

Lecture 0: Introduction

Yi, Yung (이용)

EE210: Probability and Introductory Random Processes
KAIST EE

August 27, 2022

August 27, 2022 1 / 20

Outline

- Course logistics
- Why this course?

August 27, 2022 2 / 20

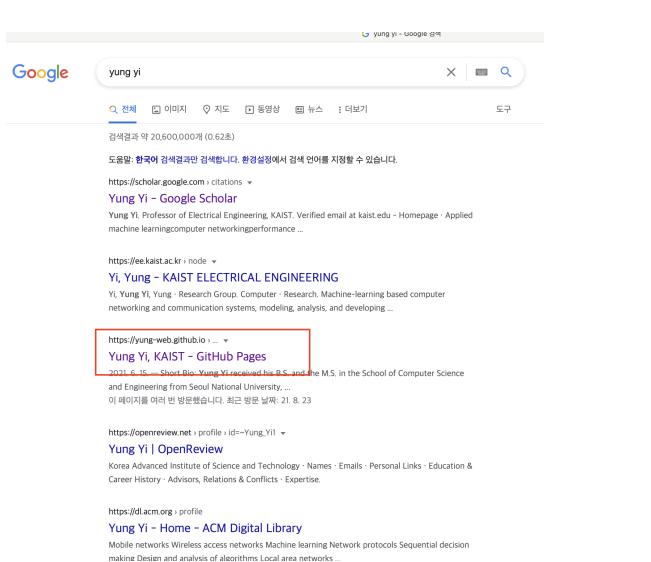
- Yi, Yung (이용)
- Office: N1, 810
- Homepage: <https://yung-web.github.io/home/>
- E-mail: yiyung@kaist.edu
- Computer Division
- In KAIST EE since 2008

How to Run This Course

- All lecture videos have already been pre-recorded. Available in **YouTube**.
- **non-real-time online ($\leq 50\%$) + real-time offline/online ($\geq 50\%$)**
- **non-real-time online**: Watch and study anytime and anywhere you like.
- **realtime offline/online**: Watch lecture videos in the classroom or in the zoom, with asking and answering questions.
- No attendance check!

Accessing Lecture Videos and Slides

- Method 1:
<https://yung-web.github.io/home/courses/probability.html>
- Method 2: (a) Type **Yung Yi** in the google, (b) visit his [GitHub homepage](#), (c) find the links on [Course](#).



Google search results for "yung yi":

- <https://scholar.google.com/citations> - Yung Yi - Google Scholar
- <https://ee.kaist.ac.kr/~node/> - **Yi, Yung - KAIST ELECTRICAL ENGINEERING**
Yi, Yung Yi, Yung - Research Group: Computer - Research: Machine-learning based computer networking and communication systems, modeling, analysis, and developing ...
- <https://yung-web.github.io/> - **Yung Yi, KAIST - GitHub Pages**
2017.6.15. — Short Bio: Yung Yi received his B.S. and the M.S. in the School of Computer Science and Engineering from Seoul National University, ...
이 페이지를 여러 번 방문했습니다. 최근 방문 날짜: 21. 8. 23
- <https://openreview.net/profile?id=Yung.Yii> - **Yung Yi | OpenReview**
Korea Advanced Institute of Science and Technology · Names · Emails · Personal Links · Education & Career History · Advisors, Relations & Conflicts · Expertise.
- <https://dl.acm.org/profile> - **Yung Yi - Home - ACM Digital Library**
Mobile networks Wireless access networks Machine learning Network protocols Sequential decision making Design and analysis of algorithms Local area networks ...



Short Bio: Yung Yi received his B.S. and the M.S. in the School of Computer Science and Engineering from Seoul National University in 1997 and 1999, respectively, and his Ph.D. in the Department of Electrical and Computer Engineering at the University of Texas at Austin in 2006. From 2006 to 2008, he was a post-doctoral research associate in the Department of Electrical Engineering at KAIST, South Korea. His current research interests include machine learning, design and analysis of wired/wireless networking systems. He was the recipient of two best paper awards at SECON 2013 and ACM MobiHoc 2013. He was the co-recipient of IEEE William R. Bennett Award, 2016.

LANADA (Laboratory of Network Architecture, Design, and Analysis)

LANADA is a research group which I currently lead. Currently, we do not hire new graduate students.

Students advised (PhD)

1. Jimung Lee, 2012, Postdoc at U. of Colorado
2. Jihyeong Lee, 2014, Sony Ericsson, Sweden
3. Joohyun Lee, 2014, Hanyang Univ.
4. Hanjin Park, 2015, National Security Research Institute
5. Donghyun Kim, 2016, Naver
6. Sochwan Lee, 2016, ETRI
7. Jinhyeong Lee, 2016, SK Telecom
8. Hyeyoung Jang, 2016, Donguk Univ.
9. Jungseok Oh, 2017, POSTECH
10. Hyojeong Lee, 2017, Samsung

Education

- Ph.D. Dept. of Electrical and Computer Engineering, University of Texas at Austin, 2006 - Current
- M.S. Dept. of Computer Science and Engineering, Seoul National University, 1999
- B.S. Dept. of Computer Science and Engineering, Seoul National University, 1997

Position

- KAIST Chair Professor (KAIST 총장(校長)) Dept. of Electrical Engineering, KAIST, 2007 - Current
- Full Professor, Dept. of Electrical Engineering, KAIST, 2018.2 - Current
- Associate Professor, Dept. of Electrical Engineering, KAIST, 2011.8 - 2018.2
- Assistant Professor, Dept. of Electrical Engineering, KAIST, 2008.8 - 2011.8
- Postdoctoral Research Associate, Dept. of Electrical Engineering Princeton University, 2006.8 - 2008.8

Courses

- Probability and Introductory Random Process (video included), Undergraduate
- Data Structures for Electrical Engineers, Undergraduate
- Mathematics for Machine Learning, Undergraduate
- Computer Network, Undergraduate
- Complex Network Analysis: Epidemics and Rumours (video included), Graduate

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August 27, 2022

5 / 20

Using KLMS and Campuswire

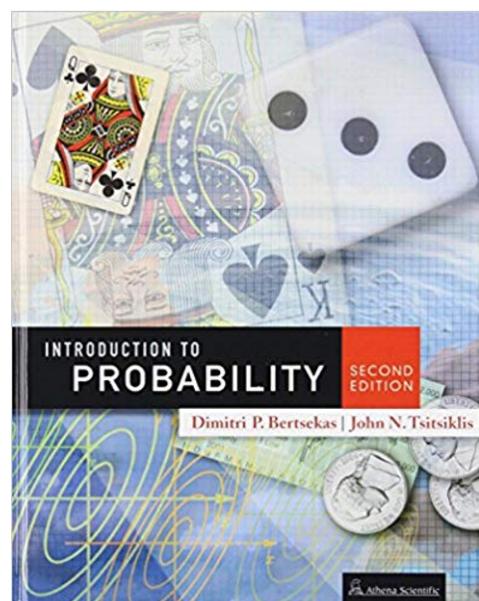
- KLMS:** All notifications and announcements (also sent to you via email)
- KLMS:** Homework upload
- KLMS:** Score upload and all the grade-related things
- Campuswire:** All Questions (course contents, logistics, etc). Should be in English.
- NOT individual emails to the instructor or the TAs
- Emails to the instructor, Prof. Yung Yi, are allowed for handling private situations.

August 27, 2022

6 / 20

Textbook

- Introduction to Probability
(2nd edition)
 - MIT course textbook
 - Dimitri P. Bertsekas and John N. Tsitsiklis
- You can order it from Yes24, Aladin, Kyobo
 - Yes24: <http://www.yes24.com/Product/Goods/3995311>
 - Aladin: <https://www.aladin.co.kr/shop/wproduct.aspx?ItemId=12945615>
 - Kyobo: <http://www.kyobobook.co.kr/product/detailViewEng.laf?ejkGb=ENG&mallGb=ENG&barcode=9781886529380&orderClick=LAG&Kc=>



- <http://athenasc.com/probbook.html>
- **Solutions for all problems** (so you have all solutions for your homework)
- Links to the old MIT courses
- You can find the urls (2006, 2010, 2013) for the MIT lectures based on the same textbook, where there are many useful resources (recitation problems, homework problems, old exam problems, etc)
- Some of my lecture slides are based on theirs, but my slides are largely modified/reorganized/edited in many places for our purpose.

Course Contents (Guided Schedule for Your Study)

1. Probabilistic model (0.5 week)
2. Conditioning and Independence (0.5 week)
3. Random Variable, Part I (Discrete Random Variable) (1.5 week)
4. Random Variable, Part II (Continuous Random Variable) (1.5 week)
5. Random Variable, Part III (Advanced Topic on Random Variable) (1.5 week)
6. Limit of Scaled Sum of Random Variables: Central Limit Theorem and Weak Law of Large Numbers (1.5 week)
7. Random Process: Bernoulli and Poisson Processes (2 week)
8. Random Process: Markov Chain (2 week)
9. Introduction to Statistical Inference (2 week)

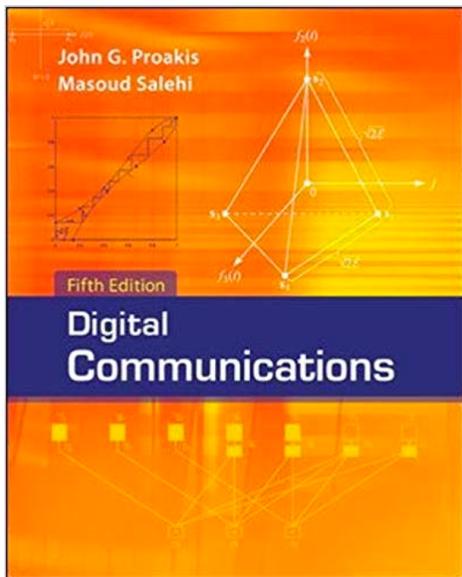
- 2 Exams (mid-term and final)
- Homeworks
 - All problems are from exercise problems in the textbook.
 - We do NOT check whether you copy your solution from the problem solutions or not.
- 9 Homeworks for each of 9 chapters.

- Read **ALL** the emails.
- Need to buy the textbook?
 - Strongly recommend it. Taking a course is NOT just solving mid-term and final exam problems and getting a good grade.
- OK not to be present in the classroom? Yes.
- OK that my homework solutions is same as those in the solutions book? Yes.
- Can I ask for a personal meeting to ask questions or get other general advices?
Sure. Send me an email.

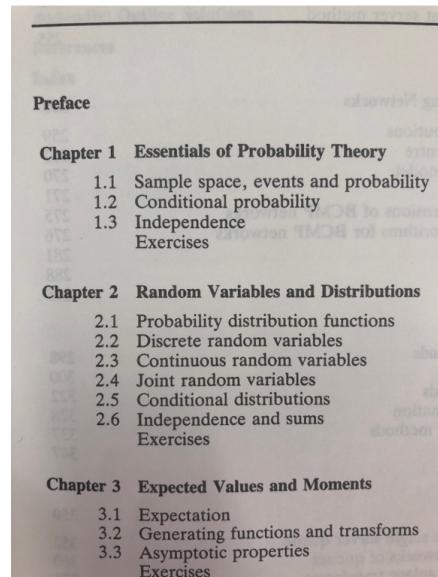
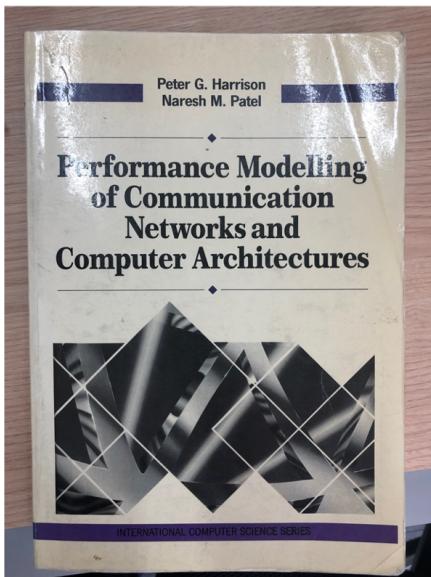
Questions?

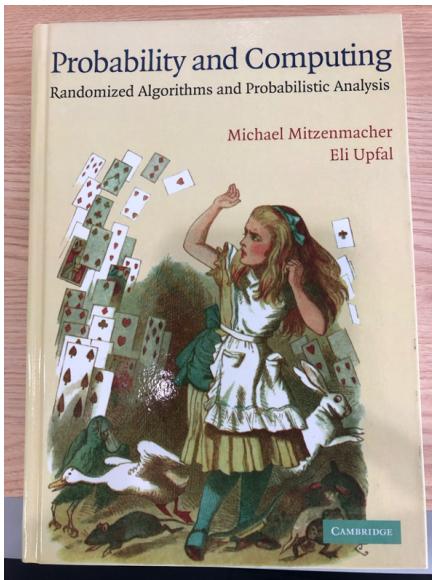
Why Probability?

- Many things are "probabilistic"
- Assume that you are a designer of the following engineering systems. Good design?
 - a web server
 - a communication device like mobile phones
 - an AI-based image classifier
- From an engineering point of view,
 - System input
 - Algorithms in systems
 - Analysis of systems

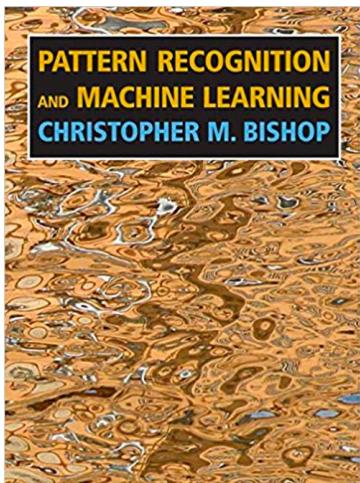


Communications 1-5 Overview of the Book 1-6 Bibliographical Notes and References	13 16 16
2 Probability and Stochastic Processes	
2-1 Probability 2-1-1 Random Variables, Probability Distributions, and Probability Densities 2-1-2 Functions of Random Variables 2-1-3 Statistical Averages of Random Variables 2-1-4 Some Useful Probability Distributions 2-1-5 Upper bounds on the Tail Probability 2-1-6 Sums of Random Variables and the Central Limit Theorem	17 17 22 28 33 37 53 58
2-2 Stochastic Processes 2-2-1 Statistical Averages 2-2-2 Power Density Spectrum 2-2-3 Response of a Linear Time-Invariant System to a Random Input Signal 2-2-4 Sampling Theorem for Band-Limited Stochastic Processes 2-2-5 Discrete-Time Stochastic Signals and Systems 2-2-6 Cyclostationary Processes	62 64 67 68 72 74 75 77
2-3 Bibliographical Notes and References Problems	77 77





Preface 1 Events and Probability 1.1 Application: Verifying Polynomial Identities 1.2 Axioms of Probability 1.3 Application: Verifying Matrix Multiplication 1.4 Application: A Randomized Min-Cut Algorithm 1.5 Exercises	2 Discrete Random Variables and Expectation 2.1 Random Variables and Expectation 2.1.1 Linearity of Expectations 2.1.2 Jensen's Inequality 2.2 The Bernoulli and Binomial Random Variables 2.3 Conditional Expectation 2.4 The Geometric Distribution 2.4.1 Example: Coupon Collector's Problem 2.5 Application: The Expected Run-Time of Quicksort 2.6 Exercises
3 Moments and Deviations 3.1 Markov's Inequality 3.2 Variance and Moments of a Random Variable 3.2.1 Example: Variance of a Binomial Random Variable 3.3 Chebyshev's Inequality 3.3.1 Example: Coupon Collector's Problem 3.4 Application: A Randomized Algorithm for Computing the 3.4.1 The Algorithm 3.4.2 Analysis of the Algorithm 3.5 Exercises	...



xiv CONTENTS Copyrighted Material	xiii Copyrighted Material
2 Probability Distributions 2.1 Binary Variables 2.1.1 The beta distribution 2.2 Multinomial Variables 2.2.1 The Dirichlet distribution 2.3 The Gaussian Distribution 2.3.1 Conditional Gaussian distributions 2.3.2 Marginal Gaussian distributions 2.3.3 Bayes' theorem for Gaussian variables 2.3.4 Maximum likelihood for the Gaussian 2.3.5 Sequential estimation 2.3.6 Bayesian inference for the Gaussian 2.3.7 Student's t-distribution 2.3.8 Periodic variables 2.3.9 Mixtures of Gaussians 2.4 The Exponential Family 2.4.1 Maximum likelihood and sufficient statistics 2.4.2 Conjugate priors 2.4.3 Noninformative priors 2.5 Nonparametric Methods 2.5.1 Kernel density estimators 2.5.2 Nearest-neighbour methods Exercises 67 68 71 74 76 78 85 88 90 93 94 97 102 105 110 113 116 117 117 120 122 124 127	
3 Linear Models for Regression 3.1 Linear Basis Function Models 3.1.1 Maximum likelihood and least squares 3.1.2 Geometry of least squares 3.1.3 Sequential learning 3.1.4 Regularized least squares 137 138 140 143 143 144	

These days, every area in CS and EE is directly or indirectly related to machine learning!

- Designer's perspective?
- In the year of 2022, suppose that unfortunately there is no theory of mathematically studying the *uncertainty* of some phenomena, events, etc.
- You have to design such a theory called "probability". How are you going to do it? Where are you going to start?
- You just have other basic mathematical theories such as set theory.
- You need to get used to the *English terms* on probability (e.g., sample space = 표본공간, probability density function = 확률밀도함수).
- We will take this exciting journey from the next lecture!

Questions?

