



# CSE 215: Database

Department of CSE  
Bangladesh University of Engineering & Technology



## What is it?

- The ER data model employs three basic concepts:
  - entity sets
  - relationship sets
  - attributes
- The ER model also has an associated diagrammatic representation, which can express the overall logical structure of a database graphically
  - ER diagram



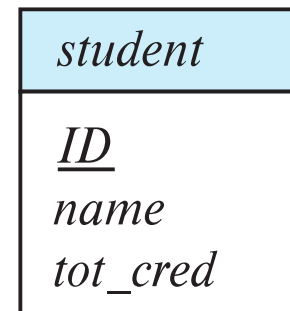
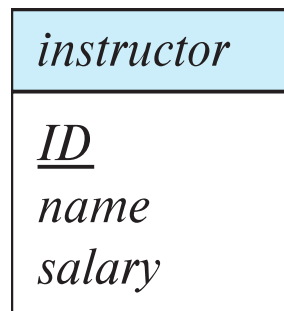
## Entity Sets

- An **entity** is an object that exists and is distinguishable from other objects
  - Example: specific person, company, plant
- An **entity set** is a set of entities of the same type that share the same properties
  - Example: set of all persons, companies, trees,
- An entity is represented by a set of attributes; i.e., descriptive properties possessed by all members of an entity set
  - Example:  
instructor = (ID, name, salary )  
course= (course\_id, title, credits)
- A subset of the attributes form a **primary key** of the entity set; i.e., uniquely identifying each member of the set

## Entity Sets – ER Diagram



- Entity sets can be represented graphically as follows:
  - Rectangles represent entity sets.
  - Attributes listed inside entity rectangle
  - Underline indicates primary key attributes



## Relationship Sets



- A **relationship** is an association among several entities

Example:

44553 (Peltier)      advisor      22222 (Einstein)  
*student* entity   relationship set   *instructor* entity

- A **relationship set** is a mathematical relation among  $n \geq 2$  entities, each taken from entity sets

$$\{(e_1, e_2, \dots, e_n) \mid e_1 \in E_1, e_2 \in E_2, \dots, e_n \in E_n\}$$

where  $(e_1, e_2, \dots, e_n)$  is a relationship

– Example:

$$(44553, 22222) \in \text{advisor}$$

## Relationship Sets



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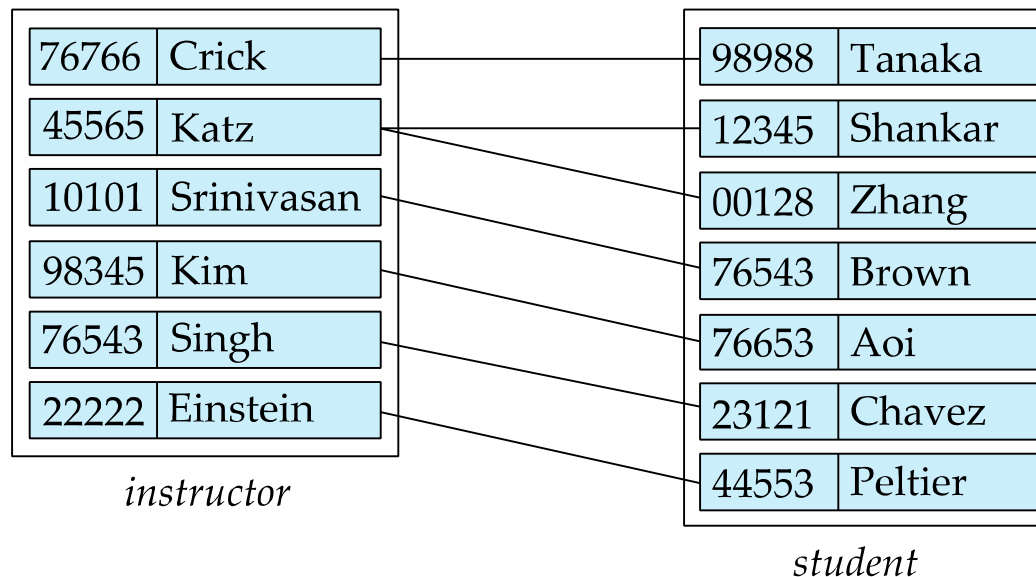
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## Relationship Sets

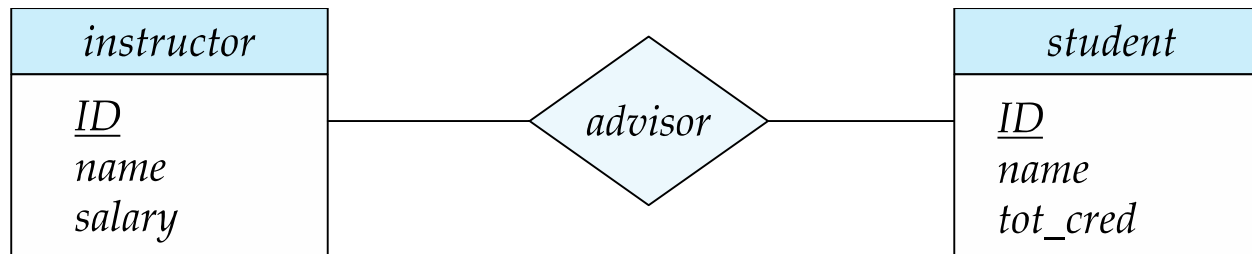


- Example: we define the relationship set *advisor* to denote the associations between students and the instructors who act as their advisors
- Pictorially, we draw a line between related entities



## Relationship Sets-ER Diagram

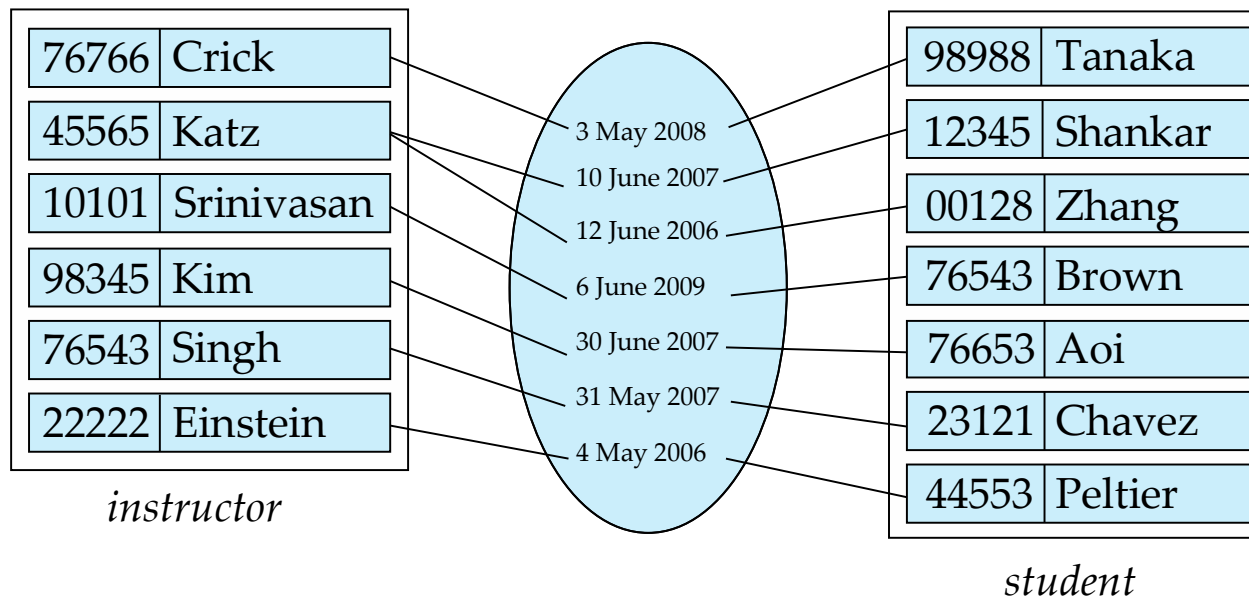
- Diamonds represent relationship sets





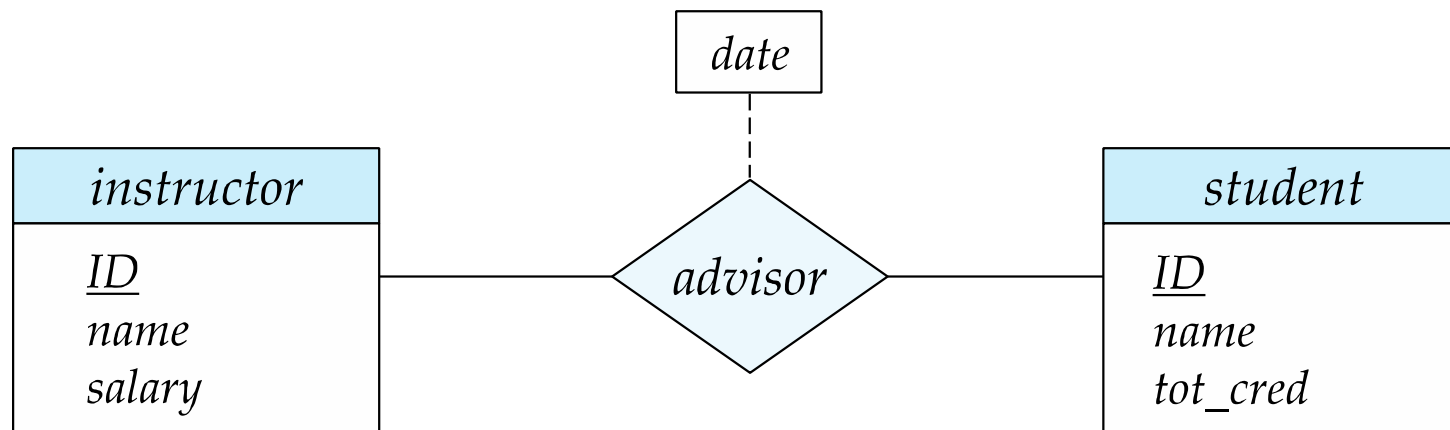
## Relationship Sets

- An attribute can also be associated with a relationship set.
- For instance, the advisor relationship set between entity sets instructor and student may have the attribute date which tracks when the student started being associated with the advisor



## Relationship Sets-ER Diagram

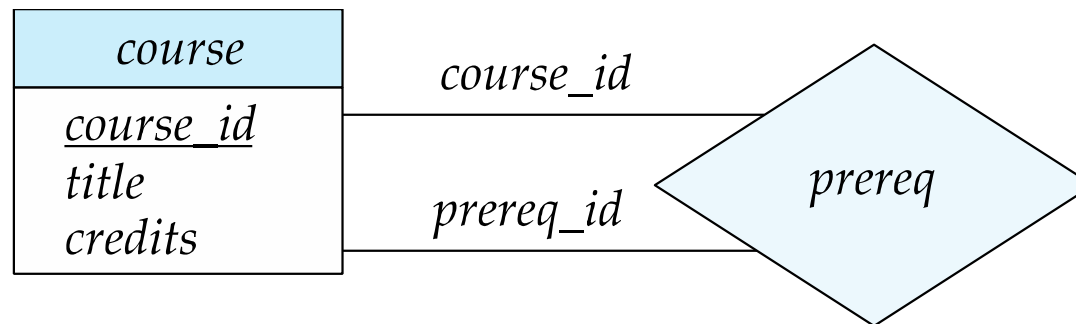
- Diamonds represent relationship sets



## Roles



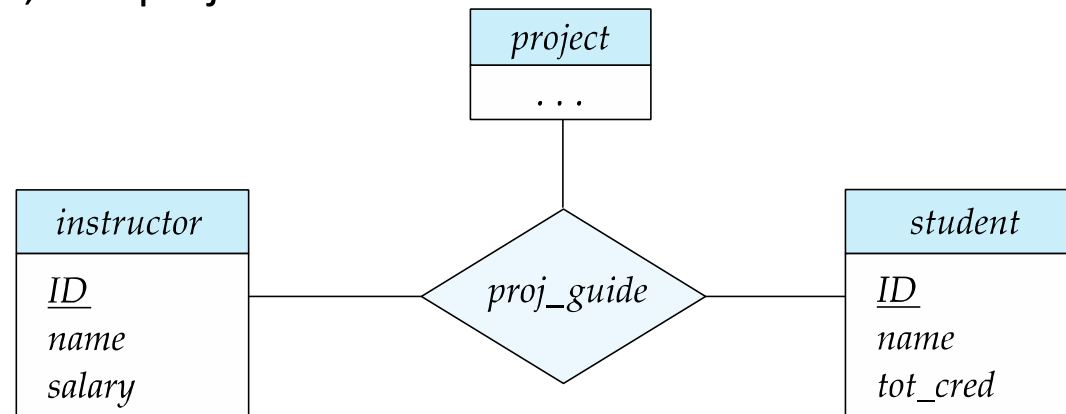
- Entity sets of a relationship need not be distinct
  - Each occurrence of an entity set plays a “**role**” in the relationship
- The labels “course\_id” and “prereq\_id” are called roles.



## Relationship Degree



- Binary relationship
  - Involve two entity sets (or degree two)
- Relationships between more than two entity sets are rare
  - Example: students work on research projects under the guidance of an instructor.
  - relationship `proj_guide` is a ternary relationship between instructor, student, and project



## Attributes



- Attribute types:
  - **Simple** and **composite** attributes
    - Composite attributes allow us to divided attributes into subparts
  - **Single-valued** and **multivalued** attributes
    - Example: multivalued attribute:  
*phone\_numbers*
  - **Derived** attributes
    - Can be computed from other attributes
    - Example: age, given *date\_of\_birth*
- **Domain** – the set of permitted values for each attribute

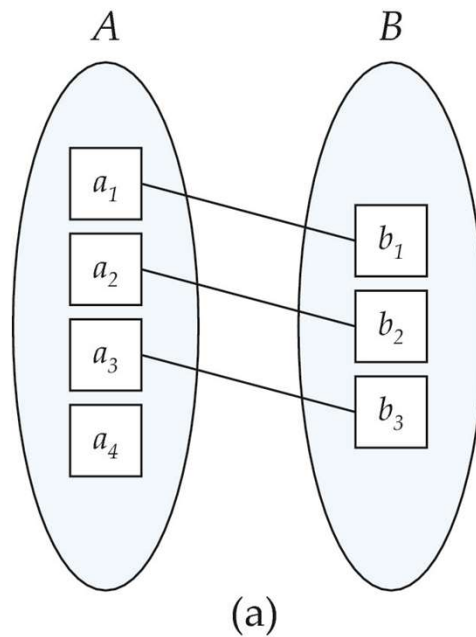
<i>instructor</i>
<u><i>ID</i></u>
<i>name</i>
<i>first_name</i>
<i>middle_initial</i>
<i>last_name</i>
<i>address</i>
<i>street</i>
<i>street_number</i>
<i>street_name</i>
<i>apt_number</i>
<i>city</i>
<i>state</i>
<i>zip</i>
{ <i>phone_number</i> }
<i>date_of_birth</i>
<i>age</i> ( )



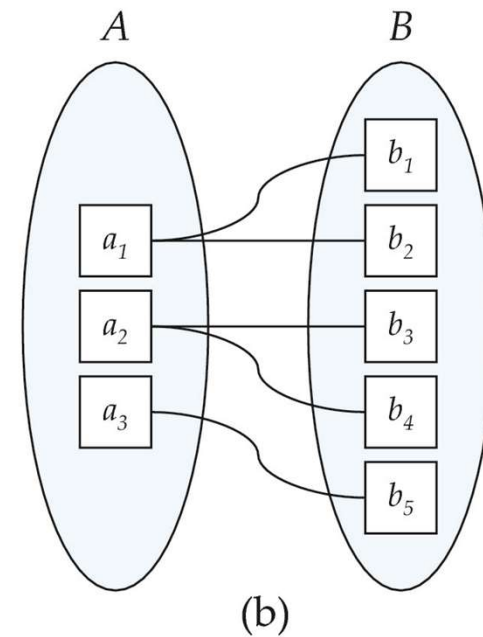
# Mapping Cardinalities

- Express the number of entities to which another entity can be associated via a relationship set
- **One to one**
  - An entity in A is associated with at most one entity in B, An entity in B is associated with at most one entity in A
- **One to many**
  - An entity in A is associated with any number (0 or more) of entities in B, An entity in B is associated with at most one entity in A
- **Many to one**
  - An entity in A is associated with at most one entity in B, An entity in B is associated with any number (0 or more) of entities in A
- **Many to many**
  - An entity in A is associated with any number (0 or more) of entities in B, An entity in B is associated with any number (0 or more) of entities in A

## Mapping Cardinalities

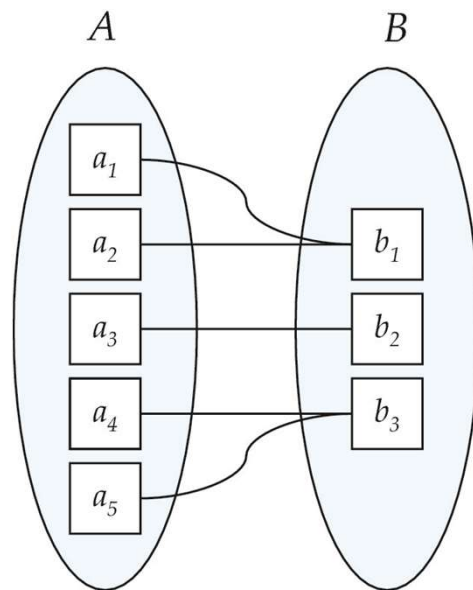


One to one



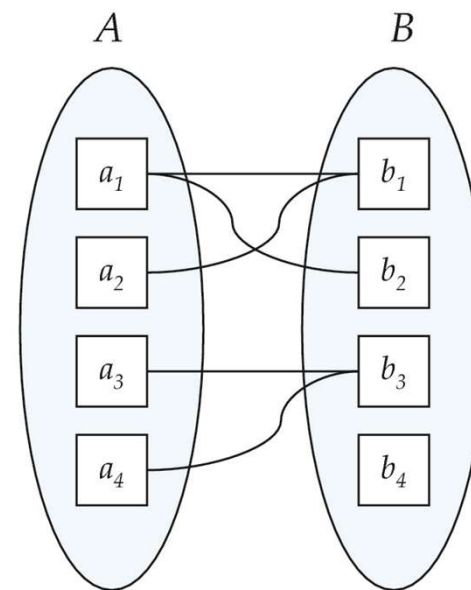
One to many

## Mapping Cardinalities



(a)

Many to one



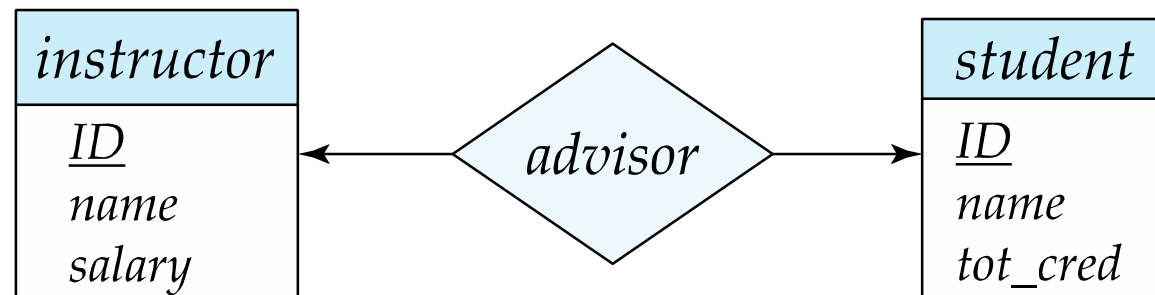
(b)

Many to many



# Cardinality Constraints-ER Diagram

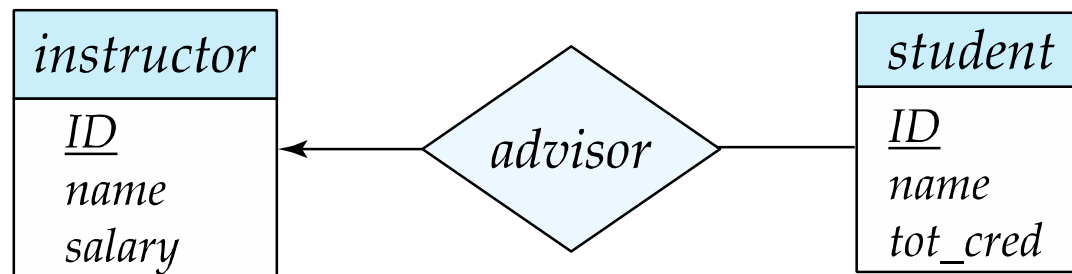
- We express cardinality constraints by drawing either a directed line (→), signifying “one,” or an undirected line (—), signifying “many,” between the relationship set and the entity set



One to one

# Cardinality Constraints-ER Diagram

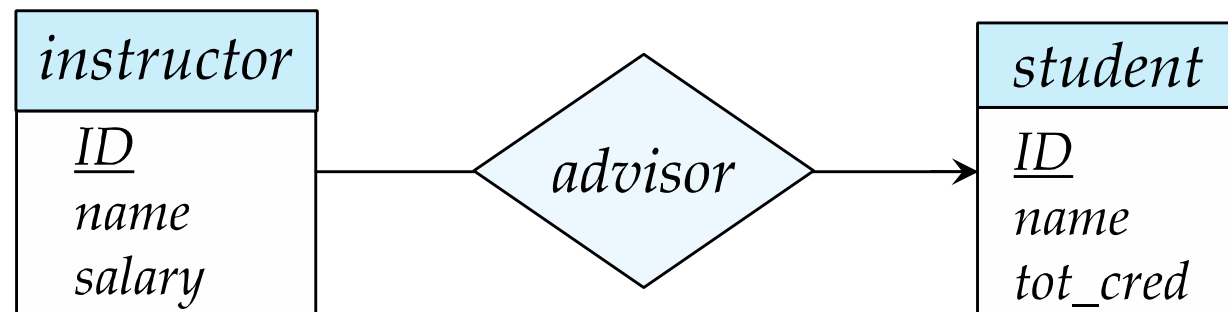
- We express cardinality constraints by drawing either a directed line (⤵), signifying “one,” or an undirected line (—), signifying “many,” between the relationship set and the entity set



One to many

# Cardinality Constraints-ER Diagram

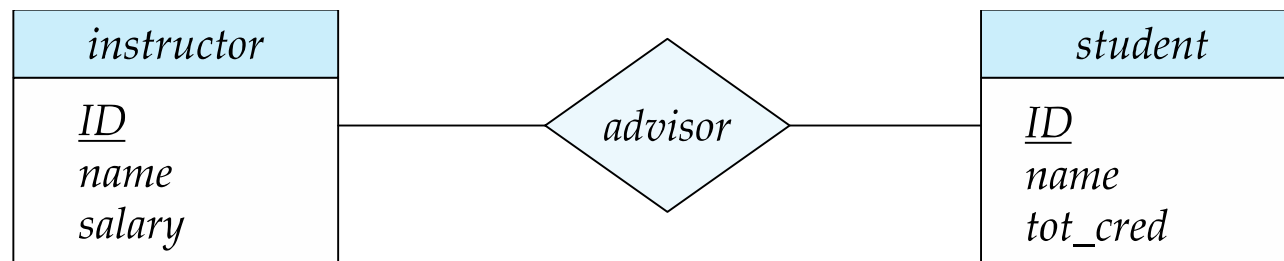
- We express cardinality constraints by drawing either a directed line (→), signifying “one,” or an undirected line (—), signifying “many,” between the relationship set and the entity set



Many to one

# Cardinality Constraints-ER Diagram

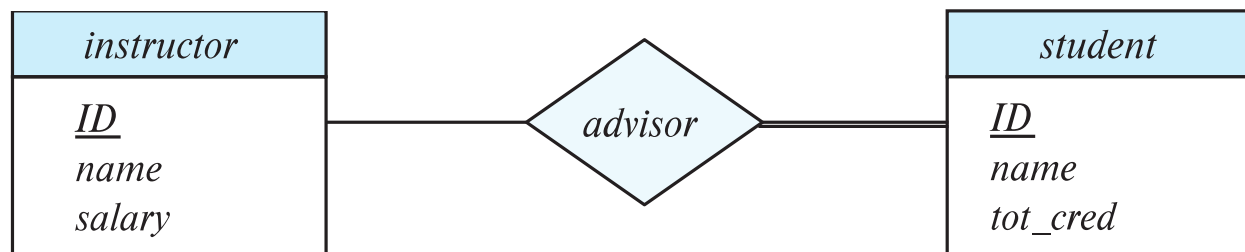
- We express cardinality constraints by drawing either a directed line (⌞), signifying “one,” or an undirected line (—), signifying “many,” between the relationship set and the entity set



Many to many

# Cardinality Constraints-ER Diagram

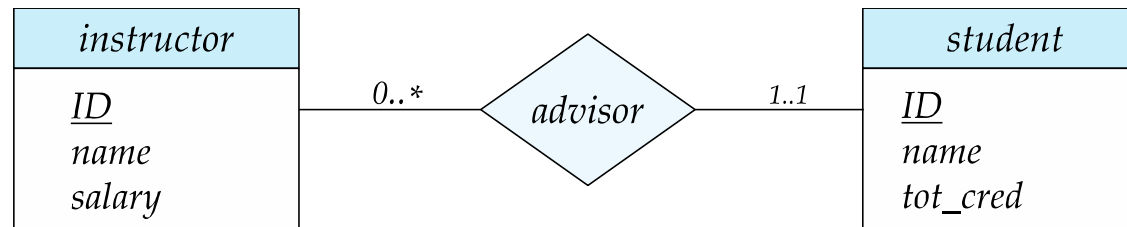
- **Total participation** (indicated by double line): every entity in the entity set participates in at least one relationship in the relationship set
  - Example: participation of student in advisor relation is total, every student must have an associated instructor



- **Partial participation**: some entities may not participate in any relationship in the relationship set
  - Example: participation of instructor in advisor is partial

# Cardinality Constraints-ER Diagram

- A line may have an associated minimum and maximum cardinality, shown in the form l..h, where l is the minimum and h the maximum cardinality
  - A minimum value of 1 indicates total participation
  - A maximum value of 1 indicates that the entity participates in at most one relationship
  - A maximum value of \* indicates no limit



**Instructor can advise 0 or more students**  
**A student must have 1 advisor; cannot have multiple advisors**

# Cardinality Constraints-ER Diagram



- We allow at most one arrow out of a ternary (or greater degree) relationship to indicate a cardinality constraint
  - For example, an arrow from proj\_guide to instructor indicates each student has at most one guide for a project
- If there is more than one arrow, there are two ways of defining the meaning.
  - For example, a ternary relationship R between A, B and C with arrows to B and C could mean
    1. Each A entity is associated with a unique entity from B and C
    2. Each pair of entities from (A, B) is associated with a unique C entity, and each pair (A, C) is associated with a unique B



# Primary Key for Entity Sets

- By definition, individual entities are distinct.
- From database perspective, the differences among them must be expressed in terms of their attributes.
- The values of the attribute values of an entity must be such that they can uniquely identify the entity.
  - No two entities in an entity set are allowed to have exactly the same value for all attributes.
- A **key** for an entity is a set of attributes that suffice to distinguish entities from each other



## Keys



- Let  $K$  is a subset of attributes
- $K$  is a superkey if values for  $K$  are sufficient to identify a unique tuple of each possible relation  $r(R)$ 
  - Example:  $\{ID\}$  and  $\{ID, name\}$  are both superkeys of instructor
- Superkey  $K$  is a candidate key if  $K$  is minimal
  - Example:  $\{ID\}$  is a candidate key for Instructor
- One of the candidate keys is selected to be the primary key

# Primary Key for Relationship Sets

- To distinguish among the various relationships of a relationship set we use the individual primary keys of the entities in the relationship set
- Let  $R$  be a relationship set involving entity sets  $E_1, E_2, \dots, E_n$
- The primary key for  $R$  consists of the union of the primary keys of entity sets  $E_1, E_2, \dots, E_n$ 
  - If the relationship set  $R$  has attributes  $a_1, a_2, \dots, a_m$  associated with it, then the primary key of  $R$  and attributes  $a_1, a_2, \dots, a_m$  describe the relationship in set  $R$
- Example: relationship set “advisor”
  - The primary key consists of instructor.ID and student.ID

# Primary Key for Relationship Sets

- The choice of the primary key for a relationship set depends on the mapping cardinality of the relationship set
- Many-to-Many relationships
  - The preceding union of the primary keys is a minimal superkey and is chosen as the primary key
- One-to-Many relationships
  - The primary key of the “Many” side is a minimal superkey and is used as the primary key
- Many-to-one relationships
  - The primary key of the “Many” side is a minimal superkey and is used as the primary key
- One-to-one relationships
  - The primary key of either one of the participating entity sets forms a minimal superkey, and either one can be chosen as the primary key

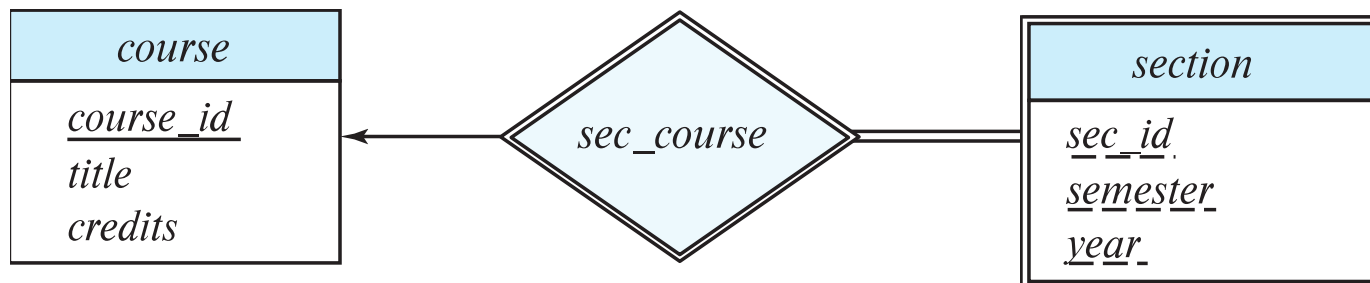
# Weak/Strong Entity Sets



- A **weak entity set** is one whose existence is dependent on another entity, called its **identifying entity**
- Instead of associating a primary key with a weak entity, we use the primary key of identifying entity, along with extra attributes called **discriminator** to uniquely identify a weak entity
- The identifying entity set is said to **own** the weak entity set that it identifies
- The relationship associating the weak entity set with the identifying entity set is called the **identifying relationship**
- An entity set that is not a weak entity set is termed a **strong entity set**.

# Weak Entity Sets-ER Diagram

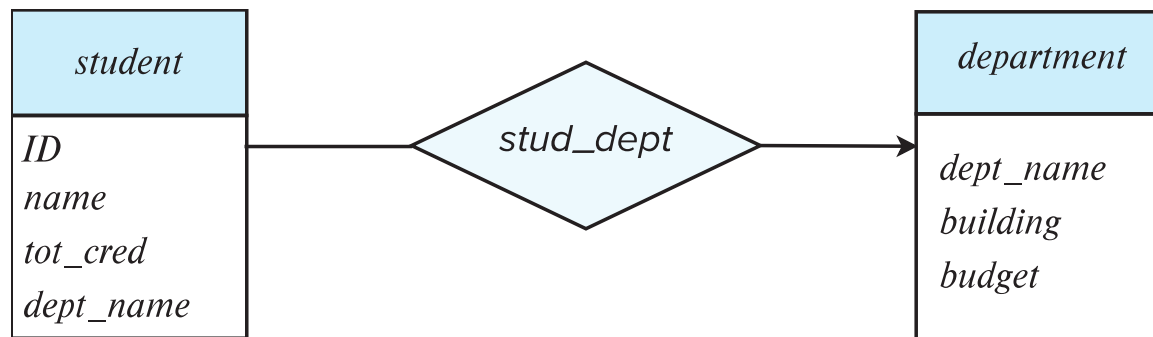
- In E-R diagrams, a weak entity set is depicted via a double rectangle.
- We underline the discriminator of a weak entity set with a dashed line.
- The relationship set connecting the weak entity set to the identifying strong entity set is depicted by a double diamond.
- Primary key for section – (course\_id, sec\_id, semester, year)



## Redundant Attributes



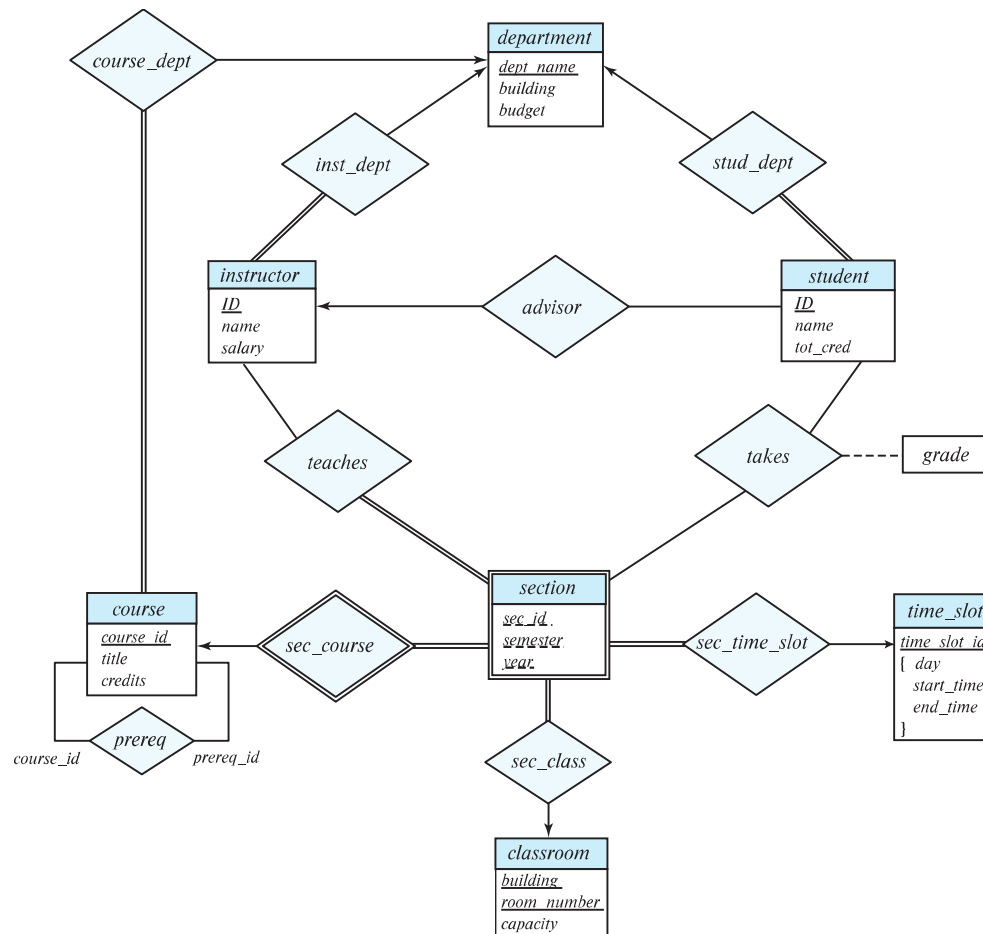
- We model the fact that each student has an associated department using a relationship set *stud\_dept*
- The attribute *dept\_name* in *student* below replicates information present in the relationship and is therefore redundant and needs to be removed.
- BUT: when converting back to tables, in some cases the attribute gets reintroduced, as we will see later



(a) Incorrect use of attribute

# ER Model

## ER Diagram of University





# Reduction to Relation Schemas

- Entity sets and relationship sets can be expressed uniformly as *relation schemas* that represent the contents of the database
- A database which conforms to an E-R diagram can be represented by a collection of schemas
- For each entity set and relationship set there is a unique schema that is assigned the name of the corresponding entity set or relationship set
- Each schema has a number of columns (generally corresponding to attributes), which have unique names





# Representing Entity Sets

- A strong entity set reduces to a schema with the same attributes

*student(ID, name, tot\_cred)*

- A weak entity set becomes a table that includes a column for the primary key of the identifying strong entity set

*section ( course id, sec id, sem, year )*

# ER Model to Relation Schema



## Composite Attributes

- Composite attributes are flattened out by creating a separate attribute for each component attribute
- Ignoring multivalued attributes, extended instructor schema is
  - instructor(ID, first\_name, middle\_initial, last\_name, street\_number, street\_name, apt\_number, city, state, zip\_code, date\_of\_birth)

<i>instructor</i>
<u>ID</u>
<i>name</i>
<i>first_name</i>
<i>middle_initial</i>
<i>last_name</i>
<i>address</i>
<i>street</i>
<i>street_number</i>
<i>street_name</i>
<i>apt_number</i>
<i>city</i>
<i>state</i>
<i>zip</i>
{ <i>phone_number</i> }
<i>date_of_birth</i>
<i>age</i> ( )



# Multivalued Attributes

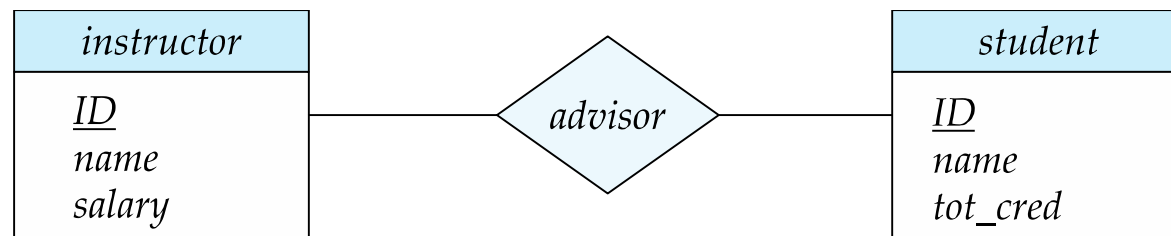
- A multivalued attribute M of an entity E is represented by a separate schema EM
- Schema EM has attributes corresponding to the primary key of E and an attribute corresponding to multivalued attribute M
  - Example: Multivalued attribute phone\_number of instructor is represented by a schema:  
inst\_phone= ( ID, phone\_number)
- Each value of the multivalued attribute maps to a separate tuple of the relation on schema EM
  - For example, an instructor entity with primary key 22222 and phone numbers 456-7890 and 123-4567 maps to two tuples:  
(22222, 456-7890) and (22222, 123-4567)

## ER Model to Relation Schema

# Reduction to Relation Schemas

- A many-to-many relationship set is represented as a schema with attributes for the primary keys of the two participating entity sets, and any descriptive attributes of the relationship set
- Example: schema for relationship set *advisor*

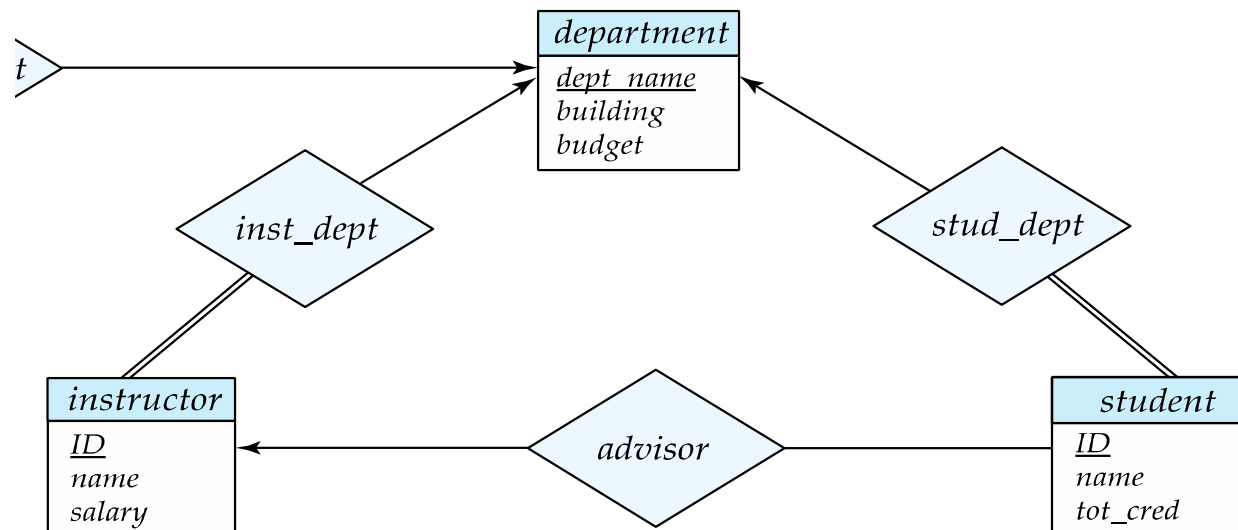
*advisor* = (*s id*, *i id*)



# ER Model to Relation Schema

## Reduction to Relation Schemas

- Many-to-one and one-to-many relationship sets that are total on the many-side can be represented by adding an extra attribute to the “many” side, containing the primary key of the “one” side
- Example: Instead of creating a schema for relationship set *inst\_dept*, add an attribute *dept\_name* to the schema arising from entity set *instructor*





# Reduction to Relation Schemas

- For one-to-one relationship sets, either side can be chosen to act as the “many” side
- That is, an extra attribute can be added to either of the tables corresponding to the two entity sets
- If participation is partial on the “many” side, replacing a schema by an extra attribute in the schema corresponding to the “many” side could result in null values

# Reduction to Relation Schemas



- For one-to-one relationship sets, either side can be chosen to act as the primary key. The schema corresponding to a relationship set linking a weak entity set to its identifying strong entity set is redundant.
- Example: The section schema already contains the attributes that would appear in the sec\_course schema

# Binary Vs. Non-Binary Relationships

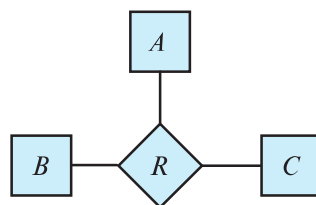
- Although it is possible to replace any non-binary ( $n$ -ary, for  $n > 2$ ) relationship set by a number of distinct binary relationship sets, a  $n$ -ary relationship set shows more clearly that several entities participate in a single relationship.
- Some relationships that appear to be non-binary may be better represented using binary relationships
  - For example, a ternary relationship *parents*, relating a child to his/her father and mother, is best replaced by two binary relationships, *father* and *mother*
    - Using two binary relationships allows partial information (e.g., only mother being known)
  - But there are some relationships that are naturally non-binary
    - Example: *proj\_guide*



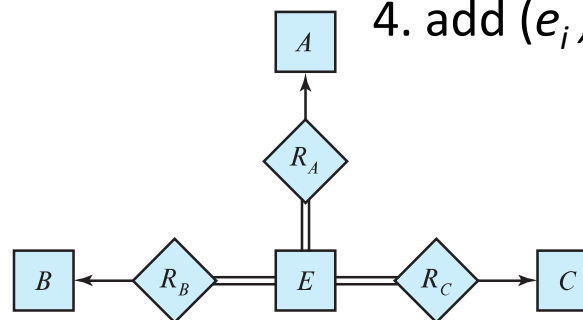
# ER Model to Relation Schema

## Binary Vs. Non-Binary Relationships

- In general, any non-binary relationship can be represented using binary relationships by creating an artificial entity set
  - Replace  $R$  between entity sets  $A$ ,  $B$  and  $C$  by an entity set  $E$ , and three relationship sets:
    1.  $R_A$ , relating  $E$  and  $A$
    2.  $R_B$ , relating  $E$  and  $B$
    3.  $R_C$ , relating  $E$  and  $C$
  - Create an identifying attribute for  $E$  and add any attributes of  $R$  to  $E$
  - For each relationship  $(a_i, b_i, c_i)$  in  $R$ , create
    1. a new entity  $e_i$  in the entity set  $E$
    2. add  $(e_i, a_i)$  to  $R_A$
    3. add  $(e_i, b_i)$  to  $R_B$
    4. add  $(e_i, c_i)$  to  $R_C$



(a)



(b)

## *ER Model to Relation Schema*

# Binary Vs. Non-Binary Relationships

- Contracts(Supplier, Part, Project)
- A supplier supplies a particular part to a particular project

Supplier	Part	Project
S1	P1	J1
S1	P2	J2
S2	P1	J1

- SUPPLIER — supplies — CONTRACT
- PART — provides — CONTRACT
- PROJECT — used\_for — CONTRACT

## *ER Model to Relation Schema*

# Binary Vs. Non-Binary Relationships

- CONTRACT Table

ContractID

C1

C2

C3

## *ER Model to Relation Schema*

# Binary Vs. Non-Binary Relationships

- SUPPLIER–CONTRACT relationship

Supplier

S1

S1

S2

ContractID

C1

C2

C3

## *ER Model to Relation Schema*

# Binary Vs. Non-Binary Relationships

- PART–CONTRACT relationship

Part	ContractID
P1	C1
P2	C2
P1	C3

## *ER Model to Relation Schema*

# Binary Vs. Non-Binary Relationships

- PROJECT–CONTRACT relationship

Project

J1

J2

J1

ContractID

C1

C2

C3



## Acknowledgement

- Some slides and figures are collected from
  - <https://www.db-book.com/>