

In[1]:= $\int_0^{+\infty} x^k * E^{-a*x^2-b*x} \, dx$

$\int_0^{+\infty} x^k * E^{-a*x^2-b*x} \, dx - \text{Gamma}[k + 1] * E^{\frac{b^2}{8*a}} * (2 * a)^{-\frac{k + 1}{2}} * \text{ParabolicCylinderD}[-k - 1, \frac{b}{\sqrt{2 * a}}] // \text{FullSimplify}$

Out[1]= $\frac{1}{2} a^{-1-\frac{k}{2}} \left(-b \, \text{Gamma}\left[1 + \frac{k}{2}\right] \text{Hypergeometric1F1}\left[1 + \frac{k}{2}, \frac{3}{2}, \frac{b^2}{4 a}\right] + \sqrt{a} \, \text{Gamma}\left[\frac{1+k}{2}\right] \text{Hypergeometric1F1}\left[\frac{1+k}{2}, \frac{1}{2}, \frac{b^2}{4 a}\right] \right)$
 if Re[a] > 0 && Re[k] > -1

Out[2]= $0 \text{ if } \text{Re}[a] > 0 \text{ \&\& } \text{Re}[k] > -1$