CS460: Intro to Database Systems

Class 27: Log-Structured-Merge Trees

Instructor: Manos Athanassoulis

https://bu-disc.github.io/CS460/

Useful when?

- Massive dataset
- Rapid updates/insertions
- Fast lookups

LSM-trees are for you.

Why now?

Patrick O'Neil UMass Boston



Invented in 1996

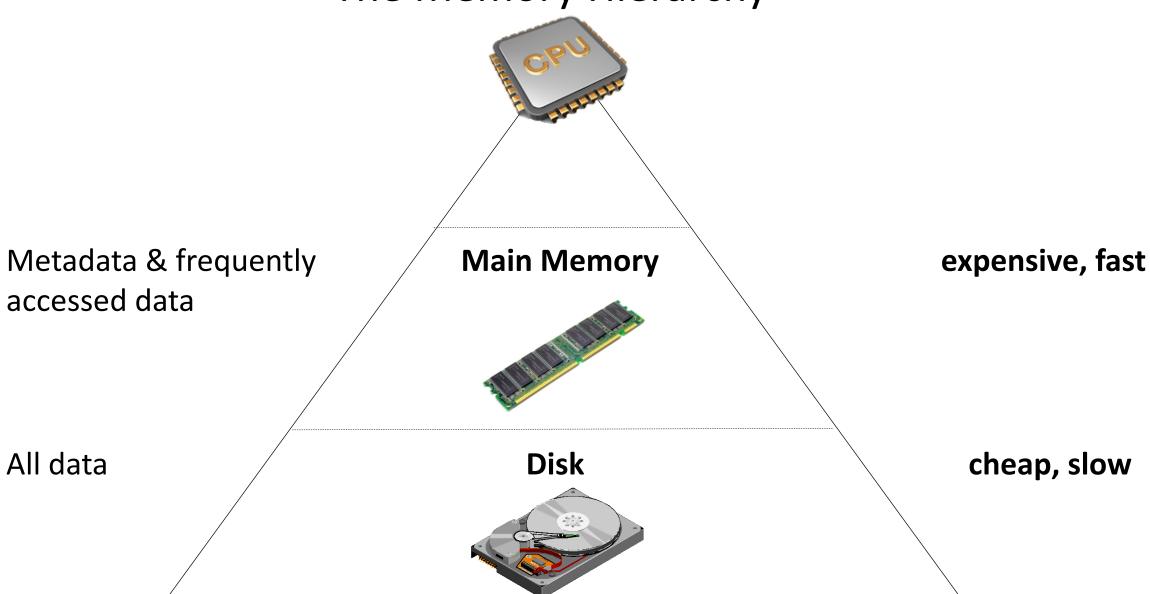


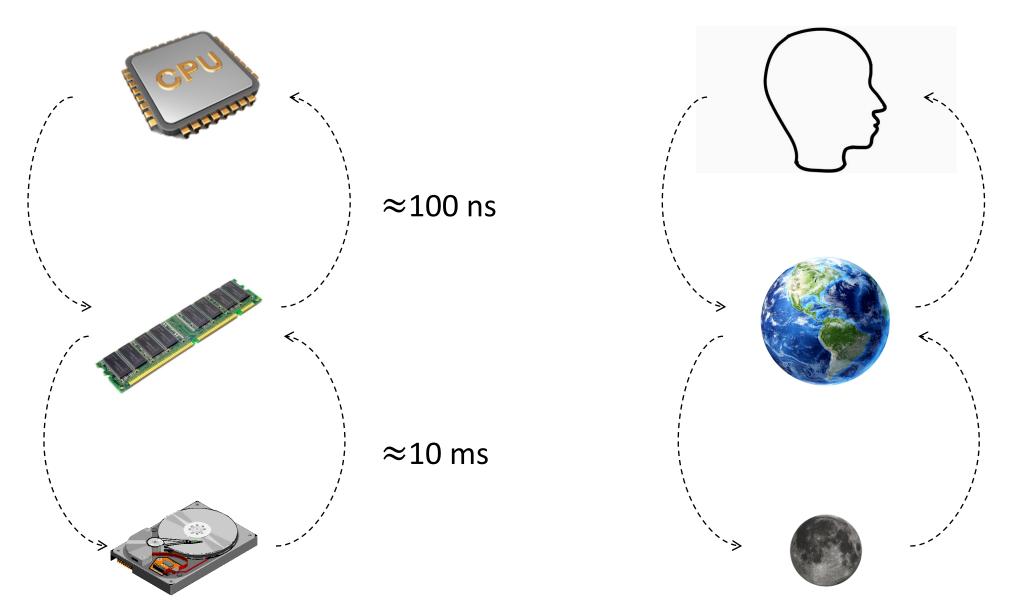
Outline

- 1. Storage devices
- 2. Indexing problem & basic solutions
- 3. Basic LSM-trees
- 4. Leveled LSM-trees
- 5. Tiered LSM-trees
- 6. Bloom filters

Storage devices

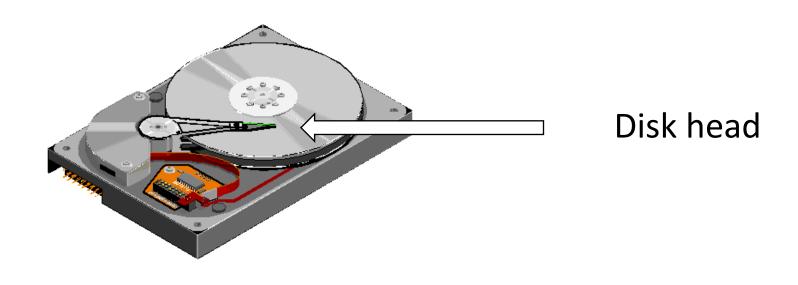
The Memory Hierarchy





≈5-6 order of magnitude difference

Why is disk slow?

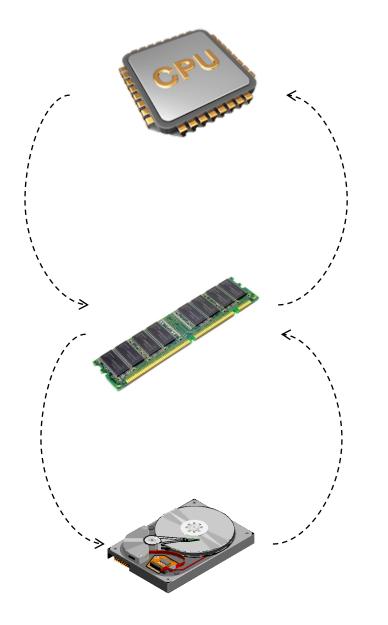


Random access is slow

Sequential access is faster

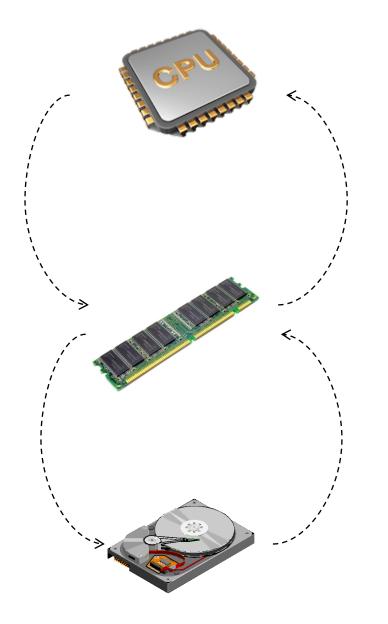
move disk head

> let disk spin



64 byte chunks Words Fine access granularity

4 kilobyte chunks Blocks **Coarse access granularity**



64 byte chunks Words Fine access granularity

4 kilobyte chunks **Blocks**

Coarse access granularity

Outline

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Indexing Problem & Basic Solutions

Indexing Problem



names phone numbers

Structure on disk?

Lookup cost?

Insertion cost?



Compare and contrast data structures.

What to use when?

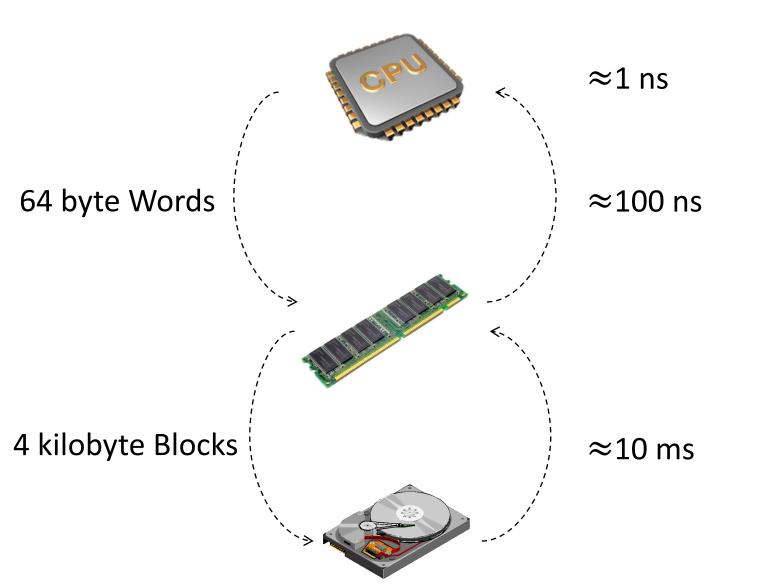
Data Structure	Lookup cost	Insertion cost
Sorted array		
Log		
B-tree		
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

Compare and contrast data structures.

What to use when?

Data Structure	Lookup cost	Insertion cost
Sorted array		
Log		
B-tree		
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

Modeling Performance



Measure bottleneck:

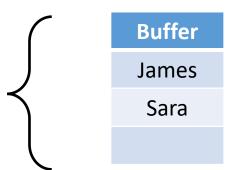
Number of block reads/writes (I/O)

Sorted Array

N entries

B entries fit into a disk block

Array spans **N/B** disk blocks



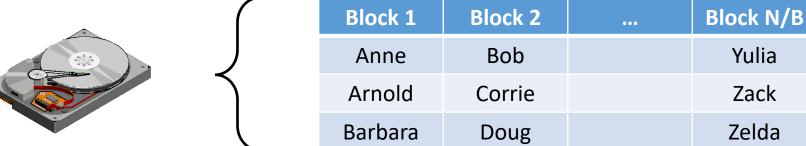
Lookup method & cost?

Binary search: $O\left(\log_2\left(\frac{N}{R}\right)\right)$

Insertion cost?

Push entries: $O\left(\frac{1}{B} \cdot \frac{N}{B}\right)$ I/Os

Array size	Pointer
	I





	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	$O(N/B^2)$
Log		
B-tree		
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

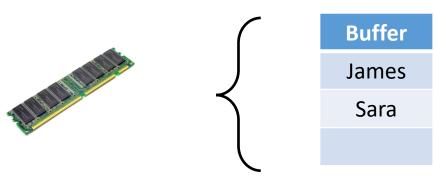
	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	$O(N/B^2)$
Log		
B-tree		
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

Log (append-only array)

N entries

B entries fit into a disk block

Array spans **N/B** disk blocks



Lookup method & cost?

Scan: $O\left(\frac{N}{B}\right)$

Insertion cost?

Append: $O\left(\frac{1}{B}\right)$

Array size	Pointer
	1

Block 1	Block 2	•••	Block N/B
Doug	Yulia		Anne
Zelda	Zack		Bob
Arnold	Barbara		Corrie



	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	$O(N/B^2)$
Log	O(N/B)	O(1/B)
B-tree		
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	$O(N/B^2)$
Log	O(N/B)	O(1/B)
B-tree		
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

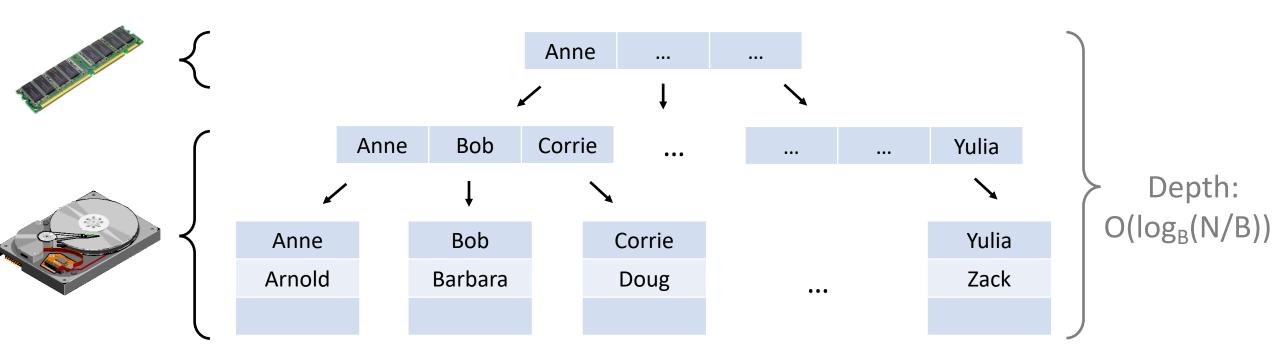
B-tree

Lookup method & cost?

Tree search: $O\left(\log_B\left(\frac{N}{B}\right)\right)$

Insertion method & cost?

Tree search & append: $O\left(\log_B\left(\frac{N}{B}\right)\right)$



	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	$O(N/B^2)$
Log	O(N/B)	O(1/B)
B-tree	$O(log_B(N/B))$	$O(log_B(N/B))$
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		

B-trees

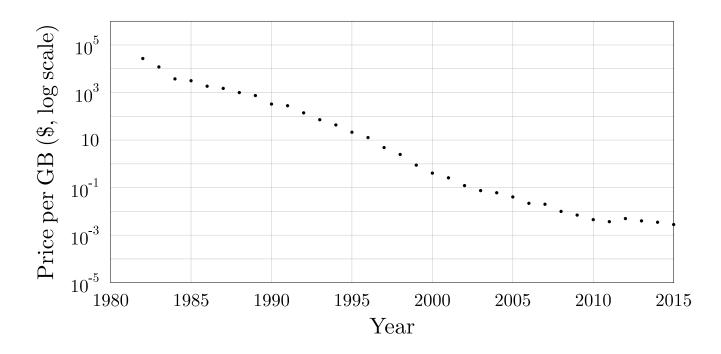


"It could be said that the world's information is at our fingertips because of B-trees"

Goetz Graefe Microsoft, HP Fellow, now Google ACM Software System Award

B-trees are no longer sufficient

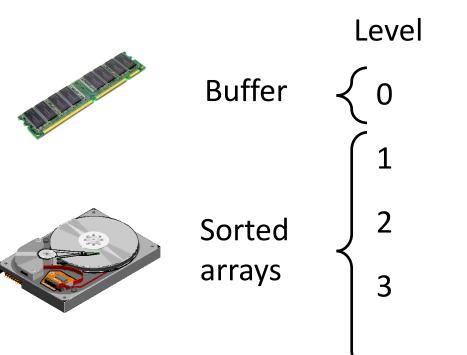
Cheaper to store data
Workloads more insert-intensive
We need better insert-performance.



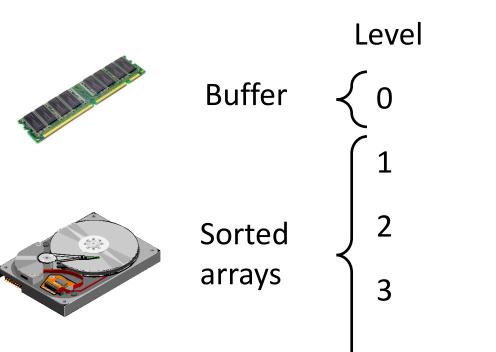
Goal to combine

sub-constant insertion cost logarithmic lookup cost

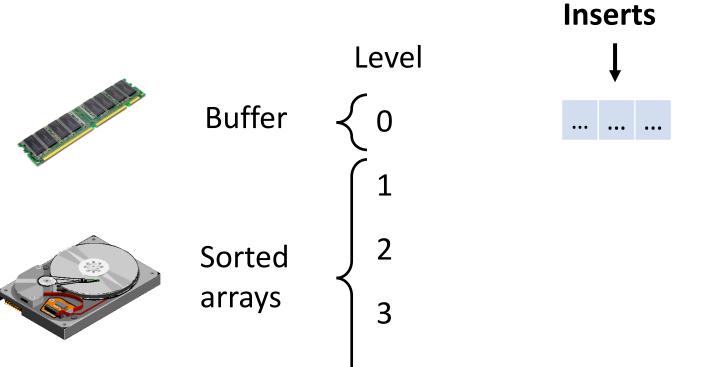
	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	$O(N/B^2)$
Log	O(N/B)	O(1/B)
B-tree	O(log _B (N/B))	$O(\log_B(N/B))$
Basic LSM-tree		
Leveled LSM-tree		
Tiered LSM-tree		



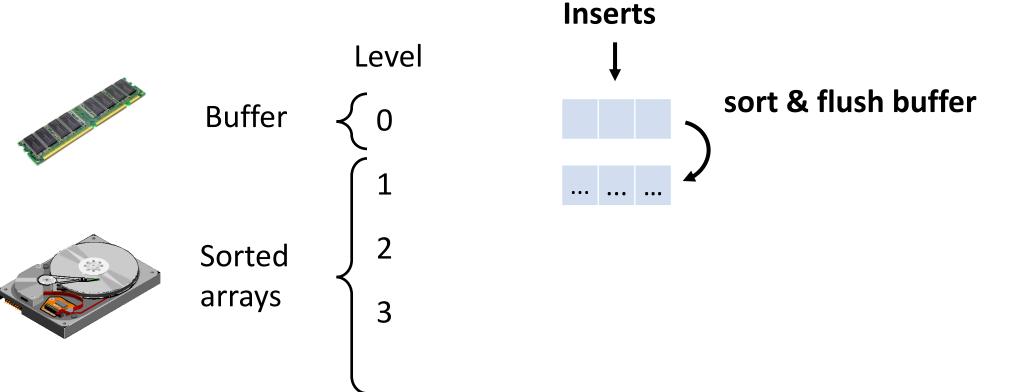
Design principle #1:



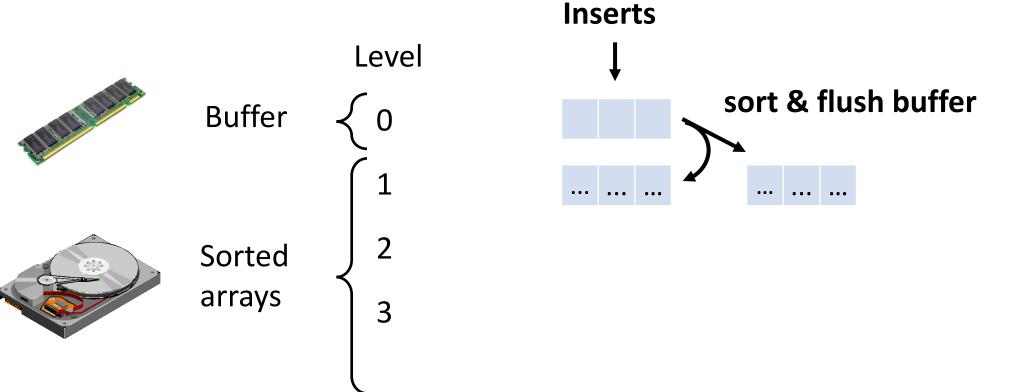
Design principle #1:



Design principle #1:



Design principle #1:

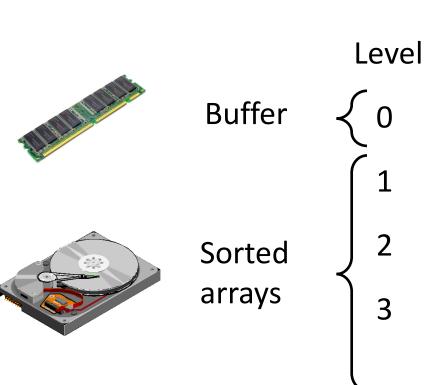


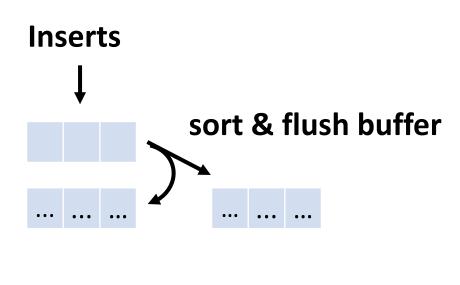
Design principle #1:

optimize for insertions by buffering

Design principle #2:

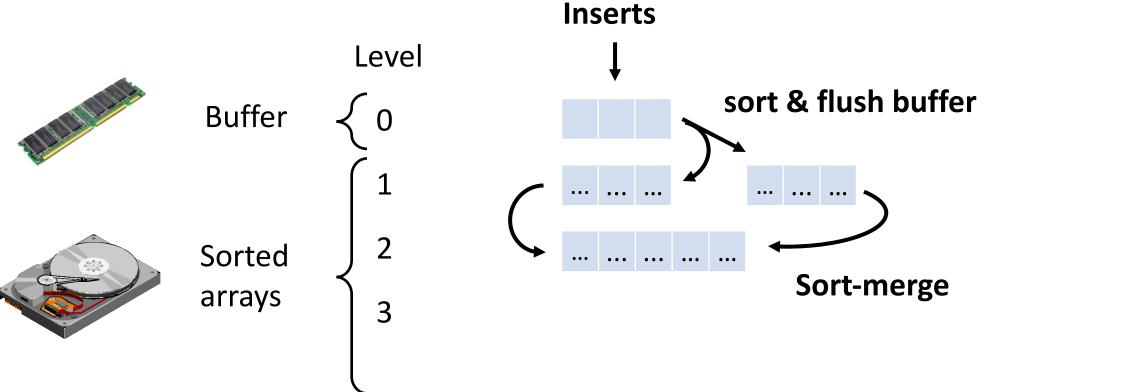
optimize for lookups by sort-merging arrays





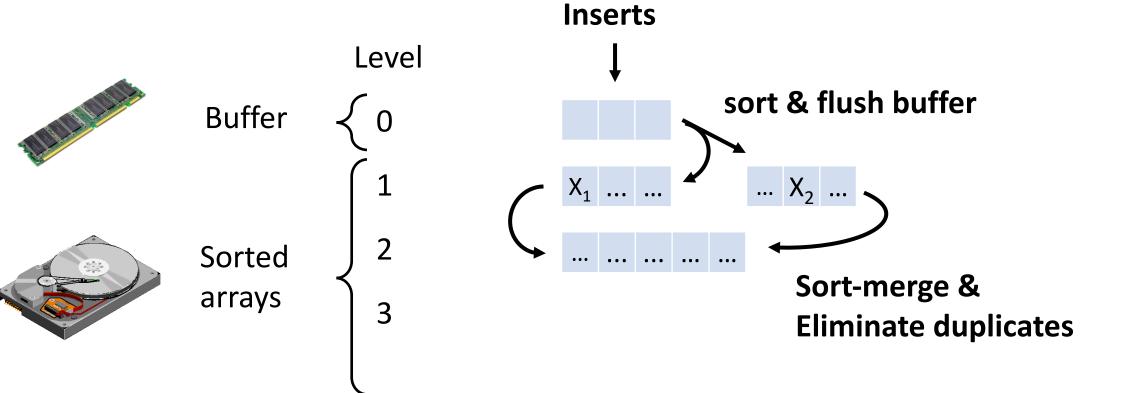
Design principle #1: optimize for insertions by buffering

Design principle #2: optimize for lookups by sort-merging arrays



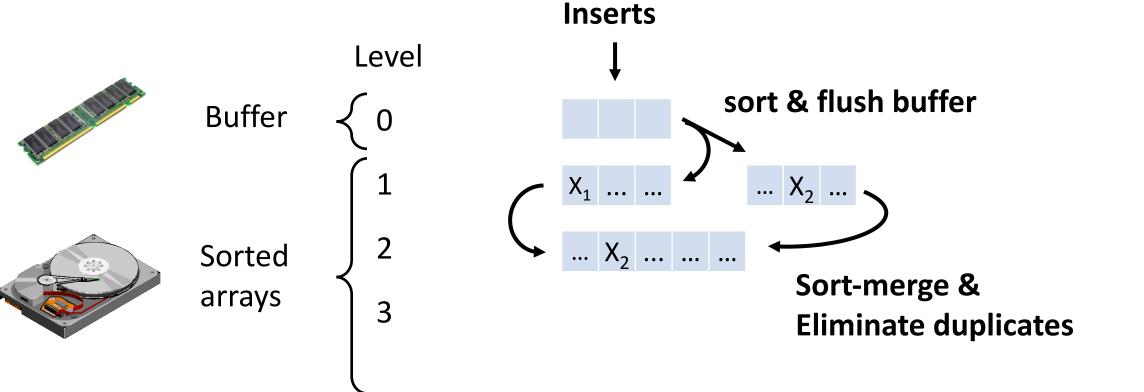
Design principle #1: optimize for insertions by buffering

Design principle #2: optimize for lookups by sort-merging arrays



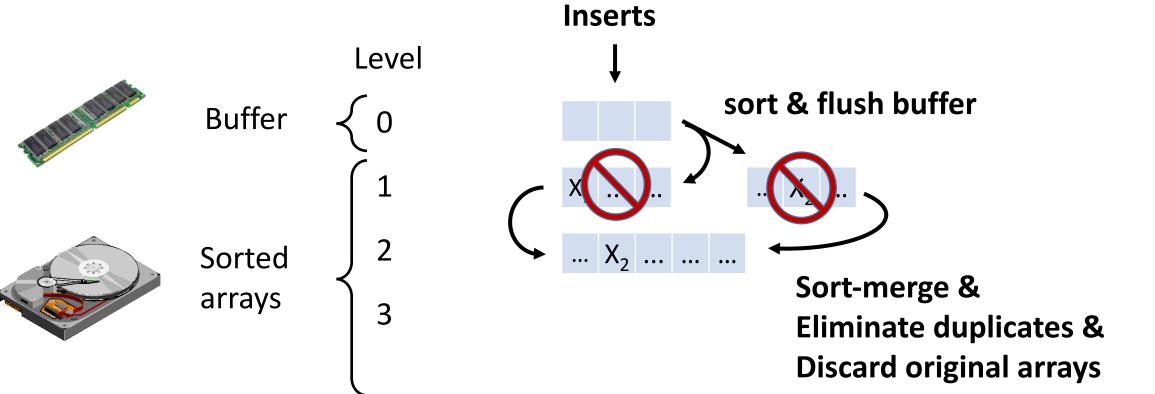
Design principle #1: optimize for insertions by buffering

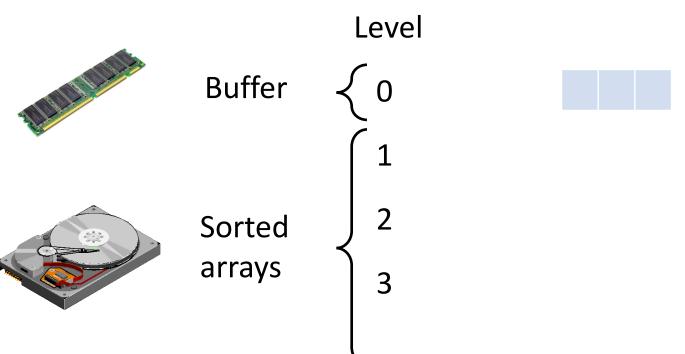
Design principle #2: optimize for lookups by sort-merging arrays

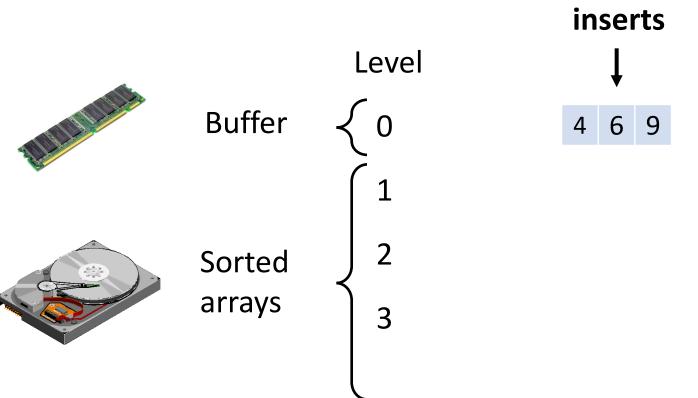


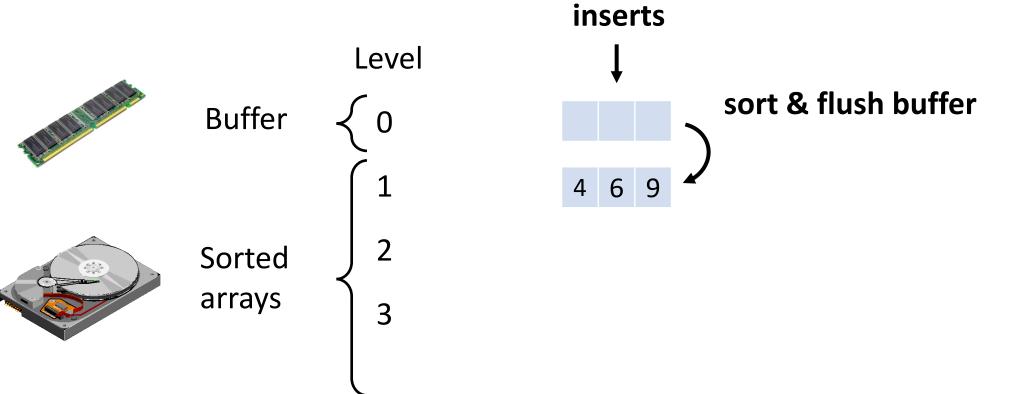
Design principle #1: optimize for insertions by buffering

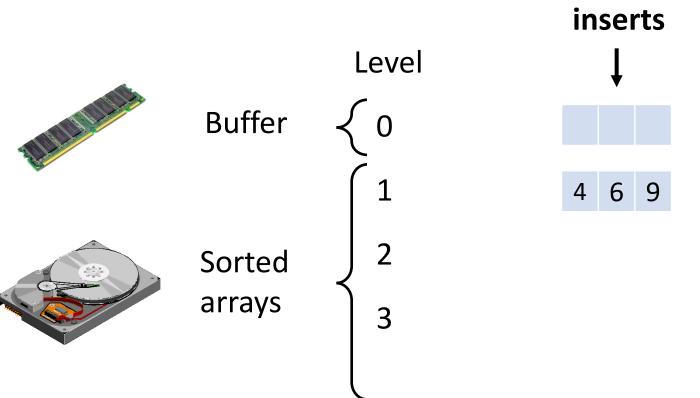
Design principle #2: optimize for lookups by sort-merging arrays

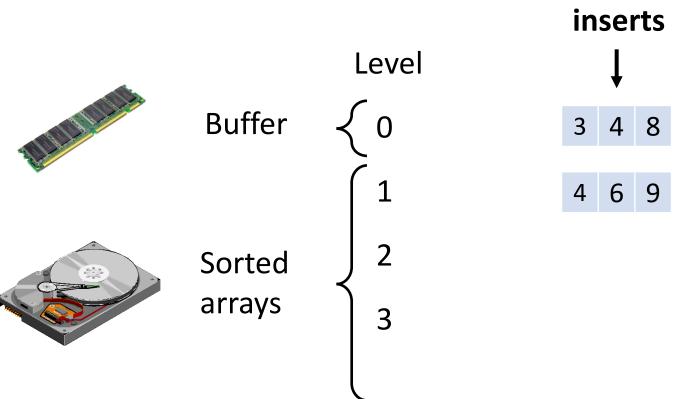


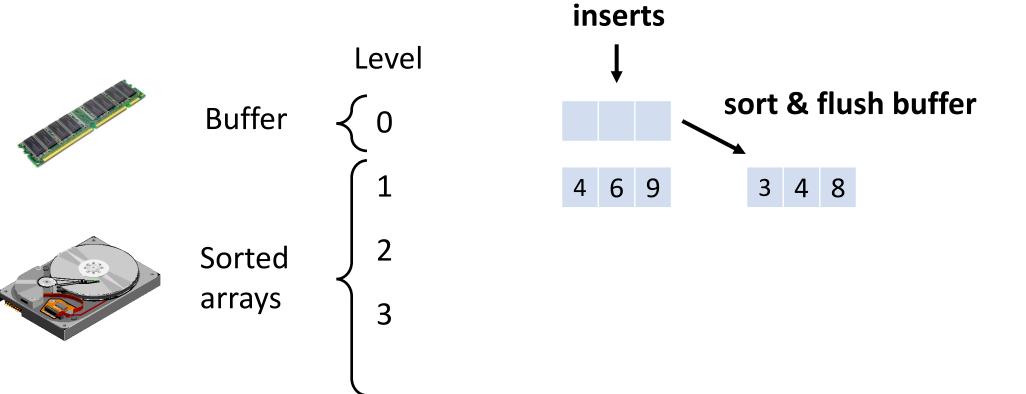


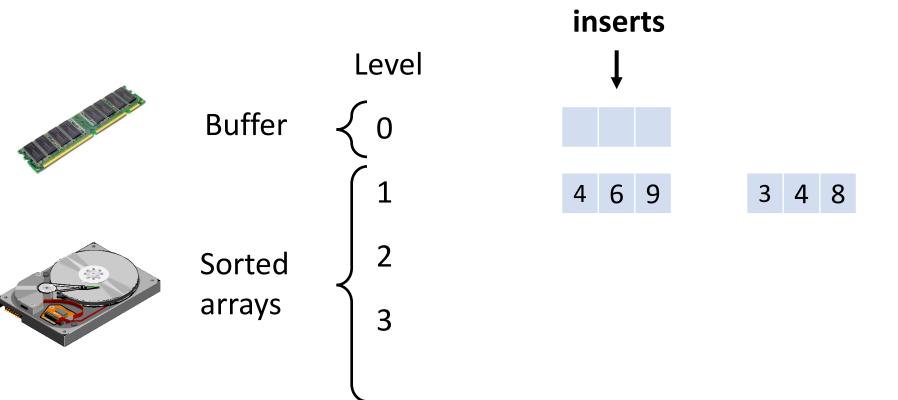


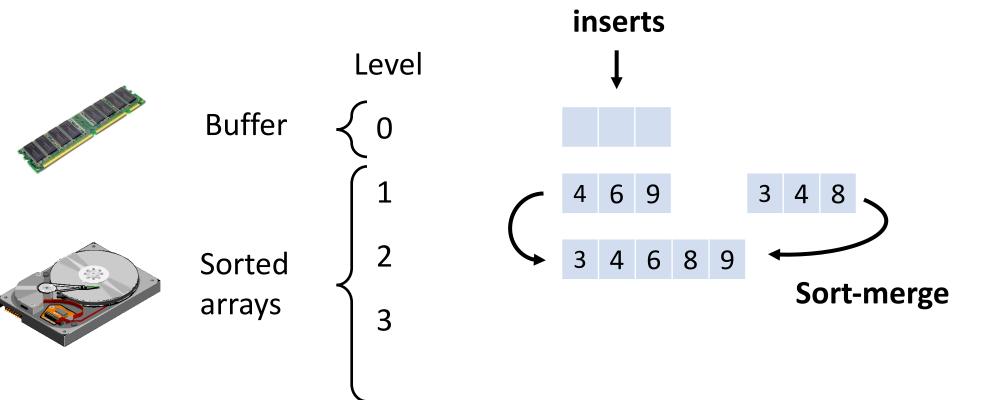


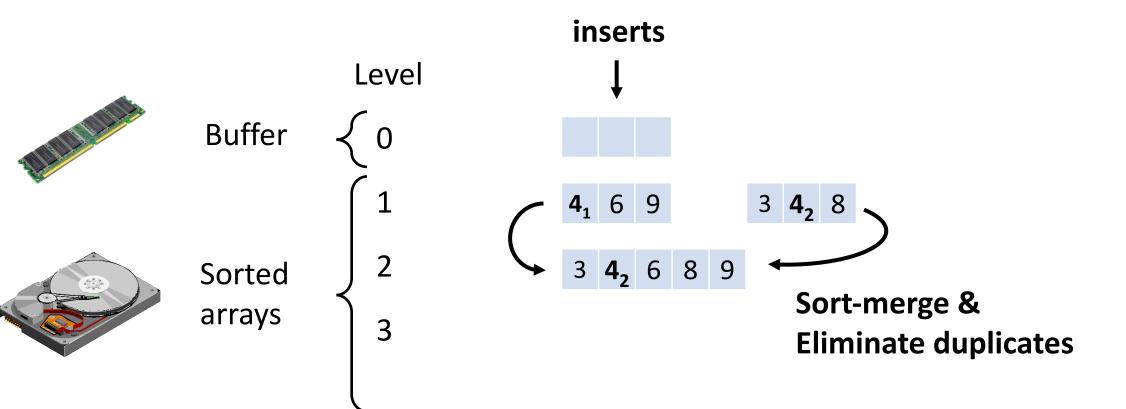


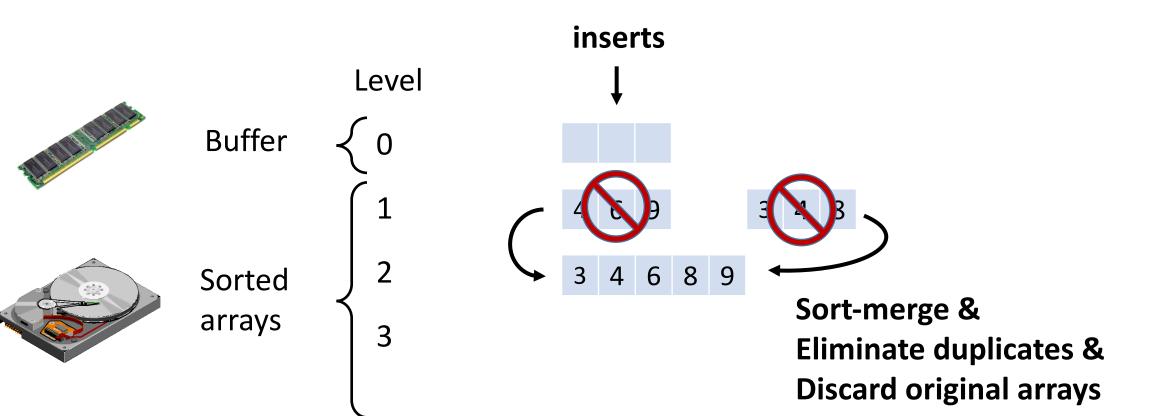






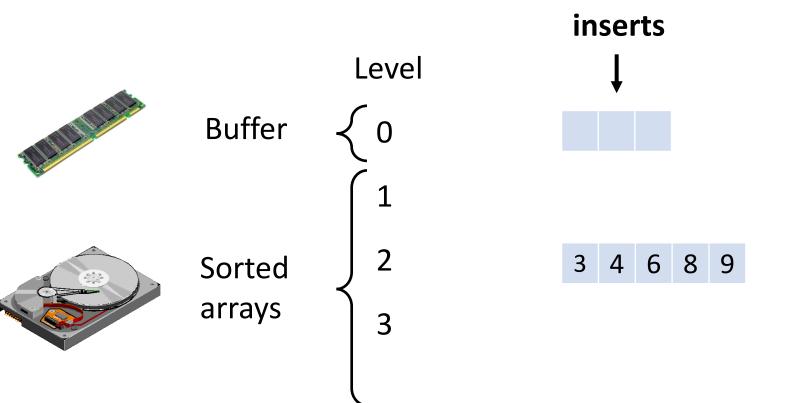


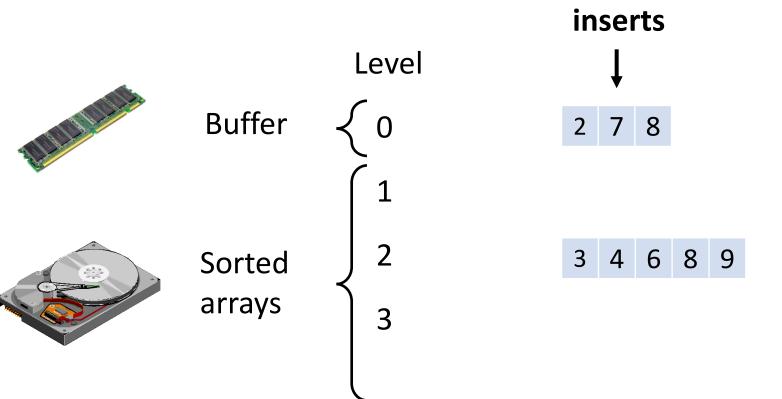


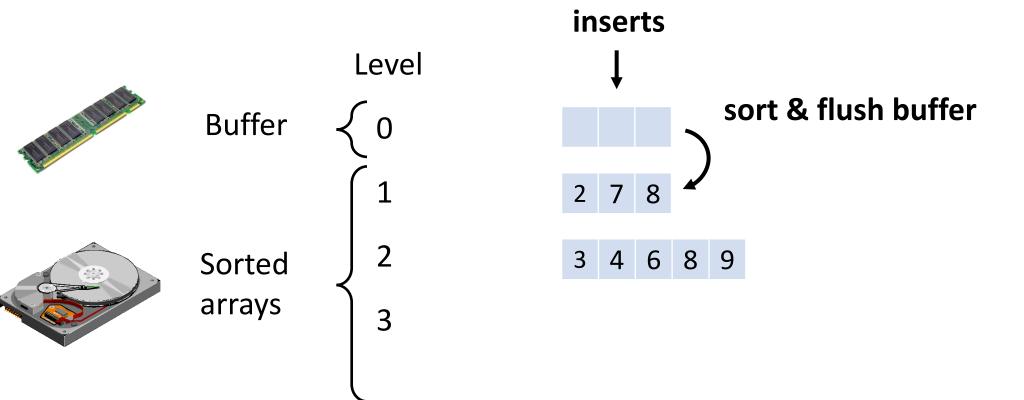


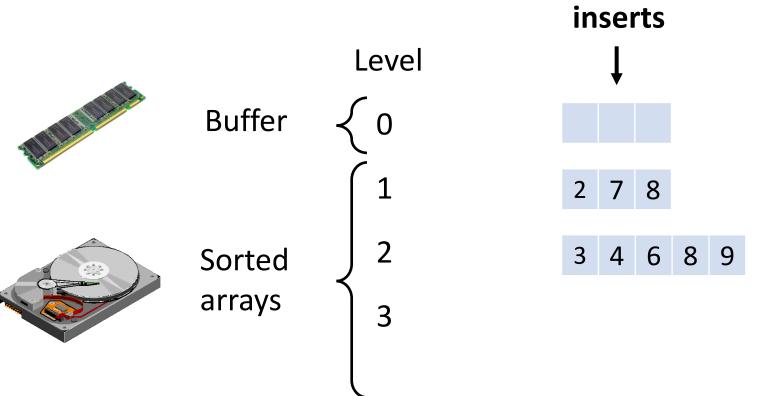




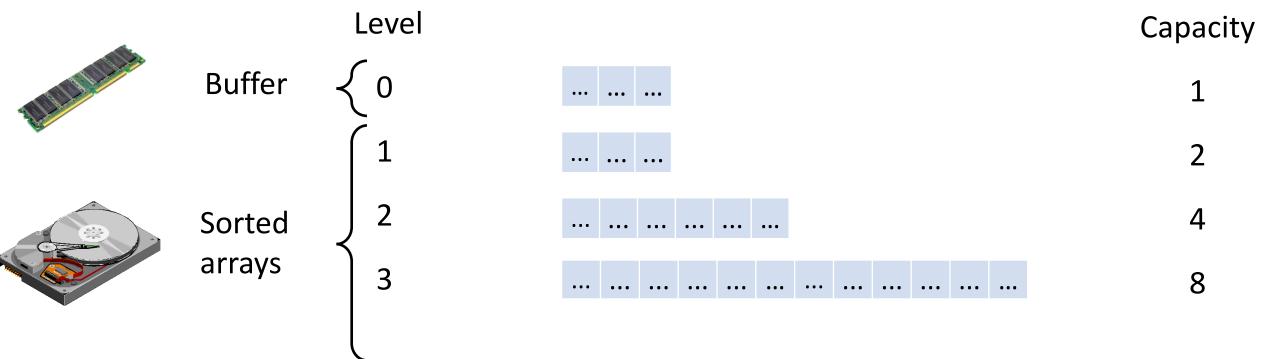








Levels have exponentially increasing capacities.



Basic LSM-tree – Lookup cost

Lookup method?

How?

Lookup cost?

Search youngest to oldest.

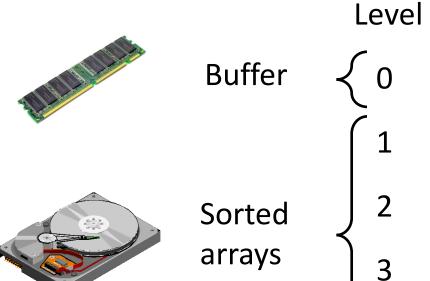
Binary search.

$$O\left(\log_2\left(\frac{N}{B}\right)\right)$$

$$O\left(\log_2\left(\frac{N}{B}\right)\right)$$

$$O\left(\log_2\left(\frac{N}{B}\right)^2\right)$$

Capacity





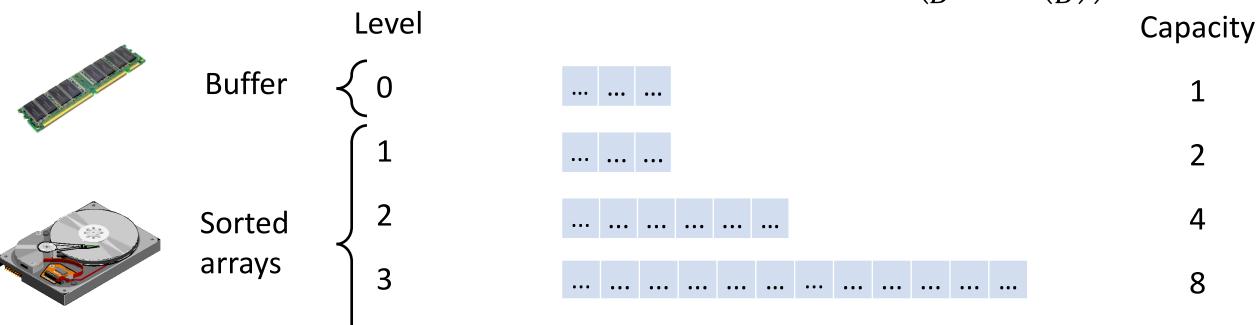
Basic LSM-tree – Insertion cost

How many times is each entry copied?

What is the price of each copy?

Total insert cost?

$O\left(\log_2\left(\right)\right)$	$\left(\frac{N}{B}\right)$
$O\left(\frac{1}{B}\right)$	
$O\left(\frac{1}{R} \cdot \log R\right)$	$g_2\left(\frac{N}{R}\right)$



Results Catalogue

	Lookup cost	Insertion cost
Sorted array	$O(\log_2(N/B))$	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	$O(\log_B(N/B))$	$O(\log_B(N/B))$
Basic LSM-tree	$O(\log_2(N/B)^2)$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree		
Tiered LSM-tree		

Results Catalogue

Better insert cost and worst lookup cost compared with B-trees

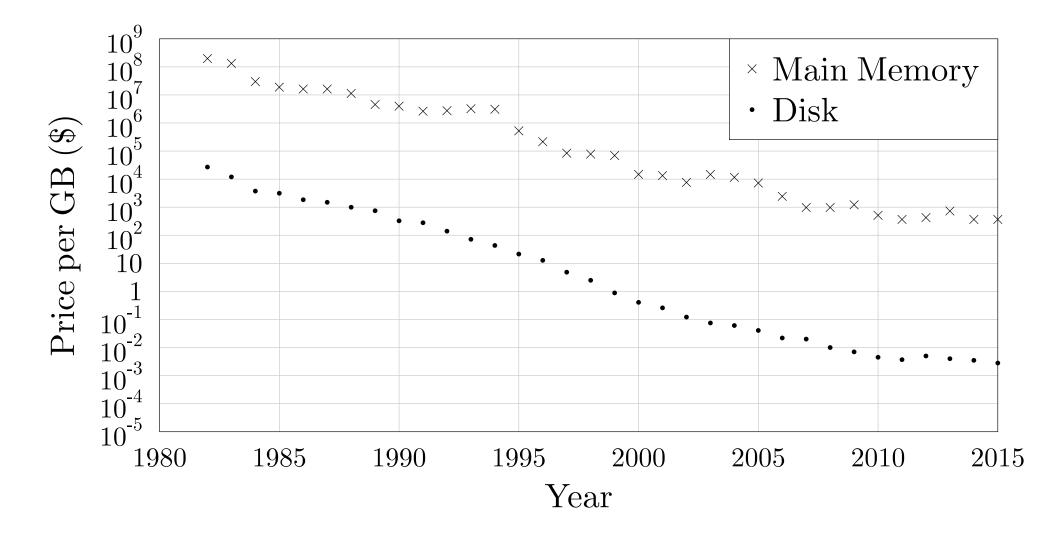
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Basic LSM-tree	$O(\log_2(N/B)^2)$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree		
Tiered LSM-tree		

Results Catalogue

Better insert cost and worst lookup cost compared with B-trees Can we improve lookup cost?

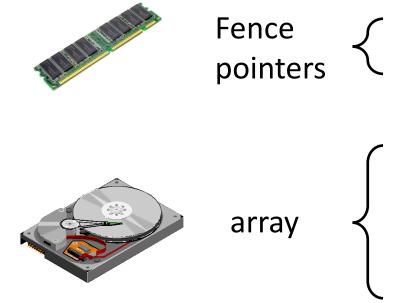
	Lookup cost	Insertion cost
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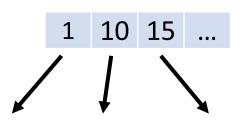
Declining Main Memory Cost



Declining Main Memory Cost

Store a fence pointer for every block in main memory





Block 1	Block 2	Block 3	•••
1	10	15	
3	11	16	
6	13	18	•••

Lookup cost	Insertion cost
$O(\log_2(N/B))$	O(N/B)
O(N/B)	O(1/B)
$O(log_B(N/B))$	$O(log_B(N/B))$
$O(\log_2(N/B)^2)$	$O(1/B \cdot \log_2(N/B))$
	$O(\log_2(N/B))$ $O(N/B)$ $O(\log_B(N/B))$

	Lookup cost	Insertion cost
Sorted array	$O(log_2(N/B))$	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	$O(log_B(N/B))$	$O(\log_B(N/B))$
Basic LSM-tree	$O(\log_2(N/B)^2)$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree		
Tiered LSM-tree		

	Lookup cost	Insertion cost
Sorted array	O(1)	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	$O(log_B(N/B))$	$O(log_B(N/B))$
Basic LSM-tree	$O(\log_2(N/B)^2)$	$O(1/B \cdot log_2(N/B))$
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	Lookup cost	Insertion cost
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Leveled LSM-tree		
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Lookup cost	Insertion cost
O(1)	O(N/B)
O(N/B)	O(1/B)
O(1)	O(1)
$O(\log_2(N/B)^2)$	$O(1/B \cdot \log_2(N/B))$
	O(1) O(N/B) O(1)

	Lookup cost	Insertion cost
Sorted array	O(1)	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	O(1)	O(1)
Basic LSM-tree	$O(\log_2(N/B))$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree		
Tiered LSM-tree		

Quick sanity check:

suppose $N = 2^{42}$

and $B = 2^{10}$

	Lookup cost	Insertion cost
Sorted array	O(1)	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	O(1)	O(1)
Basic LSM-tree	$O(\log_2(N/B))$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree		
Tiered LSM-tree		

Quick sanity check:

suppose $N = 2^{42}$

and

 $B = 2^{10}$

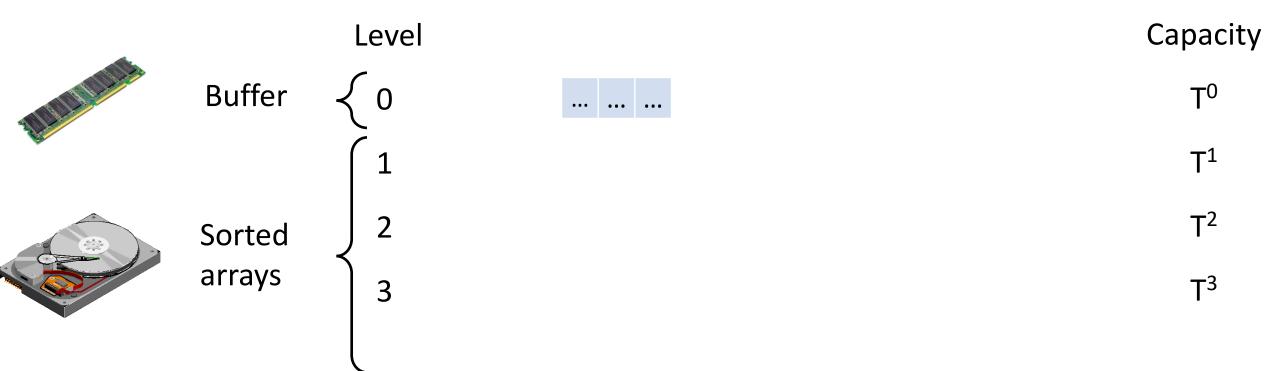
	Lookup cost	Insertion cost
Sorted array	O(1)	O(2 ³²)
Log	O(2 ³²)	O(2 ⁻¹⁰)
B-tree	O(1)	O(1)
Basic LSM-tree	O(5)	O(2 ⁻¹⁰ · 5)
Leveled LSM-tree		
Tiered LSM-tree		

Leveled LSM-tree



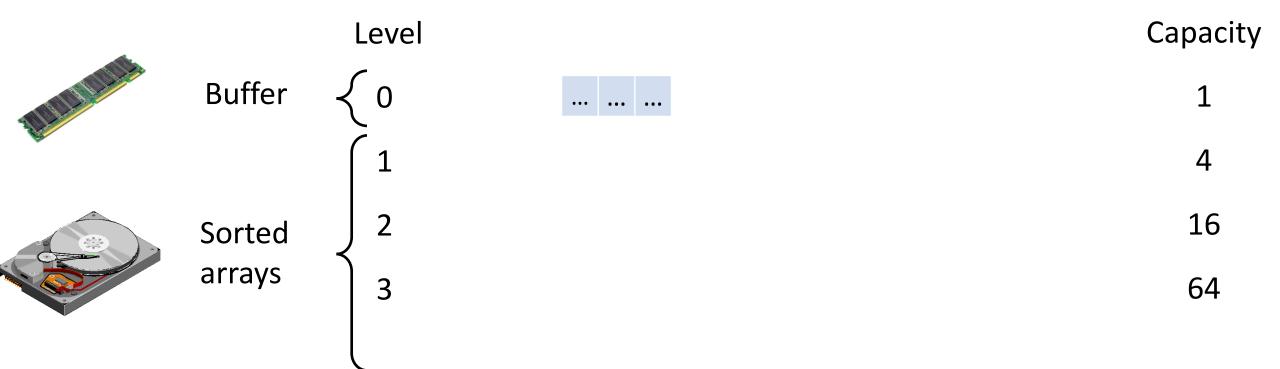


Lookup cost depends on number of levels How to reduce it?



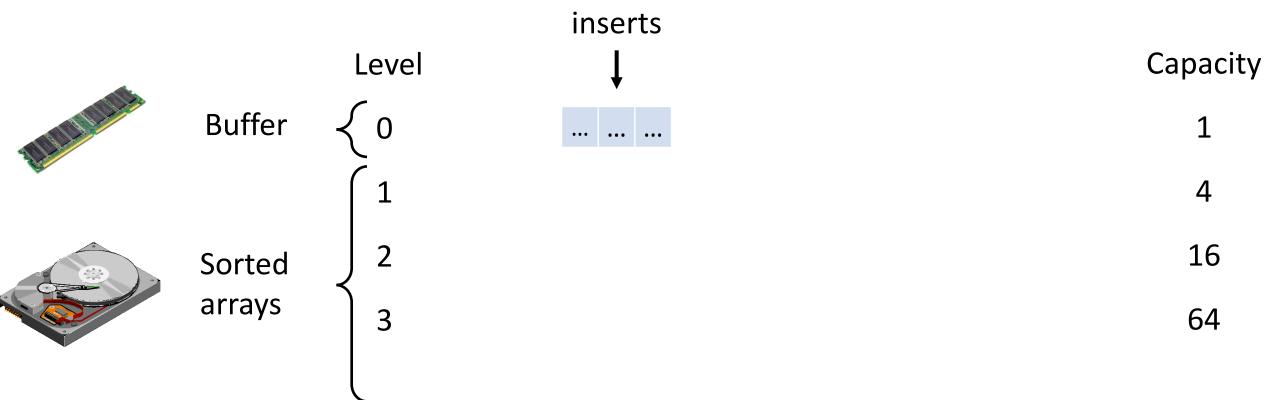
Lookup cost depends on number of levels How to reduce it?

E.g. size ratio of 4



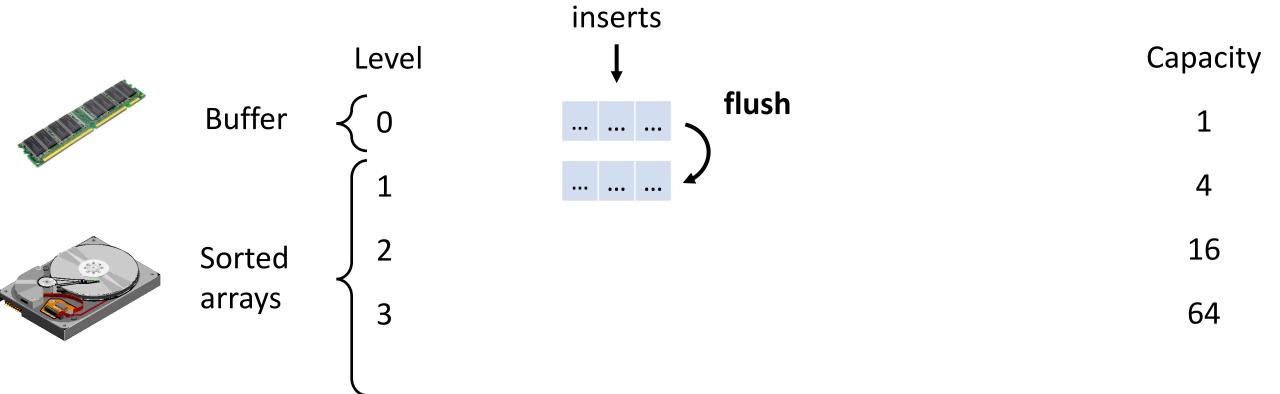
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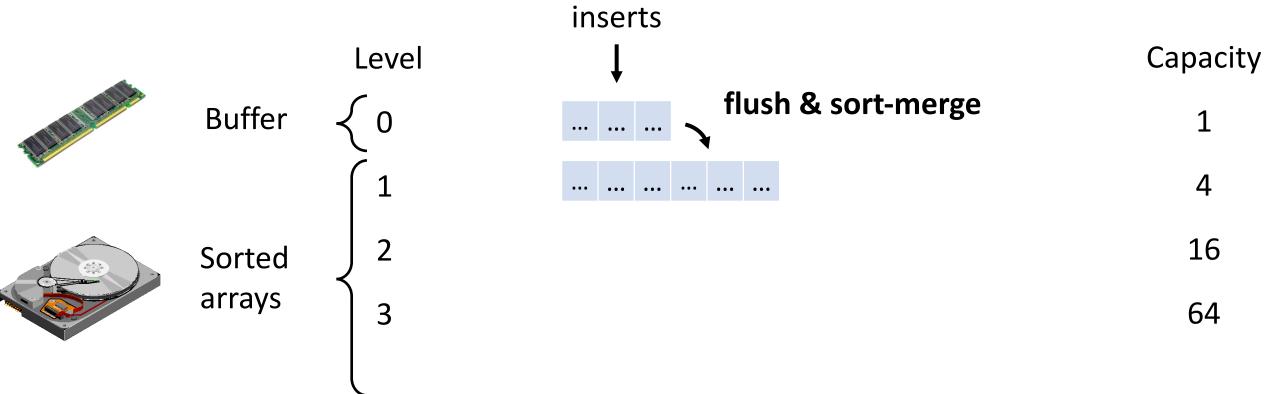
Lookup cost depends on number of levels How to reduce it?

E.g. size ratio of 4



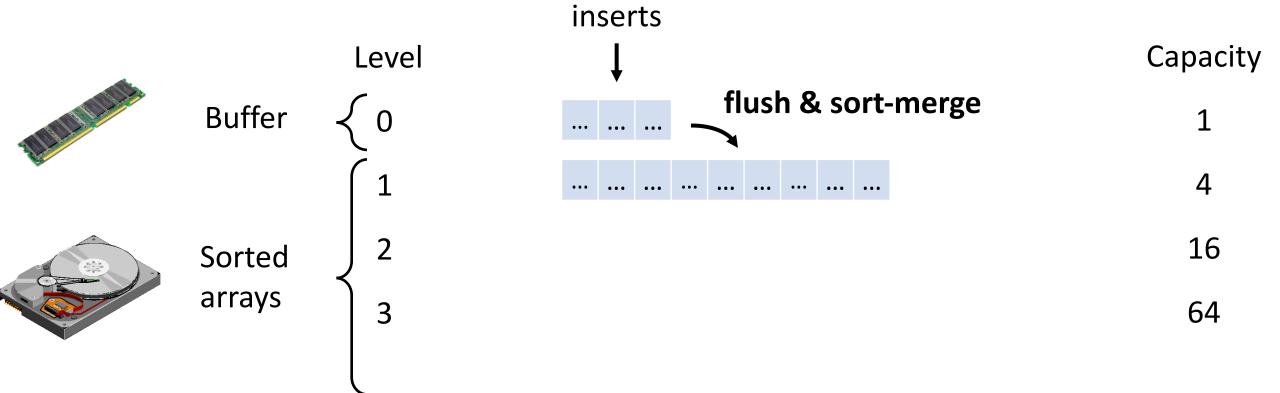
Lookup cost depends on number of levels How to reduce it?

E.g. size ratio of 4



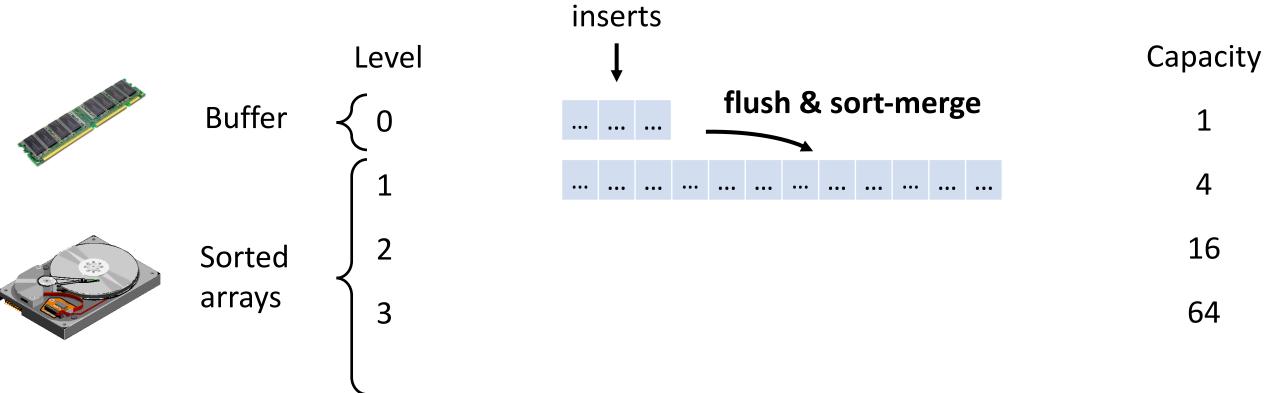
Lookup cost depends on number of levels How to reduce it?

E.g. size ratio of 4



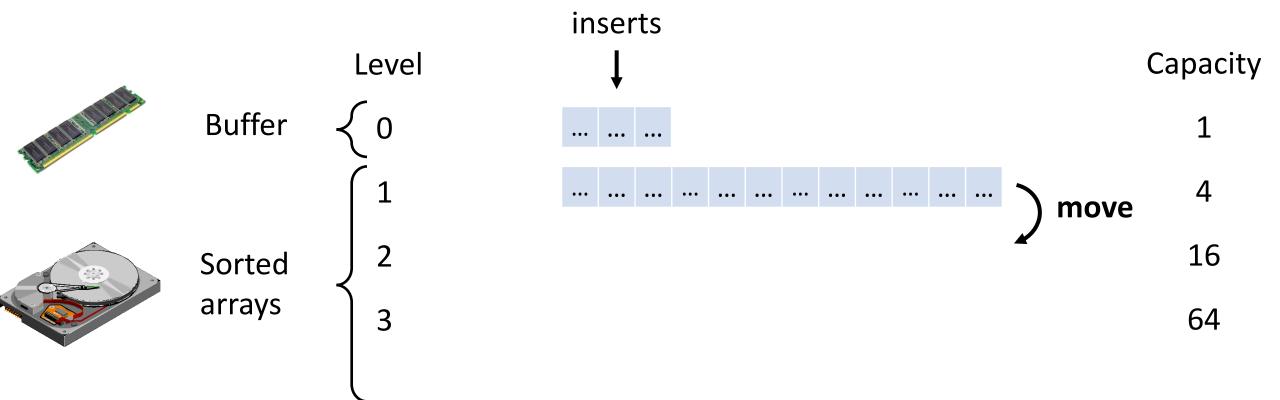
Lookup cost depends on number of levels How to reduce it?

E.g. size ratio of 4



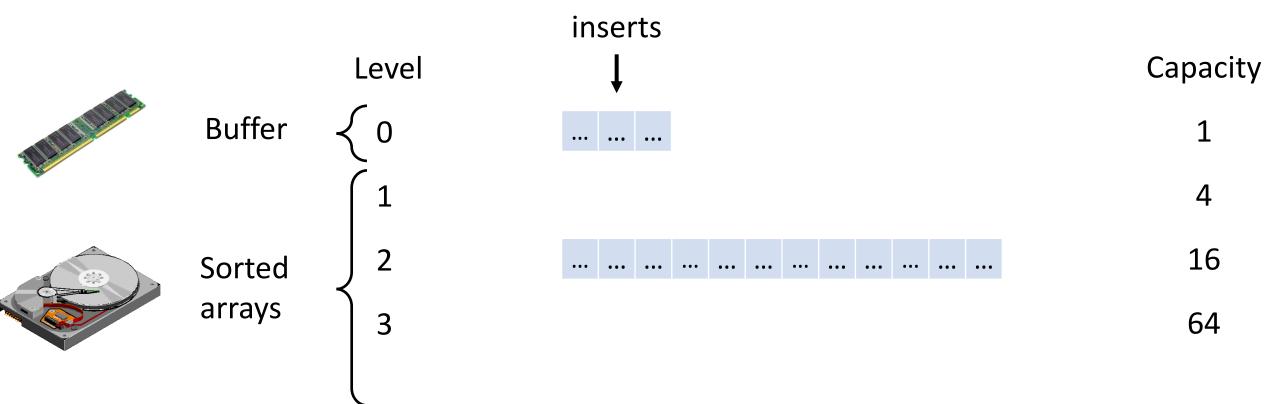
Lookup cost depends on number of levels How to reduce it?

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Lookup cost depends on number of levels How to reduce it?

E.g. size ratio of 4

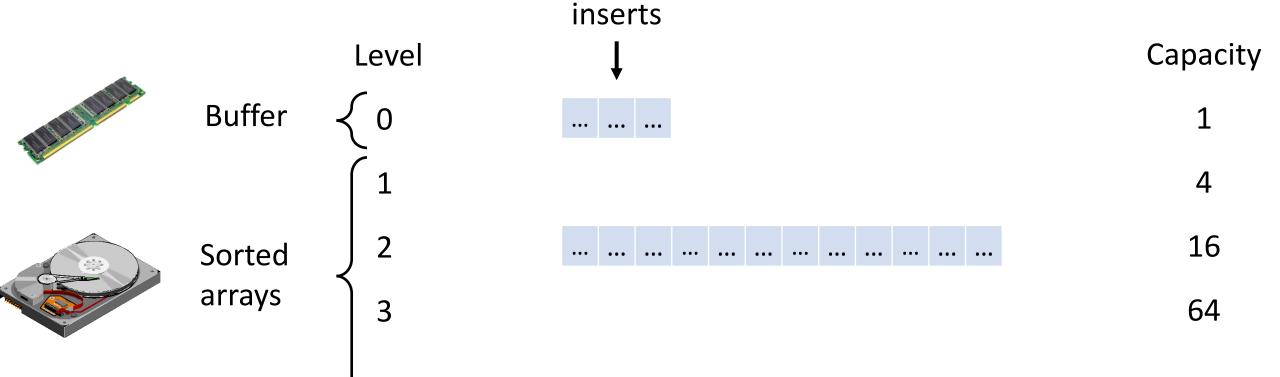


Lookup cost?

$$O\left(\log_T\left(\frac{N}{B}\right)\right)$$

Insertion cost?

$$O\left(\frac{T}{B} \cdot \log_T\left(\frac{N}{B}\right)\right)$$





Lookup cost?
$$O\left(\log_T\left(\frac{N}{B}\right)\right)$$

Insertion cost?

O
$$\left(\frac{T}{B} \cdot \log_T\left(\frac{N}{B}\right)\right)$$



What happens as we increase the size ratio T?

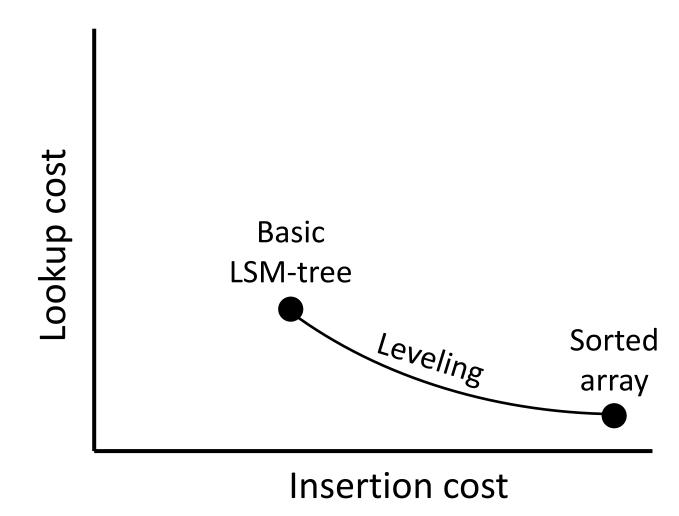
What happens when size ratio T is set to be N/B?

Lookup cost becomes:

Insert cost becomes:

$$O(N/B^2)$$

The LSM-tree becomes a sorted array!



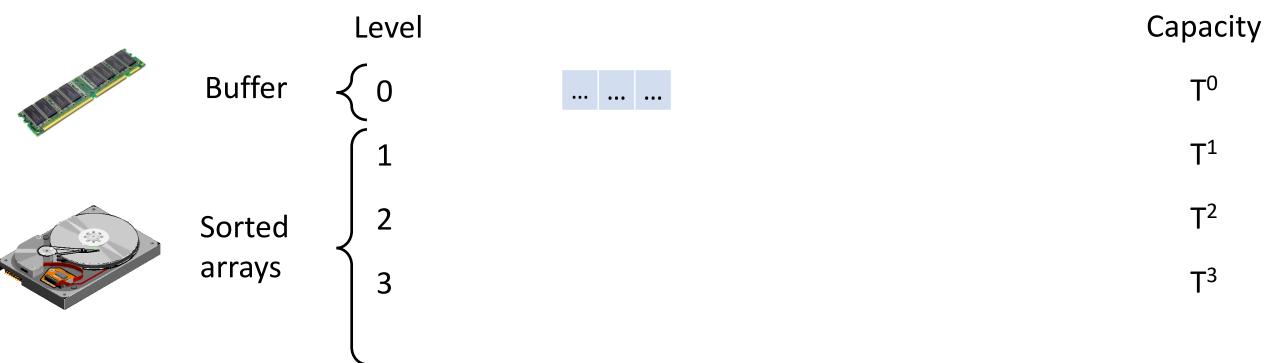
Results Catalogue – with fence pointers

	Lookup cost	Insertion cost
Sorted array	O(1)	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	O(1)	O(1)
Basic LSM-tree	$O(\log_2(N/B))$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree	$O(log_T(N/B))$	$O(T/B \cdot log_T(N/B))$
Tiered LSM-tree		





Reduce the number of levels by increasing the size ratio. Do not merge within a level.



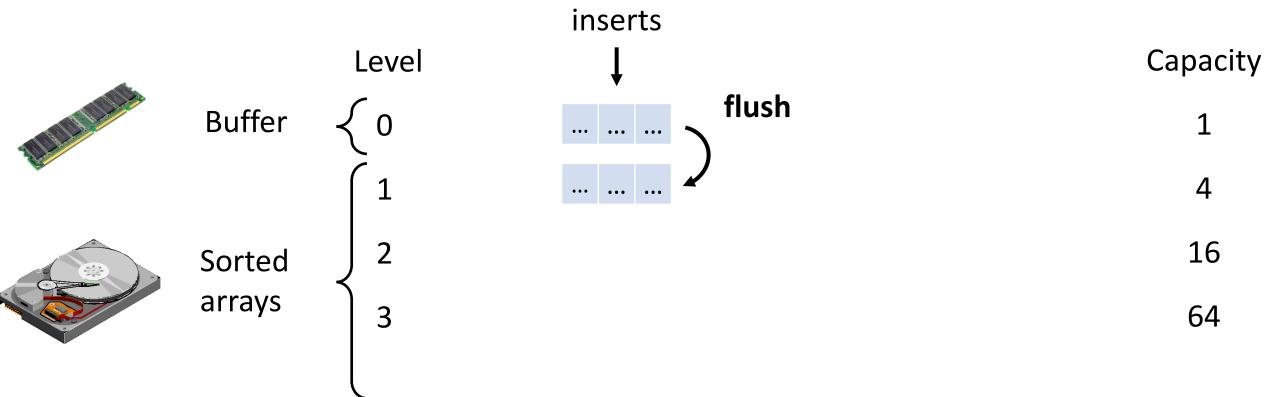
Reduce the number of levels by increasing the size ratio.

Do not merge within a level.



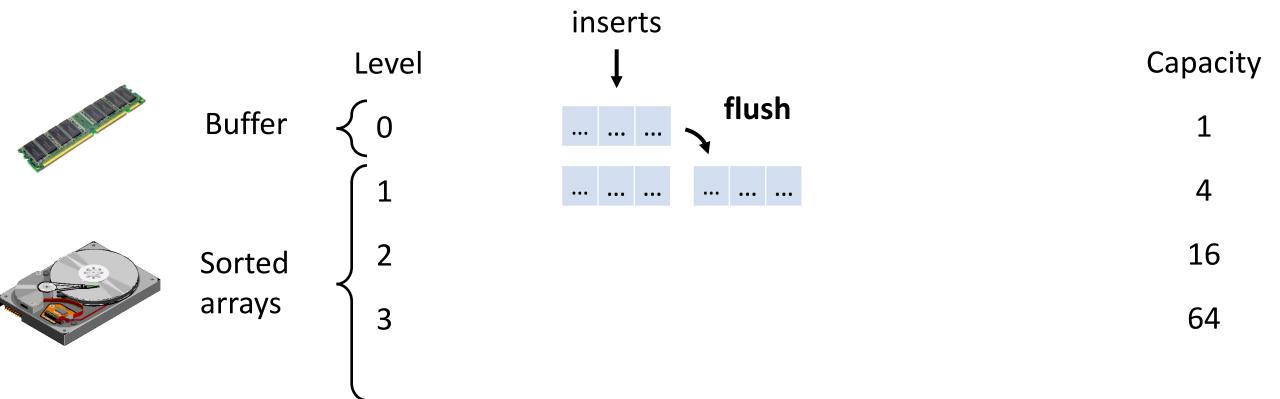
Reduce the number of levels by increasing the size ratio.

Do not merge within a level.



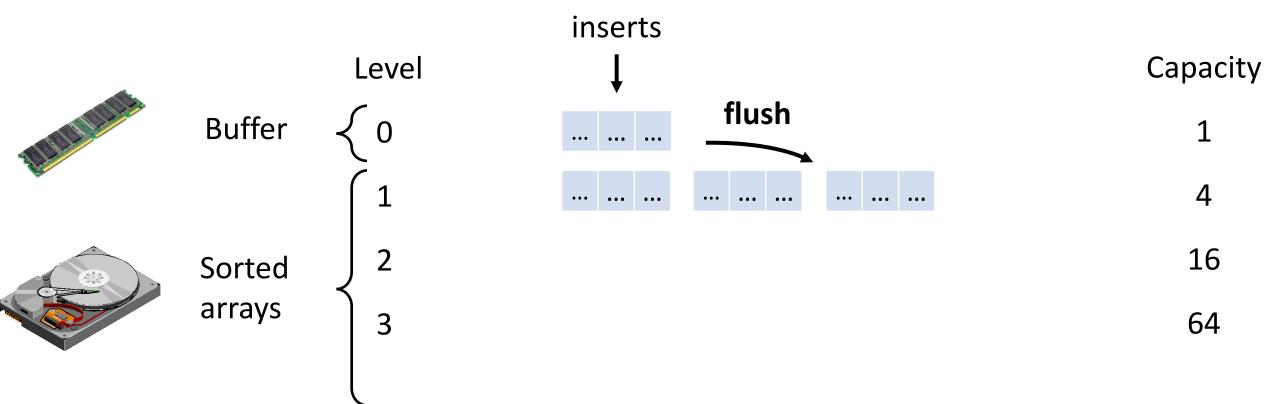
Reduce the number of levels by increasing the size ratio.

Do not merge within a level.



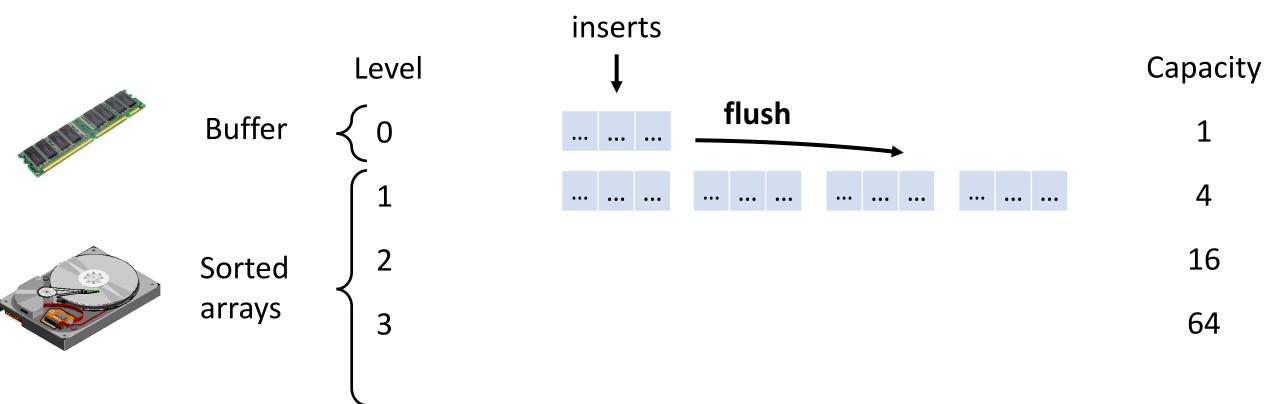
Reduce the number of levels by increasing the size ratio.

Do not merge within a level.



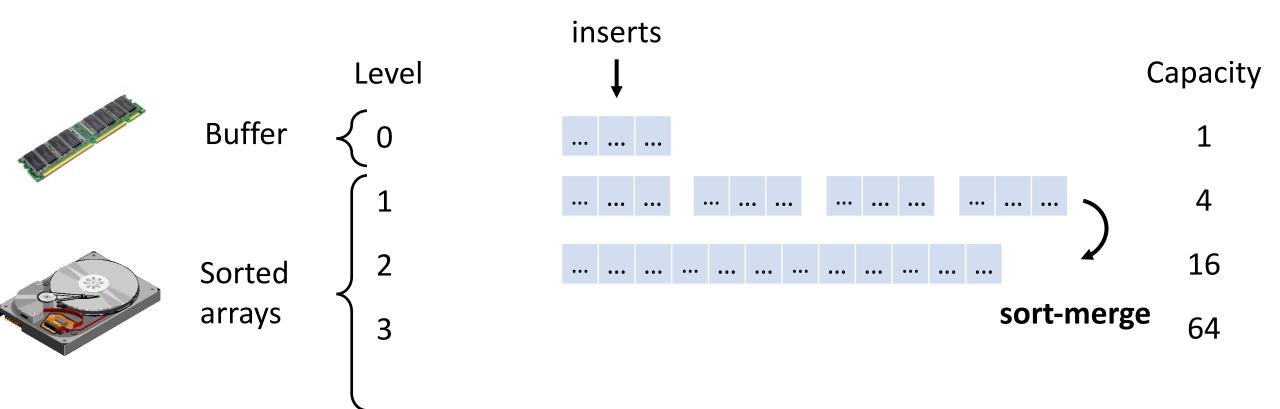
Reduce the number of levels by increasing the size ratio.

Do not merge within a level.



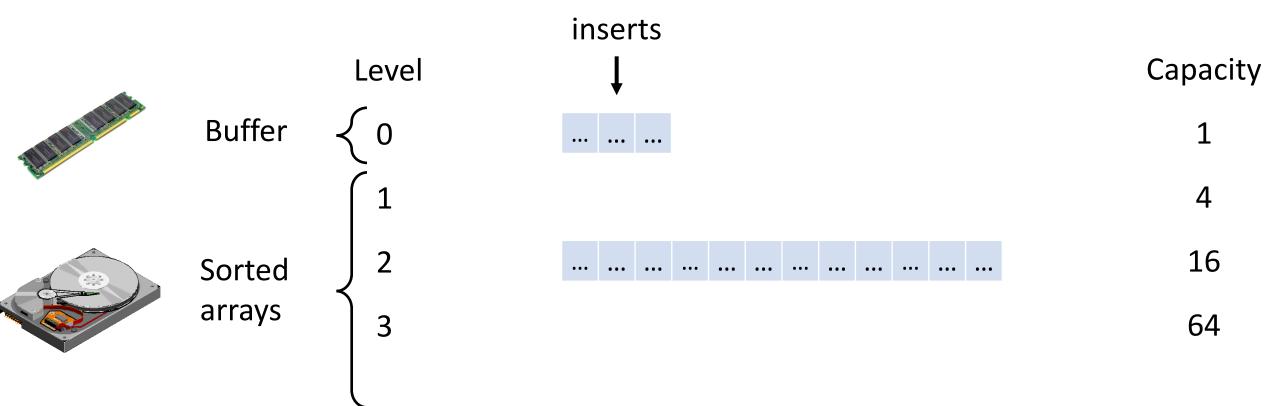
Reduce the number of levels by increasing the size ratio.

Do not merge within a level.



Reduce the number of levels by increasing the size ratio.

Do not merge within a level.

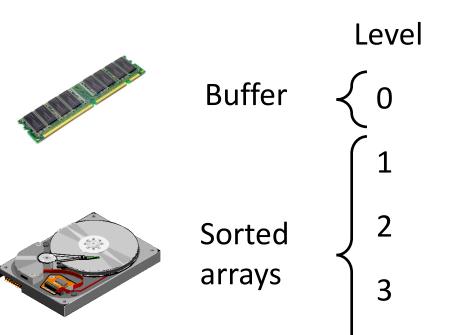


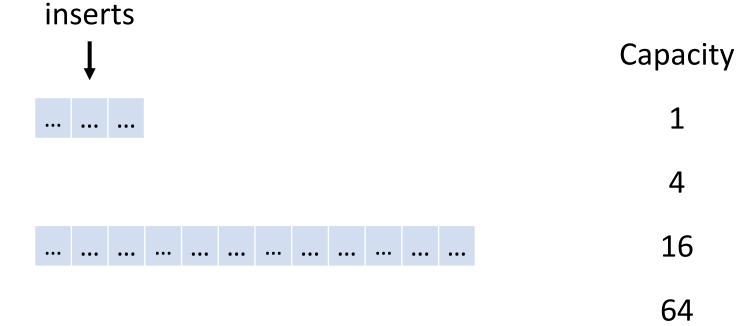
Lookup cost?

$$O\left(T \cdot \log_T\left(\frac{N}{B}\right)\right)$$

Insertion cost?

$$O\left(\frac{1}{B} \cdot \log_T\left(\frac{N}{B}\right)\right)$$





Lookup cost?
$$0\left(T \cdot \log_T\left(\frac{N}{B}\right)\right)$$

Insertion cost?

$$O\left(\frac{1}{B} \cdot \log_T\left(\frac{N}{B}\right)\right)$$



What happens as we increase the size ratio T?

What happens when size ratio T is set to be N/B?

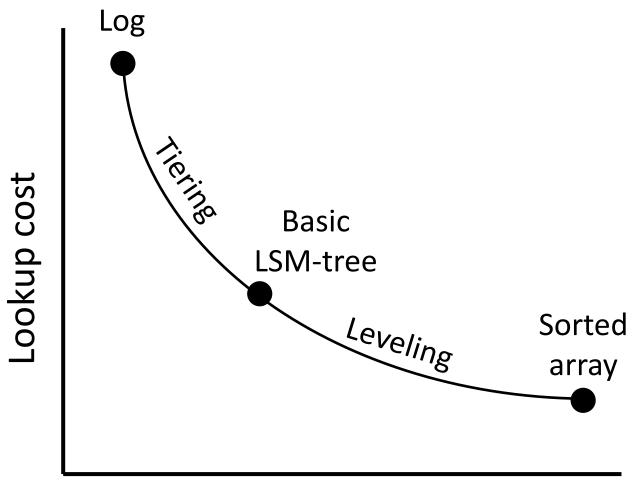
Lookup cost becomes:

O(N/B)

Insert cost becomes:

O(1/B)

The tiered LSM-tree becomes a log!

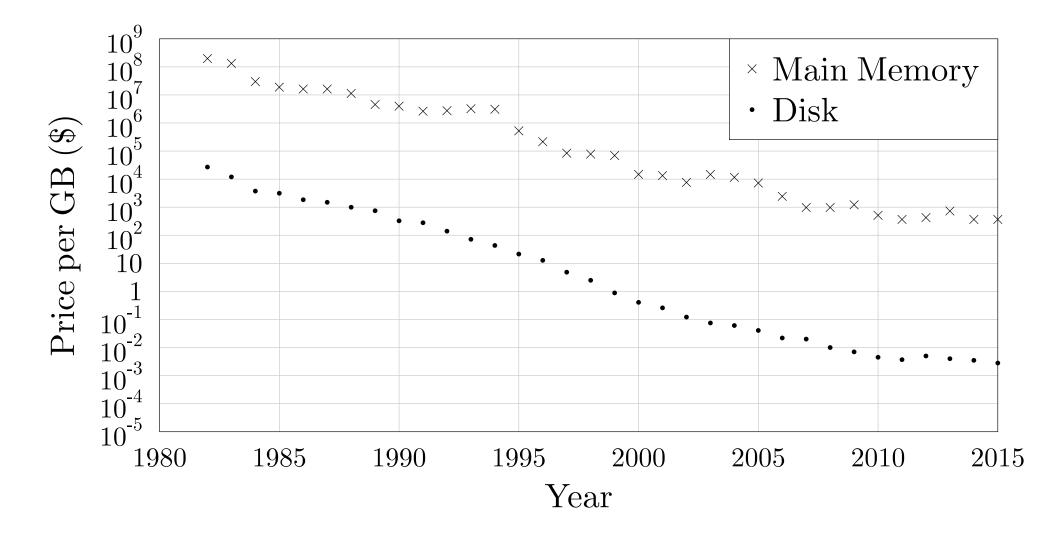


Insertion cost

Results Catalogue – with fence pointers

	Lookup cost	Insertion cost
Sorted array	O(1)	O(N/B)
Log	O(N/B)	O(1/B)
B-tree	O(1)	O(1)
Basic LSM-tree	$O(\log_2(N/B))$	$O(1/B \cdot \log_2(N/B))$
Leveled LSM-tree	$O(log_T(N/B))$	$O(T/B \cdot log_T(N/B))$
Tiered LSM-tree	$O(T \cdot log_T(N/B))$	$O(1/B \cdot log_T(N/B))$

Declining Main Memory Cost

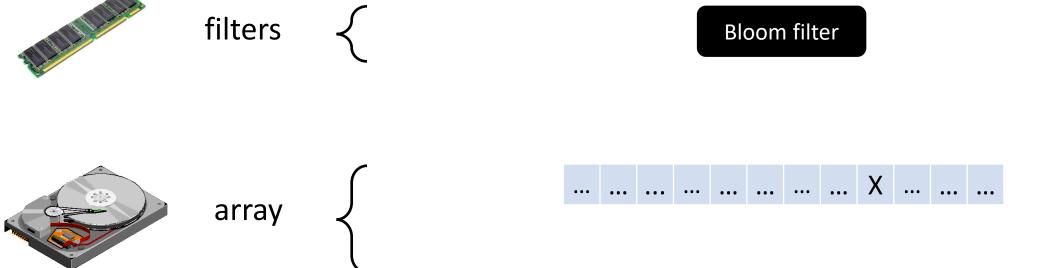


Answers set-membership queries

Smaller than array, and stored in main memory

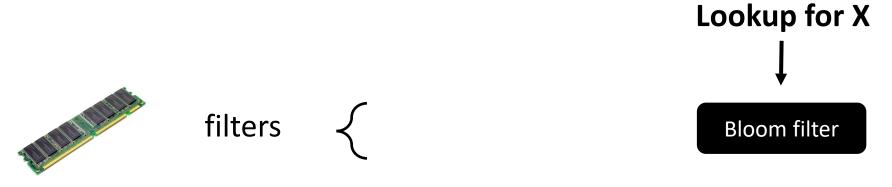
Purpose: avoid accessing disk if entry is not in array

Subtlety: may return false positives.



Answers set-membership queries
Smaller than array, and stored in main memory
Purpose: avoid accessing disk if entry is not in array

Subtlety: may return false positives.





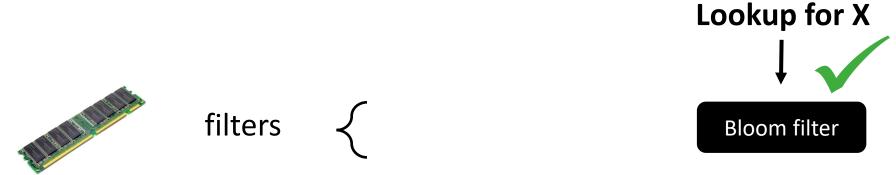


Answers set-membership queries

Smaller than array, and stored in main memory

Purpose: avoid accessing disk if entry is not in array

Subtlety: may return false positives.





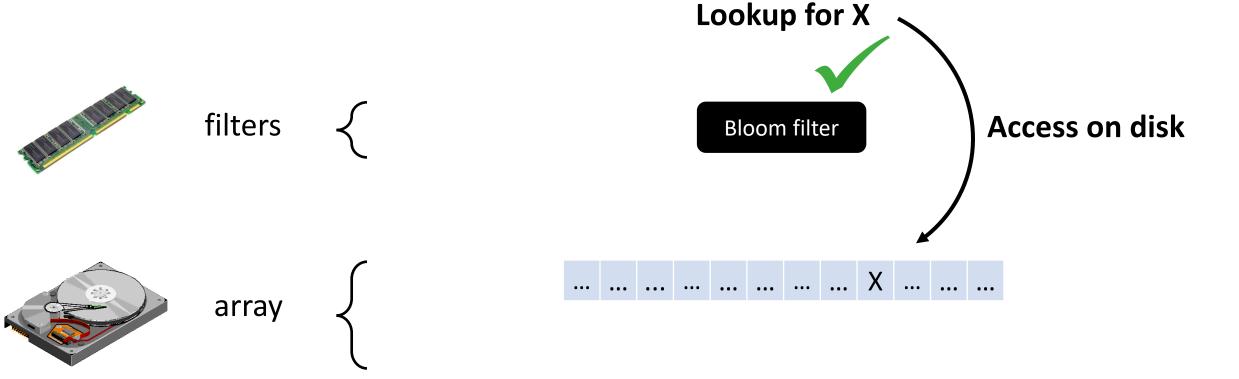


Answers set-membership queries

Smaller than array, and stored in main memory

Purpose: avoid accessing disk if entry is not in array

Subtlety: may return false positives.

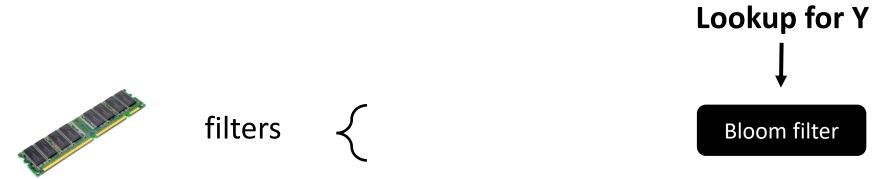


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Answers set-membership queries

Smaller than array, and stored in main memory

Purpose: avoid accessing disk if entry is not in array

Subtlety: may return false positives.

Lookup for Y



filters



Bloom filter







Answers set-membership queries

Smaller than array, and stored in main memory

Purpose: avoid accessing disk if entry is not in array

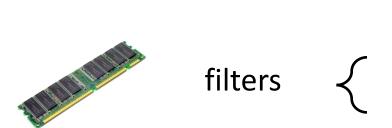
Subtlety: may return false positives.

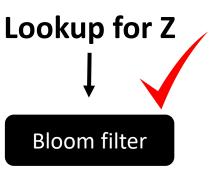






Answers set-membership queries
Smaller than array, and stored in main memory
Purpose: avoid accessing disk if entry is not in array
Subtlety: may return false positives.







array



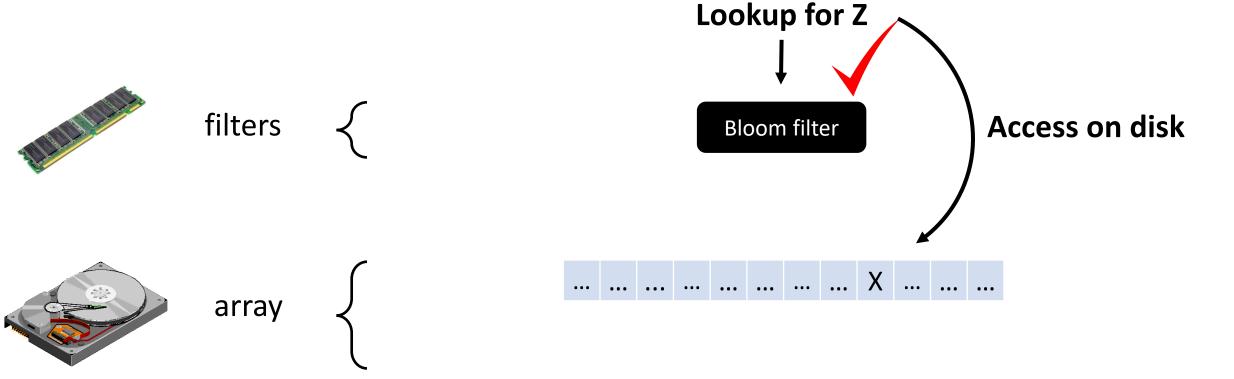


Answers set-membership queries

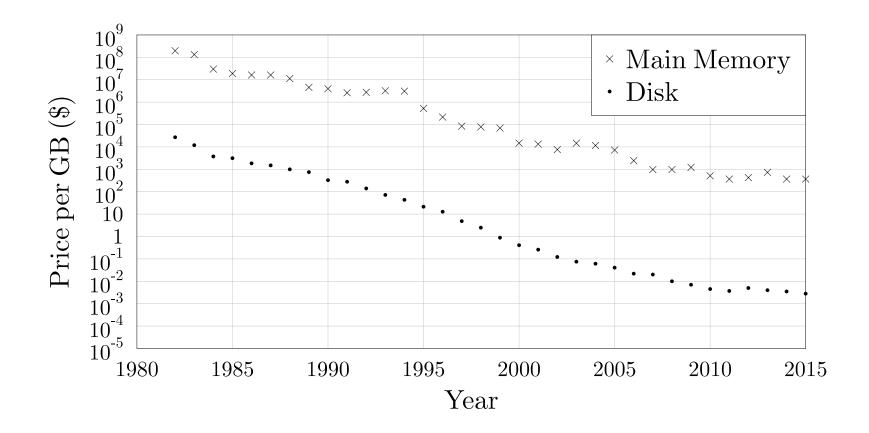
Smaller than array, and stored in main memory

Purpose: avoid accessing disk if entry is not in array

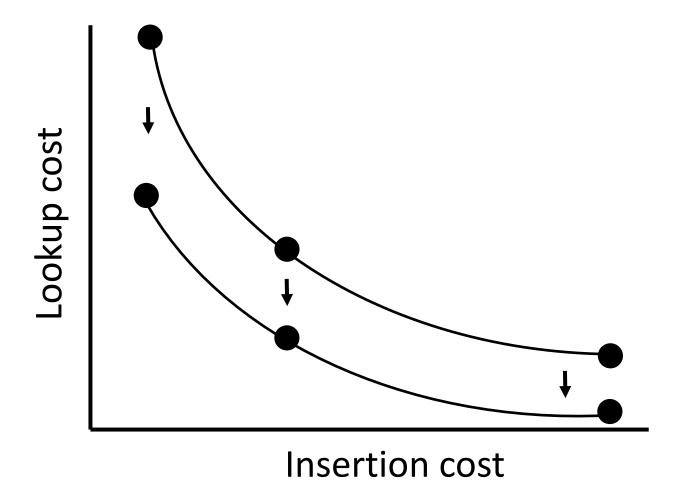
Subtlety: may return false positives.



The more main memory, the fewer false positives _____ cheaper lookups



The more main memory, the fewer false positives _____ cheaper lookups



Conclusions

Write-optimized

Highly tunable

Backbone of many modern systems

Trade-off between lookup and insert cost (tiering/leveling, size ratio)

Trade main memory for lookup cost (fence pointers, Bloom filters)

Thank you!

CS460: Intro to Database Systems

Database Systems and Beyond

Instructor: Manos Athanassoulis

https://bu-disc.github.io/CS460/

Database Systems

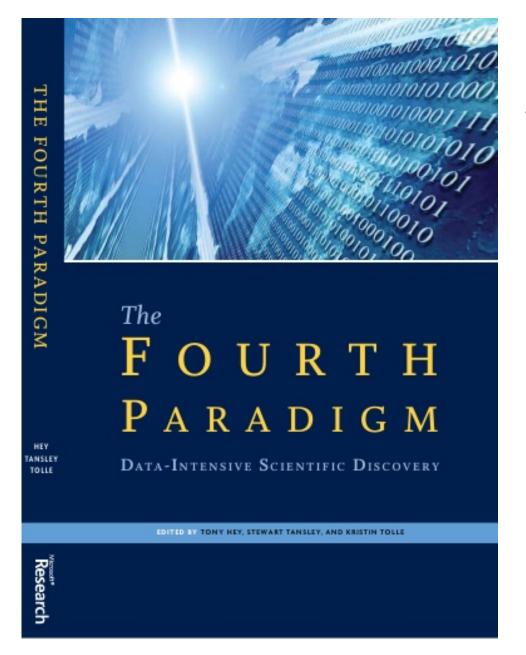
we spent a whole semester on Database Systems what is next?

what can we do with data?

data-driven science

data-driven discovery

data-driven governance

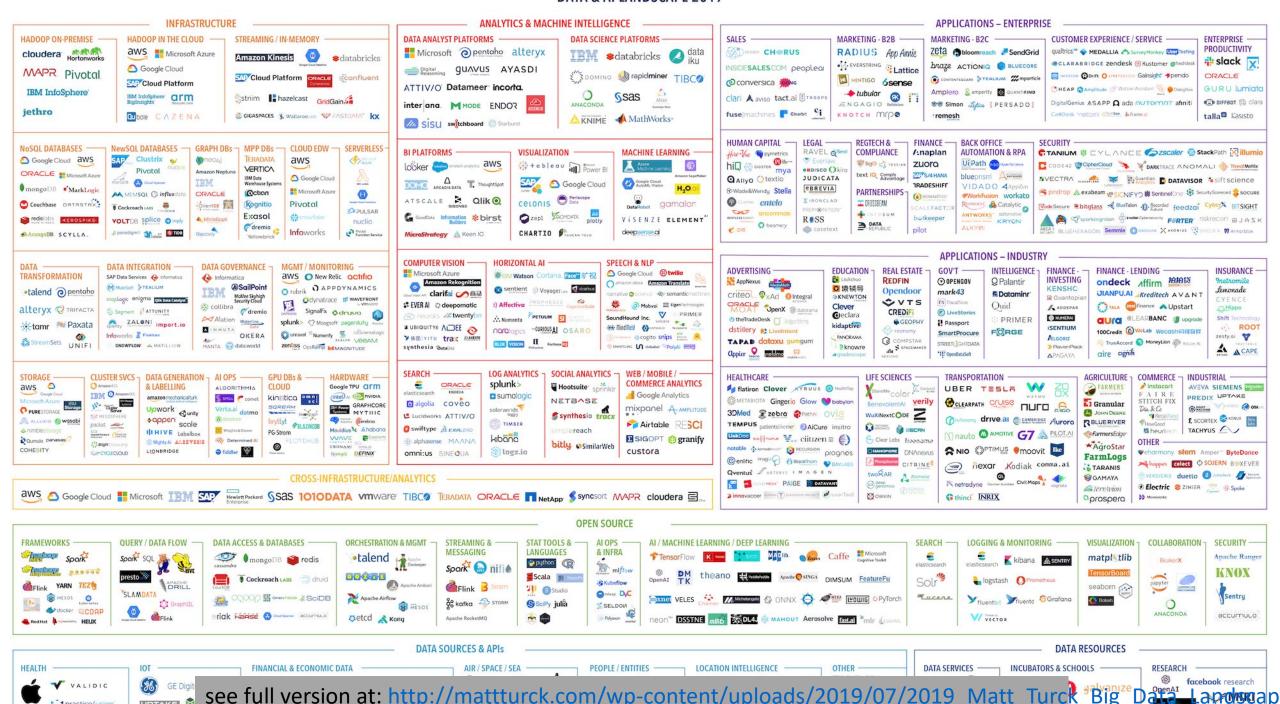


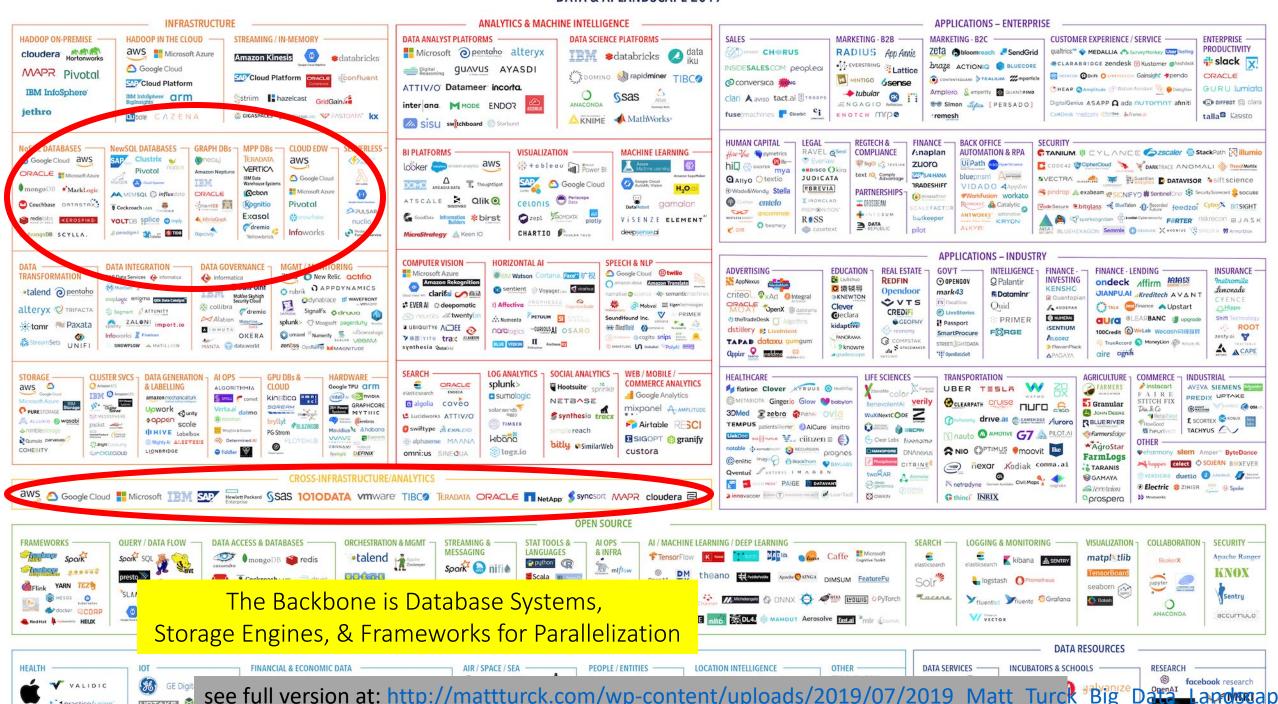
"Experimental, theoretical, and computational science are all being affected by the data deluge, and a fourth, 'data-intensive' science paradigm is emerging.

The goal is to have a world in which all of the science literature is online, all of the science data is online, and they interoperate with each other. Lots of new tools are needed to make this happen."

Faster Innovation through Data-Intensive Approaches

Need for Innovation in Data Management!





increase throughput by parallelization

"scale-up"
use more powerful machines (>#CPUs, >RAM)

"scale-out" use more machines

Scale Up Execution

how to use more cores (threads)?

inter-query parallelism each query runs on one processor

inter-operator parallelism
each query runs on multiple processors
an operator runs on one processor

intra-operator parallelism

An operator runs on multiple processors

Scale Up Storage

needs more disks!

how to distribute data?

block partition hash partition range partition

how to distribute data accesses?

Scale Out

similar questions across machines

new bottlenecks?

move data across machines: network!



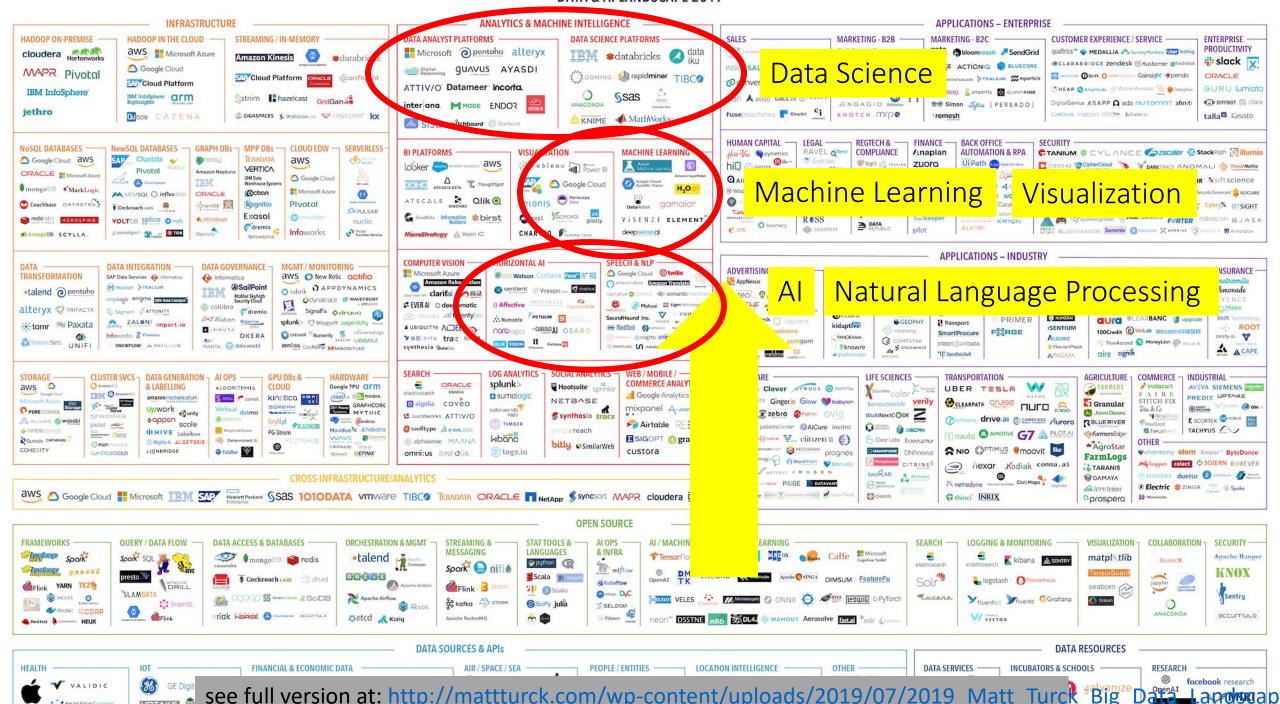
diving into the internals of modern data systems

cutting-edge designs / research projects / engineering projects

CS 561: Data Systems
Architectures

Spring 20





A path in data science

- (1) strong data systems skills
 - (i) coding skills
- (ii) system architecture insights performance tradeoffs

(2) application domain knowledge

(3) statistics, machine learning, math tools

Academic Research

Industry