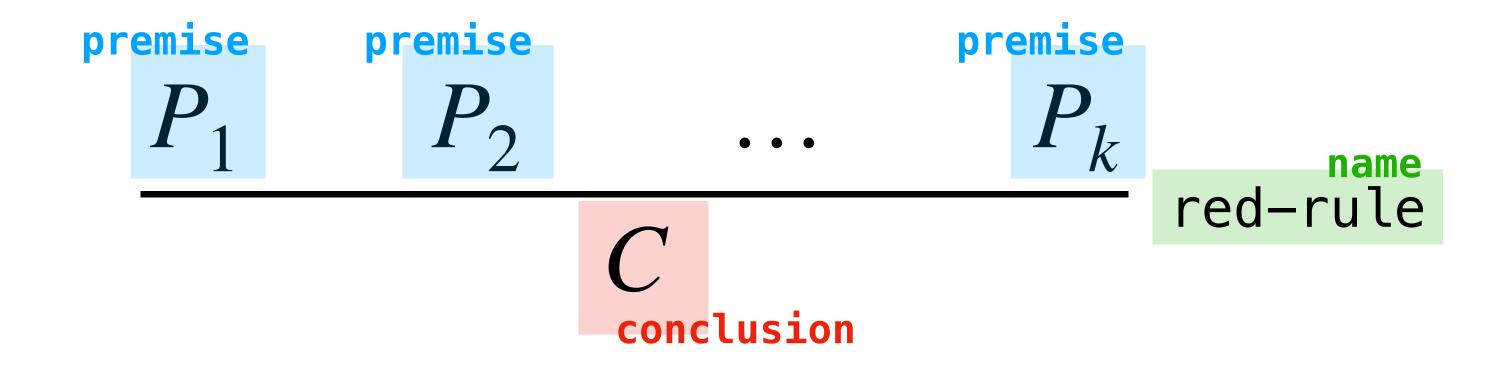
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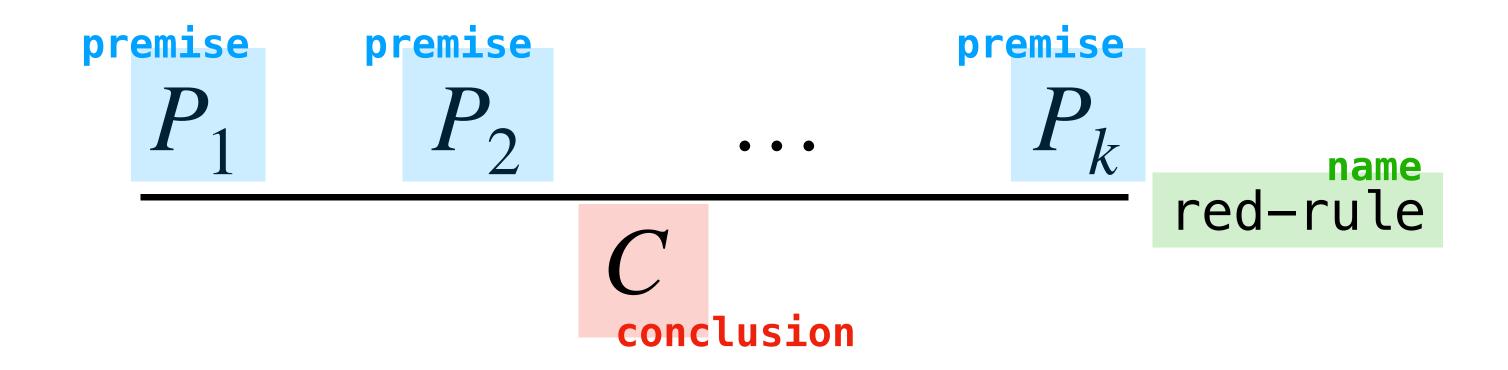
Reminder, this reads as: if e_1 is a well-formed expression and e_2 is a well-formed expression, then e_1+e_2 is a well-formed expression

We won't focus on this until the second half of the course but you should start to get comfortable with the syntax



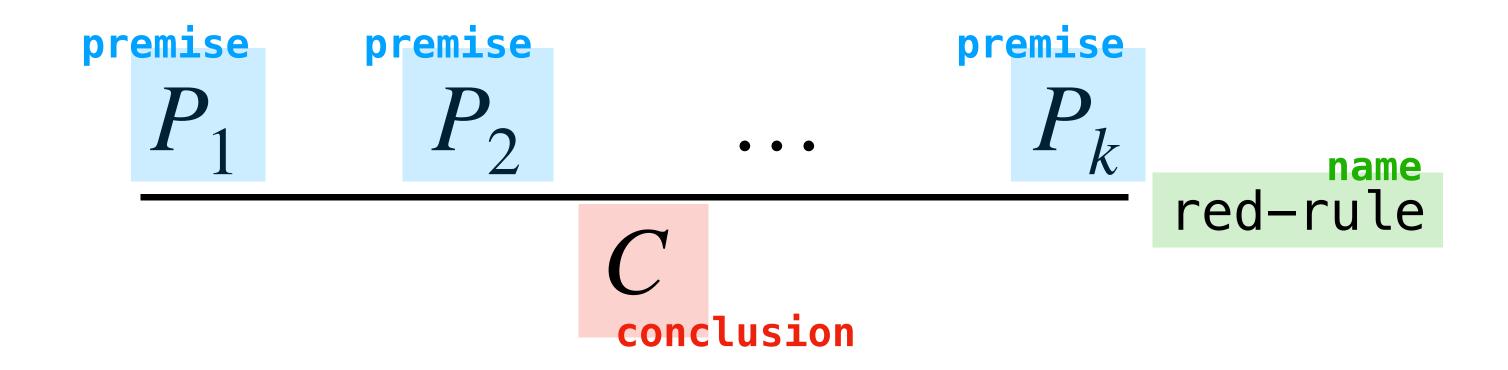


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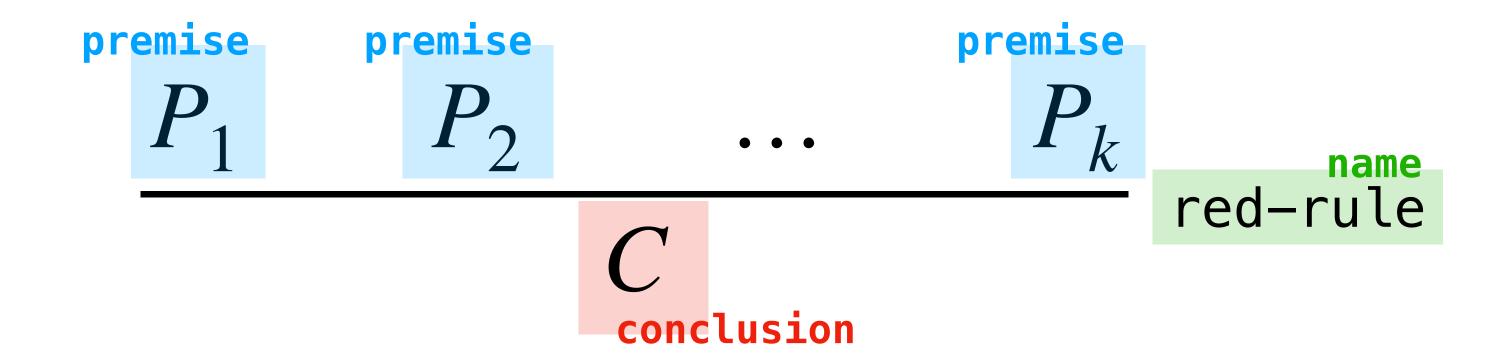
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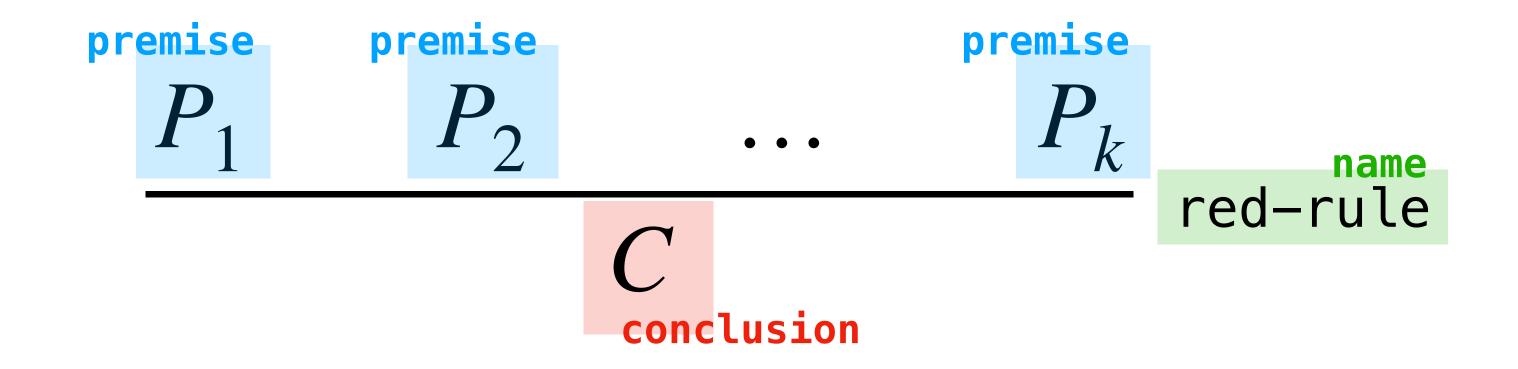


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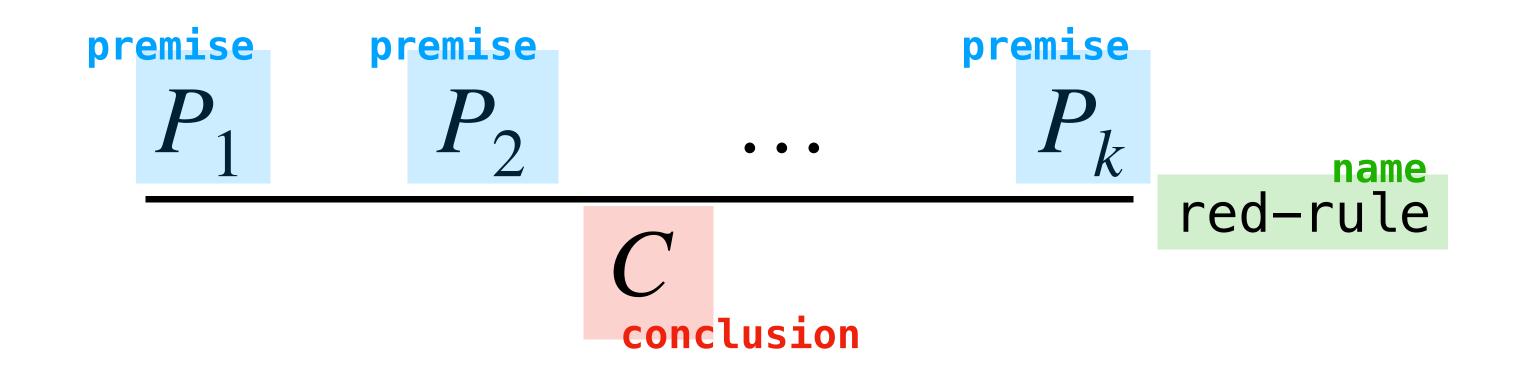
There may be no premises, this is called an axiom

Premises which are not of the same form as the conclusion are called **side-conditions**





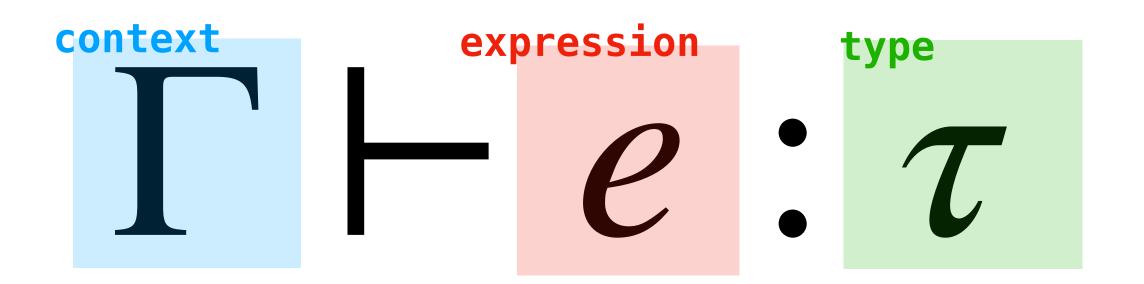
We can read this as:



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If P_1 through P_k hold, then C holds (by the **red-rule** rule).

Typing Judgments



A typing judgment a compact way of representing the statement:

e is of type au in the context Γ

A **typing rule** is an inference rule whose premises and conclusion are typing judgments

Recall: Integer Addition Typing Rule

$$\frac{\Gamma \vdash e_1 : \mathsf{int}}{\Gamma \vdash e_1 + e_2 : \mathsf{int}} \text{ (addInt)}$$

If e_1 is an int (in any context Γ) and e_2 is an int then (in any context Γ) e_1+e_2 is an int (in any context Γ)

```
\Gamma = \{ x : int, y : string, z : int -> string \}
```

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A context is a keeps track of all the types of variables in the "environment"

Example: Reading Typing Judgements

```
{b:bool} - if b then 2 else 3:int
```

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```
In English: Given I declare that b is a bool, the expression if b then 2 else 3 is an int
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Example: Reading Typing Judgements

{b:bool} - if b then 2 else 3:int

In English: Given I declare that b is a bool, the expression if b then 2 else 3 is an int

The context tells us what the types of variables need to be in order to be able to determine the type of the whole expression

```
{b:bool} H if b then 2 else 3:int
```

```
{b:bool} \ \text{if b then 2 else 3:int}
```

A judgement is a statement in the same way that "there are infinitely many twin primes" is a statement

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```

A judgement is a statement in the same way that "there are infinitely many twin primes" is a statement

We haven't proved anything by writing down a typing judgment

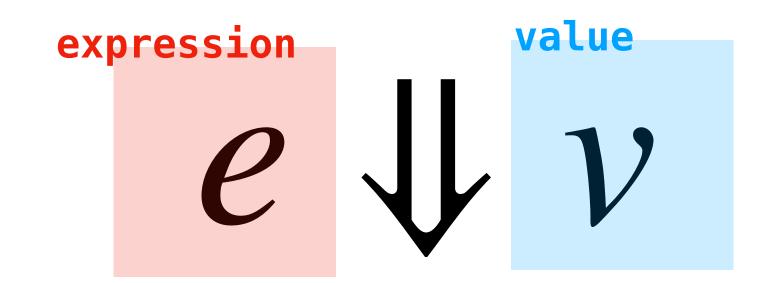
{b:bool} ⊢ if b then 2 else 3:int

A judgement is a statement in the same way that "there are infinitely many twin primes" is a statement

We haven't proved anything by writing down a typing judgment

Next week: We will talk about **typing derivations**, which are used to demonstrate that expressions actually have their desired types in our PL

Semantic Judgements



A <u>semantic judgment</u> is a compact way of representing the statement:

The expression e evaluates to the value v

A semantic rule is an inference rule with semantic judgments

Example: Reading Semantic Judgments

if 2 > 3 then 2 + 2 else $3 \Downarrow 3$

In English: The expression if 2 > 3 then 2 + 2 else 3
evaluates to the value 3

Note: we make a strong distinction between expressions and values

let's try formally specifying literals

Literal Syntax

```
<expr> ::= <int-lit> | true | false
```

We'll be a bit less formal about literal syntax (we'll see why this is the case when we talk about lexing)

For example, we'll say: An integer literal is a well-formed expression

(without saying what an integer literal actually is)

This rule allows to say that 23 is well-formed expression

That said, for booleans we can be formal: true and false are well-formed expressions

Literal Typing Rules

```
\frac{\text{rue:bool}}{\Gamma \vdash \text{true:bool}} \text{ (falseLit)}}{\frac{\text{n is an integer literal}}{\Gamma \vdash \text{n:int}}} \text{ (intLit)}
```

Literal Typing Rules

```
\frac{\Gamma \vdash \mathsf{true} : \mathsf{bool}}{\Gamma \vdash \mathsf{true} : \mathsf{bool}} \  \, \frac{\Gamma \vdash \mathsf{false} : \mathsf{bool}}{\Gamma \vdash \mathsf{false} : \mathsf{bool}} \  \, \frac{\mathsf{n} \  \, \mathsf{is} \  \, \mathsf{an} \  \, \mathsf{integer} \  \, \mathsf{literal}}{\Gamma \vdash \mathsf{n} : \mathsf{int}} \  \, (\mathsf{intLit})
```

Above are the typing rules for just Boolean and integers. Each rule expresses that a literal has its expected type in any context

Literal Typing Rules

```
\frac{}{\Gamma\vdash \mathsf{true}:\mathsf{bool}} \; (\mathsf{trueLit}) \\ \frac{}{\Gamma\vdash \mathsf{false}:\mathsf{bool}} \; (\mathsf{falseLit})
```

```
\frac{\text{n is an integer literal}}{\Gamma \vdash \text{n:int}} \text{ (intLit)}
```

Above are the typing rules for just Boolean and integers. Each rule expresses that a literal has its expected type in any context

Part in green is called a **side condition**. It's something that has to hold for the inference rule to make sense, but does not appear in the application of any rule (this will be more clear when we talk about derivations)

Literal Semantics Rules

$$\frac{\text{n is an integer literal}}{\text{n } \Downarrow n} \text{ (intLitEval)}$$

These rules express that literals evaluate to the values they denote

This takes some time to get used to but we're going to make a **strong distinction between expressions and values**

true does not evaluate to true (even though that's what UTop says) it evaluates the true Boolean value, which we will write as \top

```
and that's it, we've formally specified (integer and boolean) literals
```

We'll see more typing rules and semantic rules, we'll also give a written reference for the specification we'll talk about in class

Summary

- » OCaml is a language of expressions, everything is an expression
- » OCaml has everything we need to do basic programming
- We use inference rules to formally specify the behavior or typing and evaluation