CS660: Intro to Database Systems

Class 11: Bitmap Indexes

Instructor: Manos Athanassoulis

https://bu-disc.github.io/CS660/

Consider this relation:

```
CREATE TABLE Tweets (
    uniqueMsgID INTEGER, --unique message id
    tstamp TIMESTAMP, --when was the tweet posted
    uid INTEGER, --unique id of the user
    msg VARCHAR (140), --the actual message
    zip INTEGER, --zipcode when posted
    retweet BOOLEAN. --retweeted?
);
```

Attribute	Index?
uniqueMsg	
uid	
zip	
retweet	

Consider this relation:

```
CREATE TABLE Tweets (
    uniqueMsgID INTEGER, --unique message id
    tstamp TIMESTAMP, --when was the tweet posted
    uid INTEGER, --unique id of the user
    msg VARCHAR (140), --the actual message
    zip INTEGER, --zipcode when posted
    retweet BOOLEAN. --retweeted?
):
```

Attribute	Index?
uniqueMsg	B+ Tree
uid	B+ Tree
zip	B+ Tree / Hash
retweet	?

Can we reduce the storage overhead?

Consider this relation:

```
CREATE TABLE Tweets (
    uniqueMsgID INTEGER, --unique message id
    tstamp TIMESTAMP, --when was the tweet posted
    uid INTEGER, --unique id of the user
    msg VARCHAR (140), --the actual message
    zip INTEGER, --zipcode when posted
    retweet BOOLEAN. --retweeted?
):
```

Attribute	Index?	Size?
uniqueMsg	B+ Tree	$N_{msgs} \cdot (key_{size} + rowid_{size})$
uid	B+ Tree	$N_{users} \cdot (key_{size} + C_{users} \cdot rowid_{size})$
zip	B+ Tree / Hash	$N_{zips} \cdot \left(key_{size} + C_{zips} \cdot rowid_{size}\right)$
retweet	?	$2 \cdot (key_{size} + N/2 \cdot rowid_{size})$

Consider this relation:

```
CREATE TABLE Tweets (
    uniqueMsgID INTEGER, --unique message id
    tstamp TIMESTAMP, --when was the tweet posted
    uid INTEGER, --unique id of the user
    msg VARCHAR (140), --the actual message
    zip INTEGER, --zipcode when posted
    retweet BOOLEAN. --retweeted?
):
```

INTEGER = 8B

BOOLEAN = 1B (ideally 1 bit)

RID = 8B

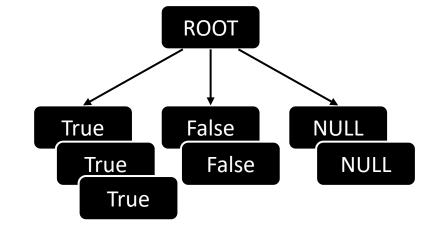
10M tweets, 100K users, 43K zip codes

Attribute	Column Size	Index Nodes Size
uniqueMsg	76MB	152MB
uid	76MB	77MB
zip	76MB	76.6MB
retweet	9.5MB (ideally 1.2MB) 🛑	76MB

Indexing for Low Cardinality Attributes

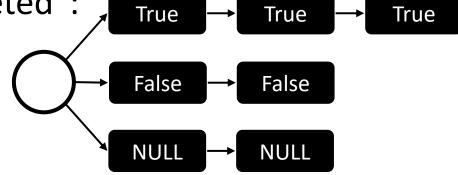
Consider building a **B+ tree** for "retweeted":

- Distinct values: True, False, NULL
- Lots of duplicates for each distinct value
- An awkward B+ tree with three long RID lists



Now consider building a **hash index** for "retweeted":

- All entries will be hashed in three buckets
- No redistribution or rehashing will solve this



Indexing for Low Cardinality Attributes

Now, consider only using **RID lists** for "retweeted":

- Similar to B+ tree
- Traversing them for disjunctive/conjunctive queries is expensive
 OR AND
- Size problem: we keep a RID for every row >> column size

Attribute	Column Size	Index Nodes Size
uniqueMsg	76MB	152MB
uid	76MB	77MB
zip	76MB	76.6MB
retweet	9.5MB (ideally 1.2MB) 🛑	76MB

Patrick O'Neil UMass Boston



Bitmap Index

First commercial system:

Model 204 O'Neil

1987

Bitmap Index

Relation (heap file)

uniqueMsgID	•••	zip	retweet
1		02135	Υ
2		11243	Υ
3		02215	N
4		90765	NULL
5		02134	N
10,000,000		53705	Υ

Bitmap Index on retweet

r-Y	r-N
1	0
1	0
0	1
0	0
0	1
•••	•••
1	0

Query Processing

- 1. Scan "r-N" bitvector
- 2. For each bit set 1 return its position (RID)
- 3. Fetch the corresponding tuples

Critical Issue

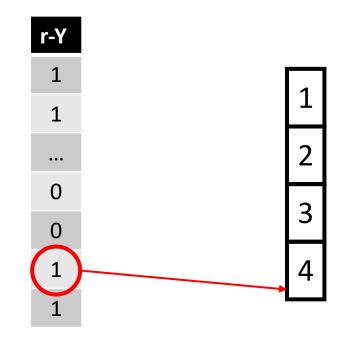
The order of bits in bitmap index **must follow** the order of rows in the file

SELECT * FROM Tweets WHERE retweet = 'Y'

Mapping a bit position to a RID

Assume **fixed records per page** in the heapfile:

- Create the heapfile pages as consecutive pages
- Then construct row id (page_id, slot#) as follows:
 - 1. page_id = bit-position / #records_per_page
 - 2. slot# = bit-position % #records_per_page



Alternatively, rely on a RID index (most systems already have it).

Bitmap Index (other queries)

Relation (heap file)

uniqueMsgID	•••	zip	retweet
1		02135	Υ
2		11243	Υ
3		02215	N
4		90765	NULL
5		02134	N
	•••		•••
10,000,000		53705	Υ

Bitmap Index on retweet

r-Y	r-N	r-NULL
1	0	0
1	0	0
0	1	0
0	0	1
0	1	0
•••	•••	•••
1	0	0

```
SELECT COUNT(*)
FROM Tweets
WHERE retweet = 'Y'

SELECT *
FROM Tweets
WHERE retweet IS NOT NULL

SELECT COUNT(*)
FROM Tweets
```

WHERE retweet IS NULL

Attribute	Column Size	Index Nodes Size	Bitamp Index Size
retweet	9.5MB (ideally 1.2MB)	76MB	(3 bitvectors of 10M entries) 3.6MB

Index Sizes

Consider this relation:

```
CREATE TABLE Tweets (
    uniqueMsgID INTEGER, --unique message id
    tstamp TIMESTAMP, --when was the tweet posted
    uid INTEGER, --unique id of the user
    msg VARCHAR (140), --the actual message
    zip INTEGER, --zipcode when posted
    retweet BOOLEAN. --retweeted?
```

INTEGER = 8B

BOOLEAN = 1B (ideally 1 bit)

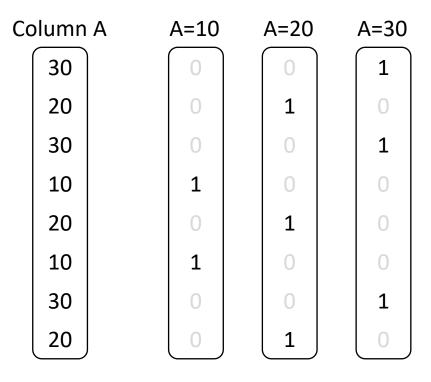
RID = 8B

10M tweets, 100K users, 43K zip codes

Bitmap Index Size (bytes): #rows * (cardinality+1) / 8

Attribute	Column Size	Index Nodes Size	Bitmap Index Size
uniqueMsg	76MB	152MB	11TB
uid	76MB	77MB	116GB
zip	76MB	76.6MB	50GB
retweet	9.5MB (ideally 1.2MB)	76MB —	3.6MB

Benefits of Bitmap Indexing



Specialized indexing

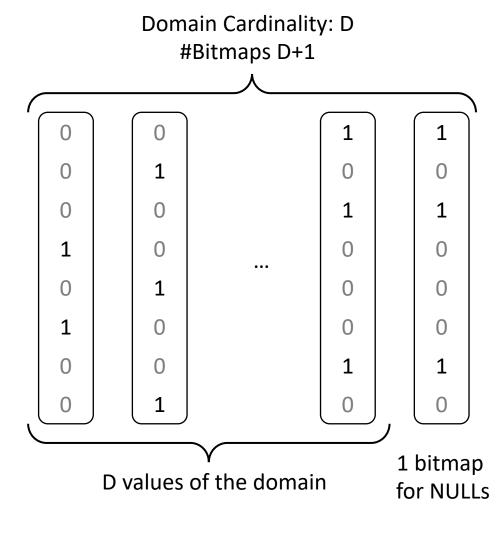
- Compact representation of query result
- Query result is readily available

Bitvectors

- Can leverage fast Boolean operators
- Bitwise AND/OR/NOT faster than looping over meta data

Storing a Bitmap Index

Column col_width: 32bits



A bitmap **per domain value** and **1 for NULLs** Each bitmap can be stored as a separate file

→ Store one bit for every value for every row

Column size (bits) = #rows * col_width

Bitmap Idx size (bits) = #rows * (cardinality+1)

if *cardinality+1 < col_width*, then the bitmap index is smaller than the column!

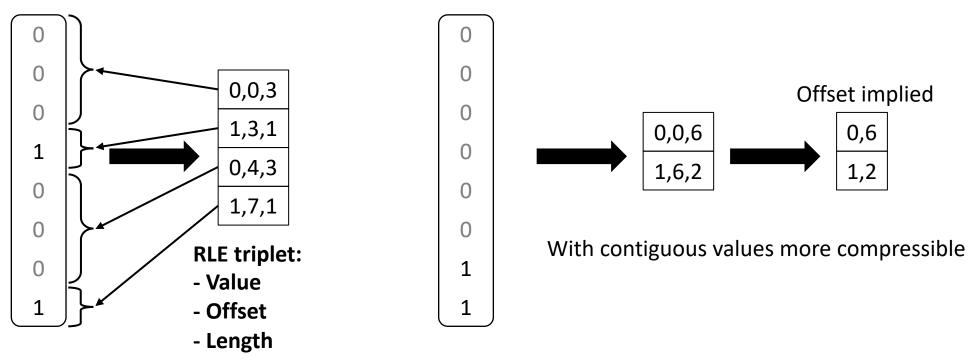
If I use **32-bit integers** but only store **10 values**: column size **32*N**, while bitmap idx size **11*N**

Even better:

Bitmaps are highly compressible!

How to Compress a Bitmap?

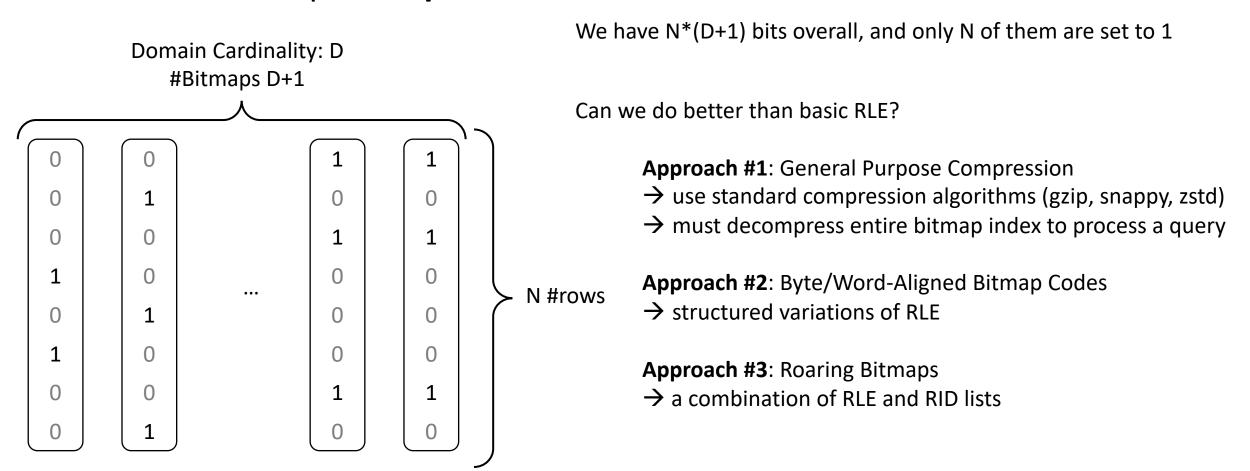
Represent consecutive bit-values with their count "Run-Length Encoding"



Can we make the bitvector more compressible?

How to Compress a Bitmap?

Observation: Bitmaps are sparse!



Divide bitmap into chunks that contain different categories of bytes:

→ Gap Byte: All the bits are 0s

→ Tail Byte: Some bits are 1s

Encode each **chunk** that consists of **Gap Bytes** followed by **Tail Bytes**

- → Gap Bytes are compressed with RLE
- → **Tail Bytes** are stored **uncompressed** unless consisting of only 1-byte or has only one non-zero bit.

Bitmap

0000000	00000000	00000000	00100000
0000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
0000000	00000000	00000000	00000000
00000000	00000000	01000000	00100010

Compressed Bitmap

Bitmap			Tail bytes
00000000	00000000	00000000	00100000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	01000000	00100010
			Tail bytes

Compressed Bitmap

	Bitmap G	ap bytes		Tail bytes
I	00000000	00000000	00000000	00100000
Ī	0000000	00000000	00000000	00000000
	00000000	00000000	00000000	00000000
	0000000	00000000	00000000	00000000
	00000000	00000000	01000000	00100010

Compressed Bitmap

#1

Bitmap

#	1
#	т,

#2

00000000	00000000	00000000	00100000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	01000000	00100010

Compressed Bitmap

00100010

Bitmap

00000000

00000000

 00000000
 00000000
 00100000

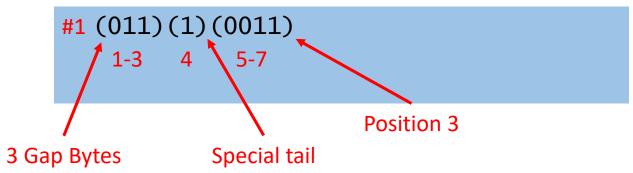
 00000000
 00000000
 00000000

 00000000
 00000000
 00000000

 00000000
 00000000
 00000000

01000000

Compressed Bitmap



00000000

Chunk #1 (Bytes 1-4)

Header Byte:

- → Number of Gap Bytes (bits 1-3)
- \rightarrow Is the tail special? (bit 4)
- \rightarrow bits 5-7:
- Number of verbatim bytes (if bit 4=0)
- Index of 1-bit in tail byte (if bit 4=1)

No extra gap length bytes since gap length < 7 No verbatim bytes since tail is special

Bitmap

00000000	00000000	00000000	00100000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	01000000	00100010

Chunk #2 (Bytes 5-20)

Header Byte:

- → 14 Gap Bytes, 2 Tail Bytes (not special)
- \rightarrow #gaps > 6, so we must use extra byte

Compressed Bitmap

```
#1 (011)(1)(0011)
#2 (111)(0)(0010) 00001110
01000000 00100010
```

One gap length byte
Two verbatim bytes for tail

#2

Bitmap

00000000	00000000	00000000	00100000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	01000000	00100010

Compressed Bitmap

```
#1 (011)(1)(0011)
#2 (111)(0)(0010) 00001110
01000000 00100010
```

for > 6 gap bytes, use 111

Chunk #2 (Bytes 5-20)

Header Byte:

- → 14 Gap Bytes, 2 Tail Bytes (not special)
- \rightarrow #gaps > 6, so we must use extra byte

One gap length byte
Two verbatim bytes for tail

Bitmap

00000000	00000000	00000000	00100000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	00000000	00000000
00000000	00000000	01000000	00100010

Compressed Bitmap

```
#1 (011) (1) (0011)
#2 (111) (0) (0010) 00001110
01000000 00100010 Gap Length = 14
```

Chunk #2 (Bytes 5-20)

Header Byte:

- → 14 Gap Bytes, 2 Tail Bytes (not special)
- \rightarrow #gaps > 6, so we must use extra byte

One gap length byte
Two verbatim bytes for tail

Bitmap

00000000	00000000	00000000	00100000
00000000	00000000	0000000	00000000
00000000	00000000	0000000	00000000
00000000	00000000	0000000	00000000
00000000	00000000	01000000	00100010

Chunk #2 (Bytes 5-20)

Header Byte:

- → 14 Gap Bytes, 2 Tail Bytes (not special)
- \rightarrow #gaps > 6, so we must use extra byte

```
Compressed Bitmap 2 verbatim bytes

#1 (011) (1) (0011)

#2 (111) (0) (0010) 00001110

01000000 00100010

Verbatim Tail Bytes

Not special tail
```

One gap length byte
Two verbatim bytes for tail

Original Bitmap Size: 20 bytes

BBC Compressed: 5 bytes

Observation for BBC

Oracle's BBC is an **obsolete** format

- → Although it provides *good compression*, it is slower than recent alternatives due to **excessive branching** (too many if statements)
- → Word-Aligned Hybrid (WAH) encoding is a patented variation on BBC that provides better performance.

None of these support **random** access.

→ to check a specific bit, decompress the whole thing

Also: hard to update (flip a single bit)!

What is a "word"?

Word is the unit a processor reads: 32 bits or 64 bits (4 or 8 bytes)

BBC had a lot of CPU overhead

Idea: fetch words which is the natural size the CPU reads

Two types of words

- → fill words (similar to gap)
- → literal words (similar to verbatim)

10001000 01001000 01000100 01000100 most significant bit: 0 for literal and 1 for fill 0000000 001001000 00111000 00100101

Two types of words

- → fill words (similar to gap)
- → literal words (similar to verbatim)

```
10001000 01001000 01000100 01000100 second most significant bit:
```

fill bit

Two types of words

- → fill words (similar to gap)
- → literal words (similar to verbatim)

10001000 01001000 01000100 01000100

remaining (w-2) bits: fill length = 138953796 zeros

Two types of words

- → fill words (similar to gap)
- → literal words (similar to verbatim)

```
101000 01001000 01000100 01000100 second most significant bit:
```

fill bit

Two types of words

- → fill words (similar to gap)
- → literal words (similar to verbatim)

```
1 001000 01001000 01000100 01000100

remaining (w-2) bits:
fill length = 138953796 ones
```

Two types of words

- → fill words (similar to gap)
- → literal words (similar to verbatim)

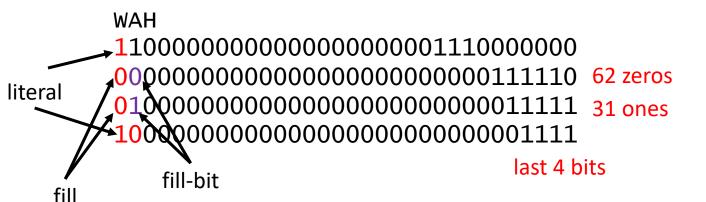
10001000 01001000 01000100 01000100

remaining (w-1) bits:

literal bits

Word-Aligned Hybrid (WAH) Code - example

Word-Aligned Hybrid (WAH) Code - example



Encodes 2^30 (1 billion) consecutive bits with 1 word

Positive Implication:

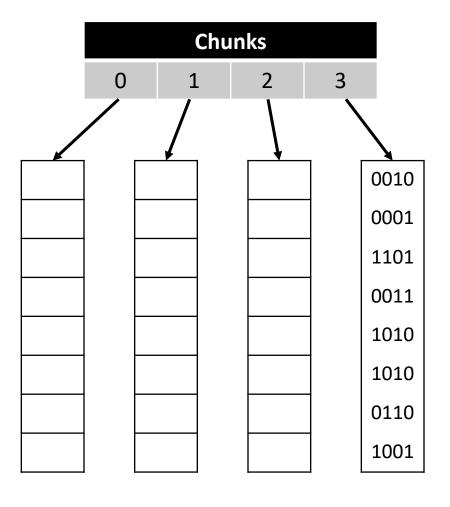
A rare column-value is encoded with 1 word instead of a huge bitvector

BUT: if a few sparse bits are set query processing take time (de-encoding > expensive than accessing data)

Store 32-bit integers (RIDS) in a compact two-level indexing data structure

- → Dense chunks are stored using bitmaps
- → Sparse chunks use packed arrays of 16-bit integers

Used in Lucene, Hive, Spark, Pinot.

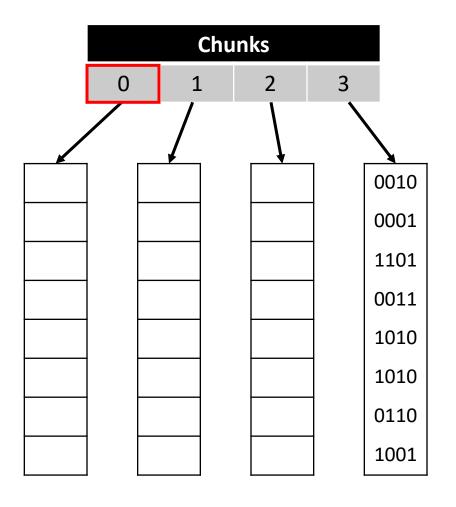


For each value k, assign it to a chunk based on k/2^16

→ Store k in the chunk's container

If # of values in container < 4096, store as array. Otherwise, store as Bitmap.

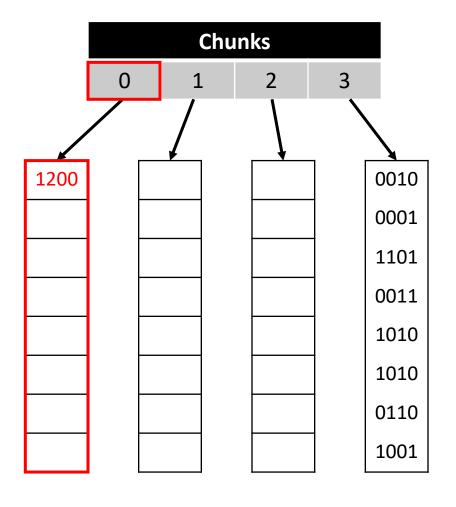
k = 1200



For each value k, assign it to a chunk based on k/2^16

→ Store k in the chunk's container

If # of values in container < 4096, store as array. Otherwise, store as Bitmap.

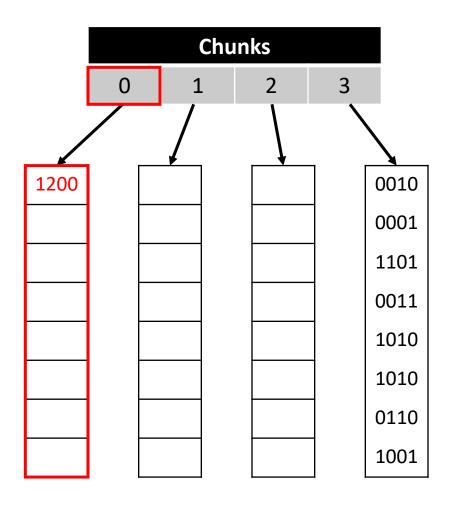


For each value k, assign it to a chunk based on k/2¹⁶

→ Store k in the chunk's container

If # of values in container < 4096, store as array. Otherwise, store as Bitmap.

```
k = 1200
1200 / 2^16 = 0
1200 % 2^16 = 1200
```

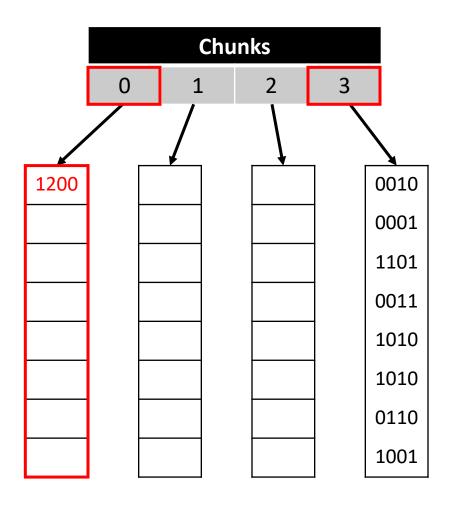


For each value k, assign it to a chunk based on k/2¹⁶

→ Store k in the chunk's container

If # of values in container < 4096, store as array. Otherwise, store as Bitmap.

k = 1200 k = 196626 1200 / 2^16 = 0 1200 % 2^16 = 1200

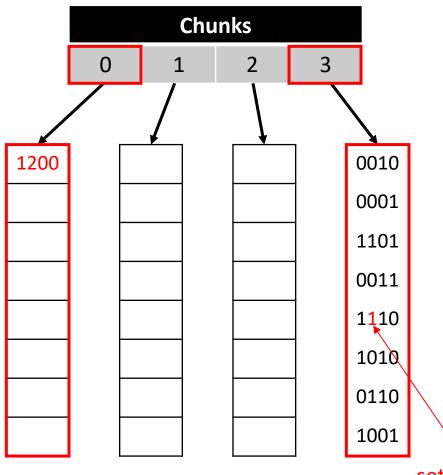


For each value k, assign it to a chunk based on k/2¹⁶

→ Store k in the chunk's container

If # of values in container < 4096, store as array. Otherwise, store as Bitmap.

1200 % 2^16 = 1200

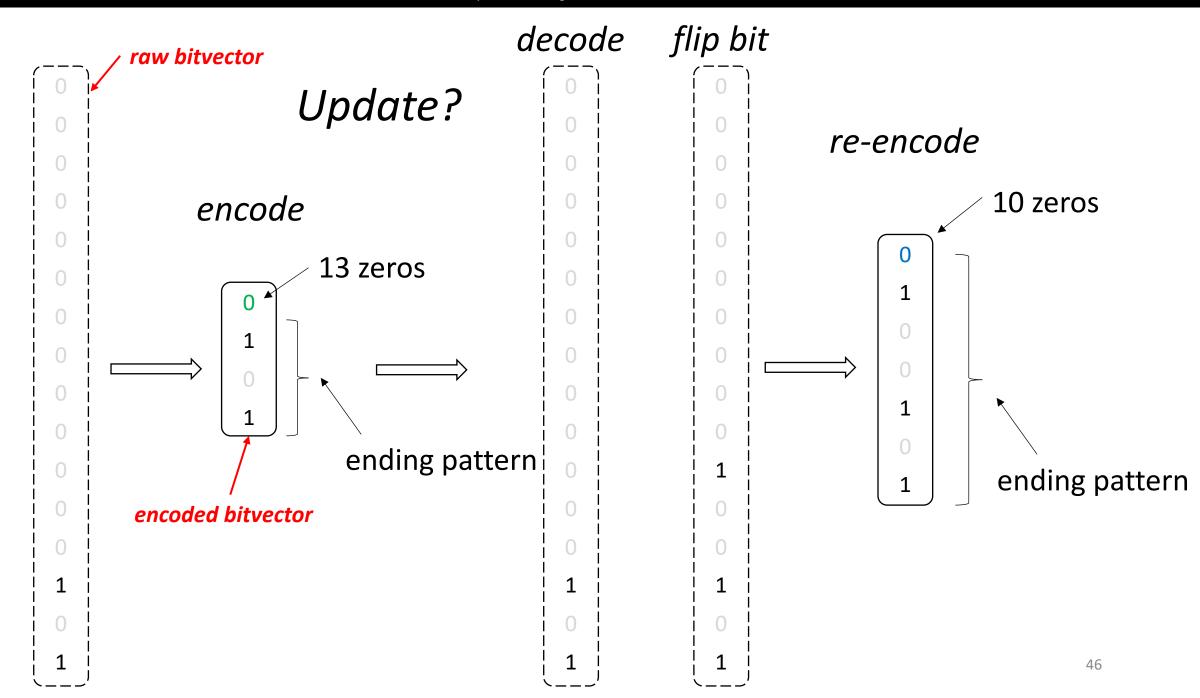


For each value k, assign it to a chunk based on k/2¹⁶

→ Store k in the chunk's container

If # of values in container < 4096, store as array. Otherwise, store as Bitmap.

Updating Bitmap Indexes



Goal

Bitmap Indexing with efficient *Reads & Updates*

Bitmap Indexing and Deletes

Update Conscious Bitmaps (UCB), SSDBM 2007

A=20

0 1

A=30

EB

efficient deletes by invalidation existence bitvector (EB)

Prior Work: Bitmap Indexing and Deletes

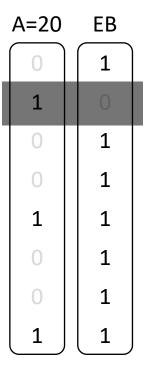
Update Conscious Bitmaps (UCB), SSDBM 2007

A=10	A=20	A=30	EB
	0	1	1
0	1	0	0
0	0	1	1
1	0	0	1
0	1	0	1
1	0	0	1
0	0	1	1
0	1	0	1

efficient deletes by invalidation existence bitvector (EB)

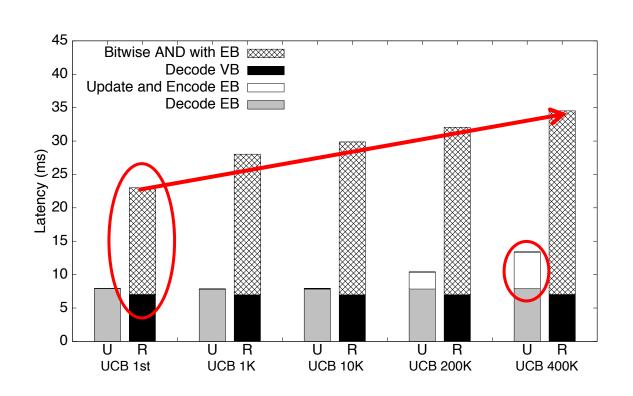
reads?
bitwise AND with EB

updates?
delete-then-append



Limitations

n=100M tuples, d=100 domain values, 50% updates / 50% reads



read cost increases with #updates

why?

bitwise AND with EB is the bottleneck

update EB is costly for >> #updates

UCB performance does not scale with #updates

single auxiliary bitvector

repetitive bitwise operations

Bitmap Indexing for Reads & Updates



distribute update cost



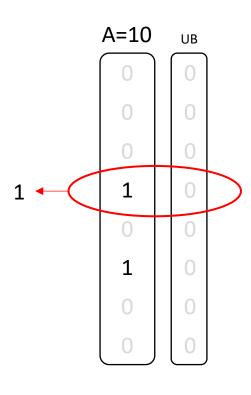
efficient random accesses in compressed bitvectors



query-driven re-use results of bitwise operations



Design Element 1: update bitvectors



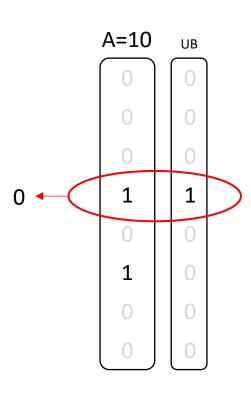
one per value of the domain initialized to 0s

the current value is the XOR

every update flips a bit on UB



Design Element 1: update bitvectors

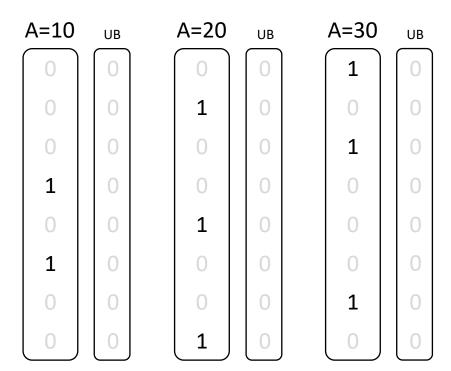


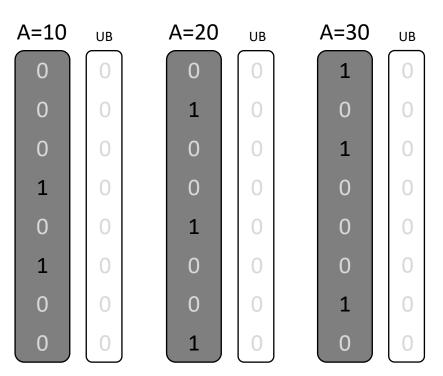
one per value of the domain initialized to 0s

the current value is the XOR

every update flips a bit on UB

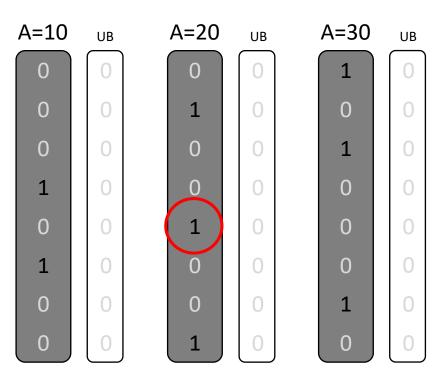
... row 5 to 10





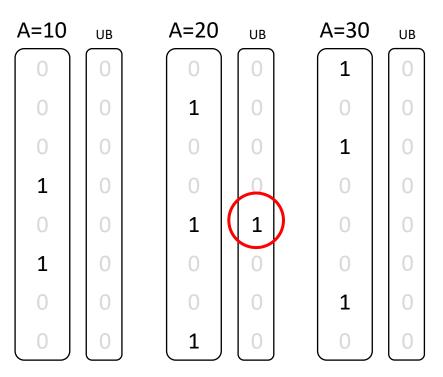
... row 5 to 10

1. find old value of row 5 (A=20)

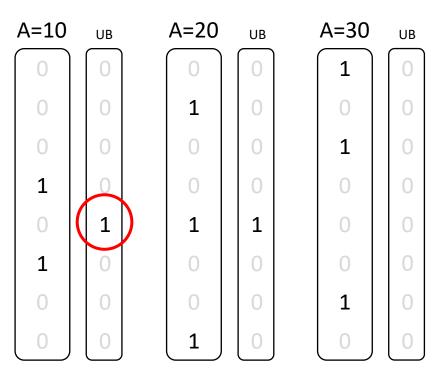


... row 5 to 10

1. find old value of row 5 (A=20)



- ... row 5 to 10
- 1. find old value of row 5 (A=20)
- 2. flip bit of row 5 of UB of A=20



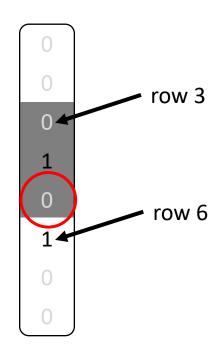
... row 5 to 10

- 1. find old value of row 5 (A=20)
- 2. flip bit of row 5 of UB of A=20
- 3. flip bit of row 5 of UB of A=10

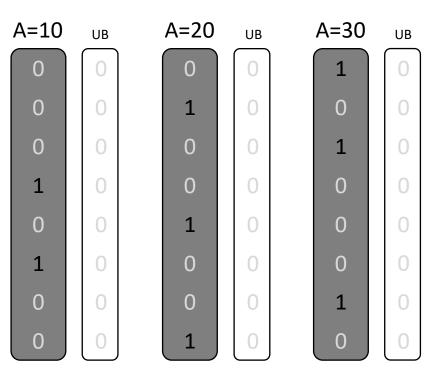


Design Element 2: fence pointers

efficient access of compressed bitvectors fence pointers

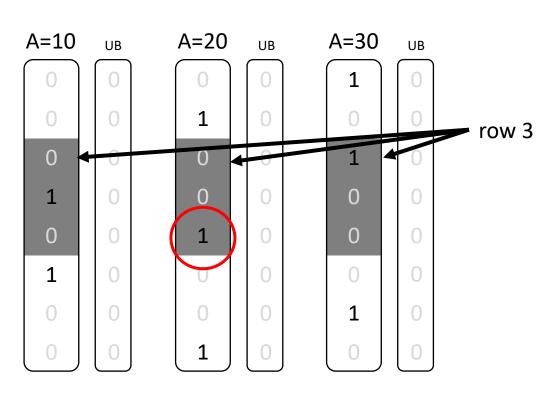


we can find row 5 without decoding & scanning the whole bitvector



- ... row 5 to 10
- 1. find old value of row 5 (A=20)

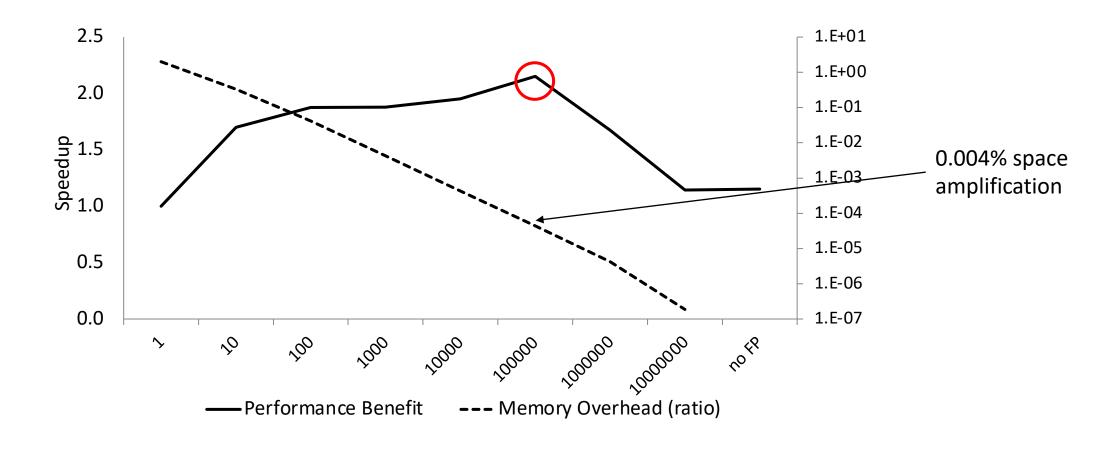
Updating UpBit (with fence pointers)...



... row 2 to 10

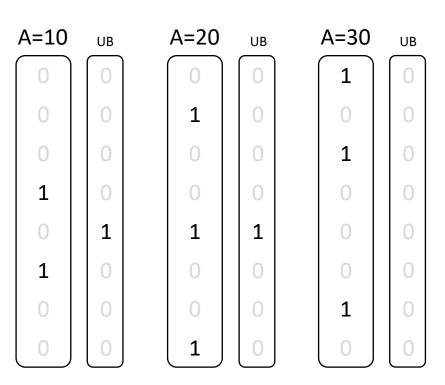
1. find old value of row 2 (A=20) using fence pointers

How dense should the fence pointers be?



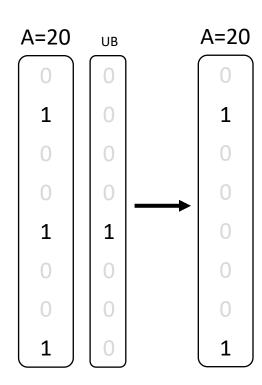
Querying

Querying UpBit ...



... A = 20 Return the XOR of A=20 and UB

Querying UpBit ...



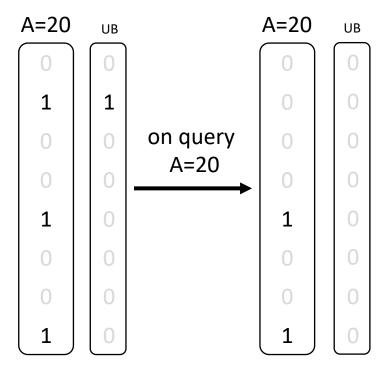
... A = 20

Return the XOR of A=20 and UB

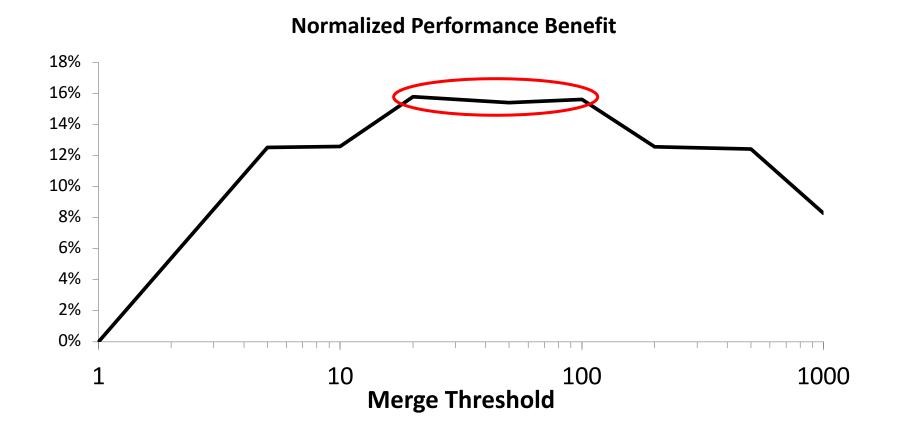


Design Element 3: query-driven merging

maintain high compressibility of UB query-driven merging



How frequently to merge UB back to VB?

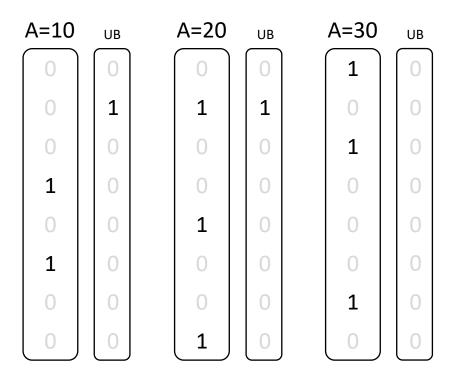


Deleting

UpBit: Updatable Bitmap Index

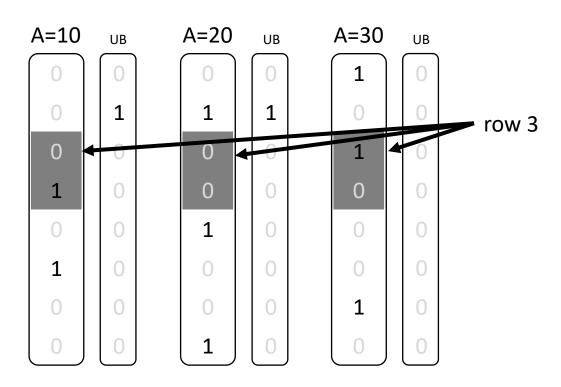
Deleting ...

... row 3



UpBit: Updatable Bitmap Index

Deleting ...

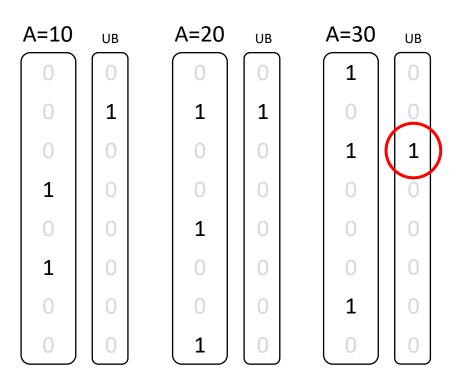


... row 3

1. find value of row 3 (A=30) using fence pointers

UpBit: Updatable Bitmap Index

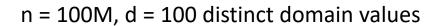
Deleting ...

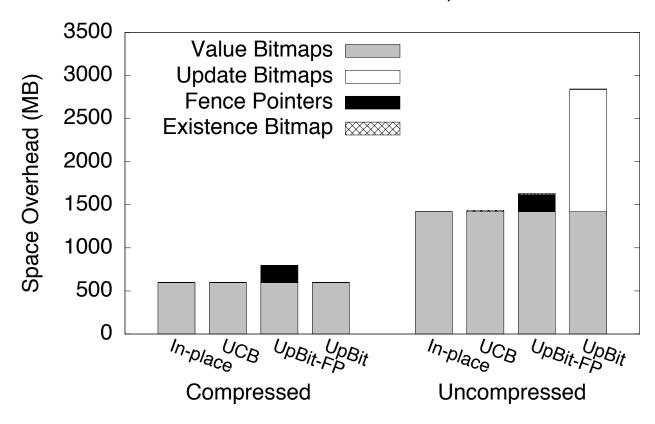


... row 3

- 1. find value of row 3 (A=30) using fence pointers
- 2. flip bit of row 3 of UB of A=30

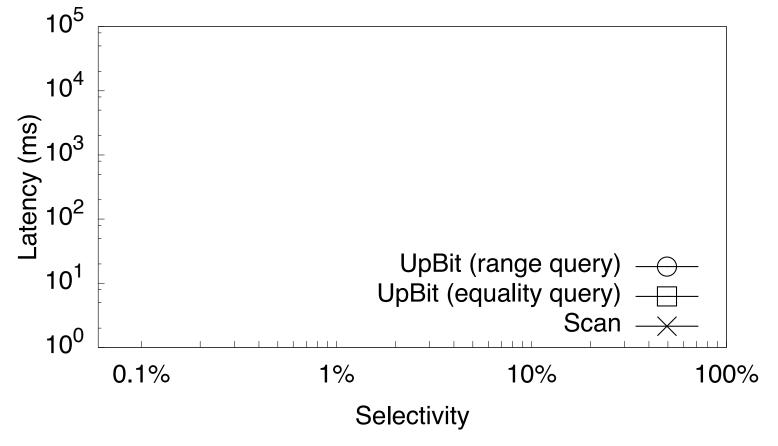
Memory Consumption





UpBit as a general index: UpBit vs. Scan

n = 1B, d = 1000 distinct domain values (range) n = 1B, d varies for equality: 1000,100,10,1



Scan

tight for-loop SIMD multi-core

Equality query

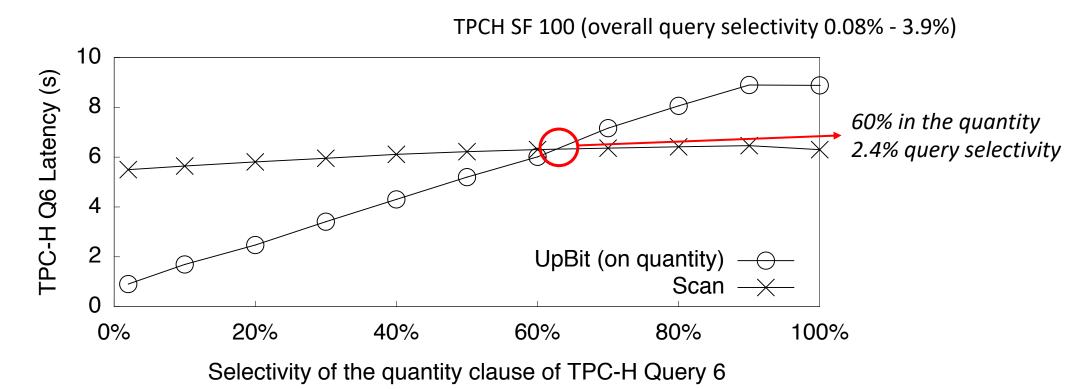
all qualifying tuples have the same value (always 1 bitvector)

Range query

qualifying tuples may have many value (bit-OR bitvectors)

break-even: 10% for equality queries and 1% for range queries

UpBit as a general index: UpBit vs. Scan TPCH Q6



SELECT sum(l_extendedprice * l_discount) as revenue FROM lineitem
WHERE l_shipdate >= date '[DATE]'
AND l_shipdate < date ' [DATE] ' + interval '1 ' year

an update-aware bitmap index is a viable *general-purpose index*