Submission Guidelines:

- Problem 1: Submit only the **PowersUsername.java** file on Canvas, by substituting the Username with your NKU username.
- Problem 2: Submit only the **PlayerSorter.java** file on Canvas.

Problem 1: Computing Powers

This problem is a case study in using recursive thinking to improve the efficiency of an iterative algorithm. You will write a sequence of methods for the exponentiation of floating point numbers. Parts I and II involve writing rather simple-minded iterative and recursive methods for the task. In Parts III and IV you use more sophisticated recurrence relations in order to write more efficient recursive methods. In Part V you convert your method from Part IV into an iterative method that is far more efficient than the Part I iterative method.

Put all of your code for this project into a **single class file – PowersUsername.java**, by substituting the Username with your NKU username. All of your methods should be **static**.

Part I

Write an iterative method called *power1* to compute b^n , where b is of type double and n is an integer ≥ 0 . Use a simple for-loop that repeatedly (n times) multiplies an accumulator variable by b.

Part II:

Write a recursive method *power2* that accomplishes the same task as *power1*, but is based on the following recurrence relation:

$$b^0 = 1$$

 $b^n = b * b^{n-1}$ if $n > 0$

Part III:

Write a recursive method *power3* that is identical to *power2* except that it is based on this recurrence relation

```
\begin{array}{ll} b^0=1 \\ b^n=(b^{n/2})^2 & \text{if } n>0 \text{ and } n \text{ is even} \\ b^n=b^*(b^{n/2})^2 & \text{if } n>0 \text{ and } n \text{ is odd (Note: This equation is not true in math. Why is it true in Java?)} \end{array}
```

Note: If n is a large exponent, then *power3* should perform far fewer multiplications than *power2*. In particular, when computing something like $(b^{n/2})^2$, there is no need to compute $b^{n/2}$ twice. Rather, compute it once, store it in a variable, and then compute the result of multiplying the variable by itself.

Part IV:

Write a <u>tail recursive</u> helper method called *multPow*, that computes the value of $a*b^n$. Base your implementation on the following recurrence relation:

```
a*b^0 = a

a*b^n = a*(b^2)^{n/2} if n > 0 and n is even
```

```
a*b^n = (a*b)*(b^2)^{n/2} if n > 0 and n is odd
```

Then write a method called *power4* that computes b^n simply by making the call multPow(1, b, n). Note that in this approach, the extra parameter a used by the helper method is serving as an accumulator for the result.

Part V:

Write an iterative method *power5* to compute b^n . Write it in such a way that the number of multiplications performed by *power5* is no more than the number performed by *power4*. (Hint: Base your solution to Part V on your solution to Part IV. Declare a as a local variable that is initialized to 1 and that eventually accumulates the result of the calculation.) Note that, in general, *power5* requires far fewer multiplications than *power1*.

Main method:

Write a main method to test your methods from Parts I - V. It should ask the user for b and n, then compute and display the results. Call the Math.pow method in order to check your results. Display the results from Math.pow first. Then display the results from your methods. Also display the number of multiplications performed by each of your methods. In order to count the number of multiplications, you may use a "global variable" that is modified by the power methods as a side-effect, as demonstrated below:

```
public class Powers
      private static int multiplications; // "global variable" for counting the
                                            //
                                                  number of
                                                                   multiplications
                                            performed // by each method
      public static void main(String[] args)
             multiplications = 0;
             System.out.println("\npower1(" + base + ", " + n + ") = " + power1(base,
             System.out.println("Multiplications = " + multiplications);
             multiplications = 0;
             . . .
      }
      public static double power1(double base, int n)
      // Returns base to the n-th power.
      // Iterative method.
             . . .
             for (...)
                    multiplications++;
                    result *= base;
             }
             return result;
      }
      . . .
}
```

Note: It is a good idea to test code as you develop it. It is recommended that you write the main method code that tests Part I as soon as (or even before) Part I is finished.

Sample session with a completed program:

Enter a decimal number: 1.001

Enter a non-negative integer exponent: 1000

Computing 1.001 to the power 1000:

Math.pow(1.001, 1000) = 2.7169239322355936

power1(1.001, 1000) = 2.7169239322355985

Multiplications = 1000

power2(1.001, 1000) = 2.7169239322355985

Multiplications = 1000

power3(1.001, 1000) = 2.716923932235485

Multiplications = 16

power4(1.001, 1000) = 2.7169239322355203

Multiplications = 16

power5(1.001, 1000) = 2.7169239322355203

Multiplications = 16

Note:

In Parts I-V, your code should **not** call any methods from java.lang.Math. For example, in those methods, if you need to compute b^2 , do not write Math.pow(b, 2). Instead, write b * b, and count the multiplication.

Problem 2: Priority queue using multiple comparators

In this program, we will use an input file containing the names of players and their points, and then sort the list of players in two ways: (a) based on the length of their names, and (b) their scores. Follow the descriptions below to develop your program:

- Input file: *players.txt*
 - o Input format in file: FirstName LastName Score
- Create a file *PlayerSorter.java*. The file will have 4 classes:
 - o PlayerSorter, Player, NameLengthComparator, ScoreCompartor

- public class PlayerSorter

- This class will contain the *main()* method, and will perform the following actions:
 - Read the inputs from the *players.txt* file. You must reach the input file with using the try-with-resources format, and catch the *FileNotFoundException*. Save the inputs as *Player* instances in *ArrayList<Player> players*.
 - Create a priority queue *playerNameLenPQ* with the comparator *NameLengthComparator* and add all the players stored in the arraylist *players*.
 - Create another priority queue *playerScorePQ* with the comparator *ScoreComparator* and add all the players stored in the arraylist *players*.
 - Use the *removeAndPrintQueue()* method to print out the details of the *Player* instances stored in *playerNameLenPQ*.
 - Use the *removeAndPrintQueue()* method to print out the details of the *Player* instances stored in *playerScorePQ*.
- Write a method *removeAndPrintQueue(PriorityQueue<Player> pq)* to remove and print out the instances of *Player* stored in the priority queue one by one, in this format:
 - FirstName <single space> LastName <tab space> Score

- class Player

- o Data variables: String fName, String lName, and Double score.
- Public constructor
 - public Player(String fName, String lName, Double score)

class NameLengthComparator implements java.util.Comparator<Player>

- Override compare method
- O Compare length of (first-name + last-name) and return -1/0/+1 accordingly.

class ScoreComparator implements java.util.Comparator<Player>

- Override compare method.
- O Compare score and return -1/0/+1 accordingly.

The standard implementation description for the *compare()* method is as follows: *Returns a negative* value if element1 is less than element2, a positive value if element1 is greater than/ element2, and zero if they are equal.

 ${\bf Submission:}\ \ {\bf Submit\ the\ PlayerSorter.java\ file\ on\ Canvas.}$

Sample input file: players.txt (included)

Sample output:

Name c	omparato	r
John Drew	20.69	
Bob Pettit	26.36	
Larry Bird	24.29	
Bob McAdoo	22.05	
Jerry West	27.03	
Rick Barry	23.17	
Dwyane Wade	21.98	
Elvin Hayes	20.96	
Karl Malone	25.02	
Kobe Bryant	24.99	
Paul Arizin	22.81	
Elgin Baylor	27.36	
Geoff Petrie	21.82	
Alex English	21.47	
Bradley Beal LeBron James	20.96	
	27.07	
James Harden	25.16	
Chris Webber	20.68	
George Mikan	23.13	
Kevin Durant	27.02	
Bernard King	22.49	
Kyrie Irving	22.43	
Julius Erving	21.97	
Pete Maravich	24.24	
Blake Griffin	21.67	
George Gervin	26.18	
Anthony Davis	24.01	
Patrick Ewing	20.98	
Stephen Curry	23.49	
Dirk Nowitzki	20.74	
John Havlicek	20.78	
Allen Iverson	26.66	
Glenn Robinson	20.69	
Michael Jordan	30.12	
Adrian Dantley	24.27	
David Robinson	21.06	
Damian Lillard	24.21	
Mitch Richmond	21.0	
David Thompson	22.13	
Carmelo Anthony		
Oscar Robertson		
Hakeem Olajuwon		
Charles Barkley		22.60
Shaquille O'Neal		23.69
DeMarcus Cousins		21.25
Wilt Chamberlain		30.07
Billy Cunningham		20.83
Dominique Wilkin		24.83
Russell Westbroo		23.25
Kareem Abdul-Jab		24.61
	Comparat	01
Chris Webber	20.68	
Glenn Robinson	20.69	
John Drew	20.69	
Dirk Nowitzki	20.74	
John Havlicek	20.78	20.02
Billy Cunningham		20.83
Elvin Hayes	20.96	
Bradley Beal	20.96	
Patrick Ewing	20.98	

Mitch Richmond David Robinson	21.0 21.06	
DeMarcus Cousins		21.25
Alex English	21.47	21.23
Blake Griffin	21.67	
Hakeem Olajuwon	21.77	
Geoff Petrie	21.77	
Julius Erving	21.82	
Dwyane Wade	21.98	
Bob McAdoo	22.05	
David Thompson	22.13	
Charles Barkley	22.14	
Kyrie Irving	22.43	
Bernard King	22.49	
Paul Arizin	22.81	
George Mikan	23.13	
Rick Barry	23.17	
Russell Westbroo		23.25
Stephen Curry	23.49	
Carmelo Anthony	23.57	
Shaquille O'Neal	L	23.69
A () B '		
Anthony Davis	24.01	
Damian Lillard	24.01	
Damian Lillard	24.21	
Damian Lillard Pete Maravich	24.21 24.24	
Damian Lillard Pete Maravich Adrian Dantley	24.21 24.24 24.27 24.29	24.61
Damian Lillard Pete Maravich Adrian Dantley Larry Bird	24.21 24.24 24.27 24.29 bbar	24.61 24.83
Damian Lillard Pete Maravich Adrian Dantley Larry Bird Kareem Abdul-Jab	24.21 24.24 24.27 24.29 bbar	
Damian Lillard Pete Maravich Adrian Dantley Larry Bird Kareem Abdul-Jab Dominique Wilkir	24.21 24.24 24.27 24.29 obar	
Damian Lillard Pete Maravich Adrian Dantley Larry Bird Kareem Abdul-Jab Dominique Wilkir Kobe Bryant	24.21 24.24 24.27 24.29 obar ns 24.99	
Damian Lillard Pete Maravich Adrian Dantley Larry Bird Kareem Abdul-Jab Dominique Wilkir Kobe Bryant Karl Malone	24.21 24.24 24.27 24.29 bbar as 24.99 25.02 25.16	
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