

Tutorial 4

Counters

Exercise 1

- For the circuit shown in [Figure 1](#), complete the timing diagram below.

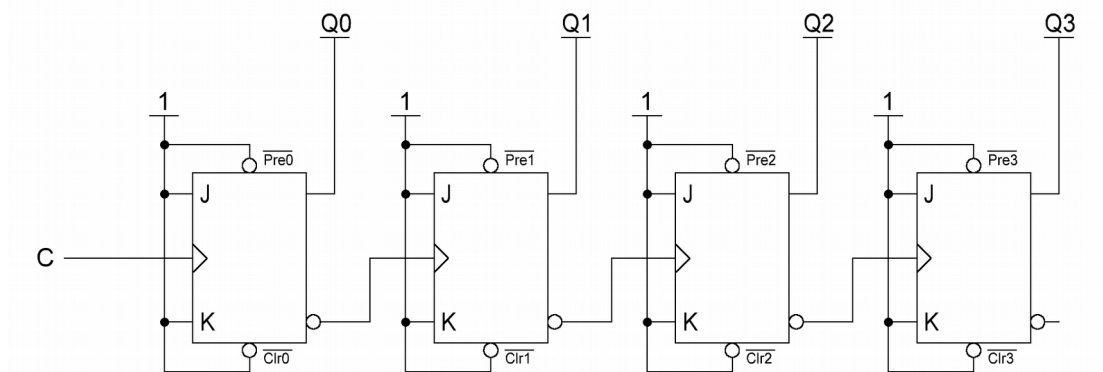
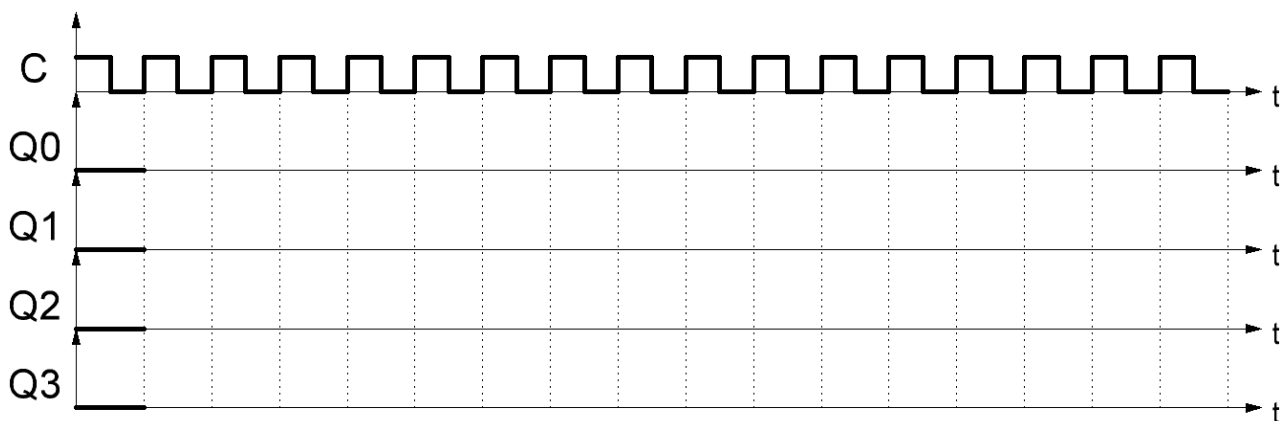


Figure 1



- What does the circuit shown in [Figure 1](#) do?

3. Slight changes are made to the circuit shown in [Figure 1](#) in order to obtain the circuit shown in [Figure 2](#). What does this new circuit do? Explain your line of reasoning.

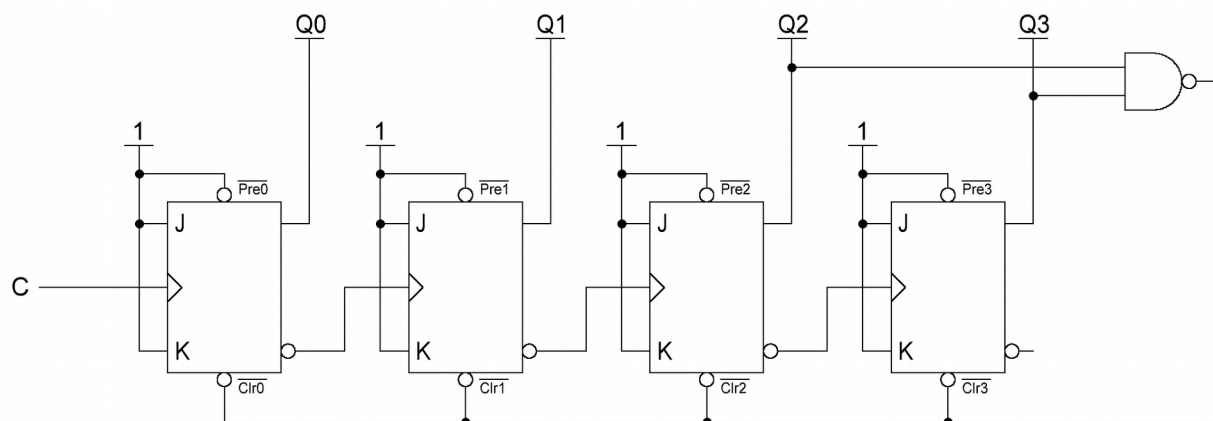


Figure 2

4. For the circuit shown in [Figure 3](#), complete the timing diagram below.

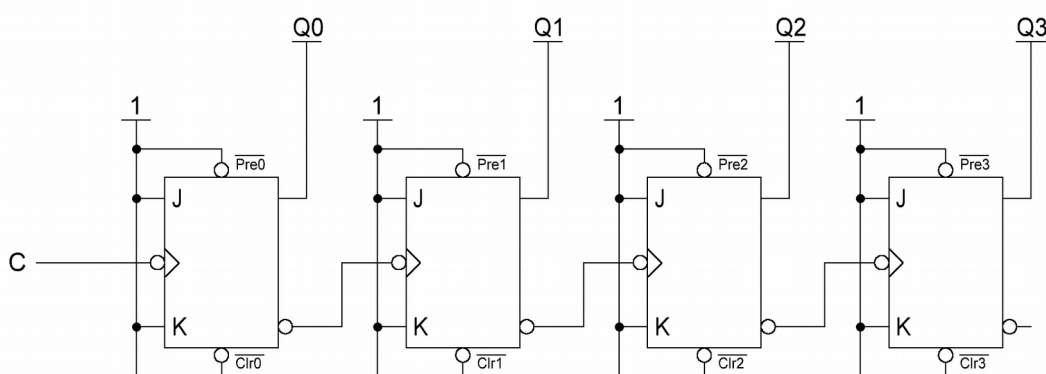
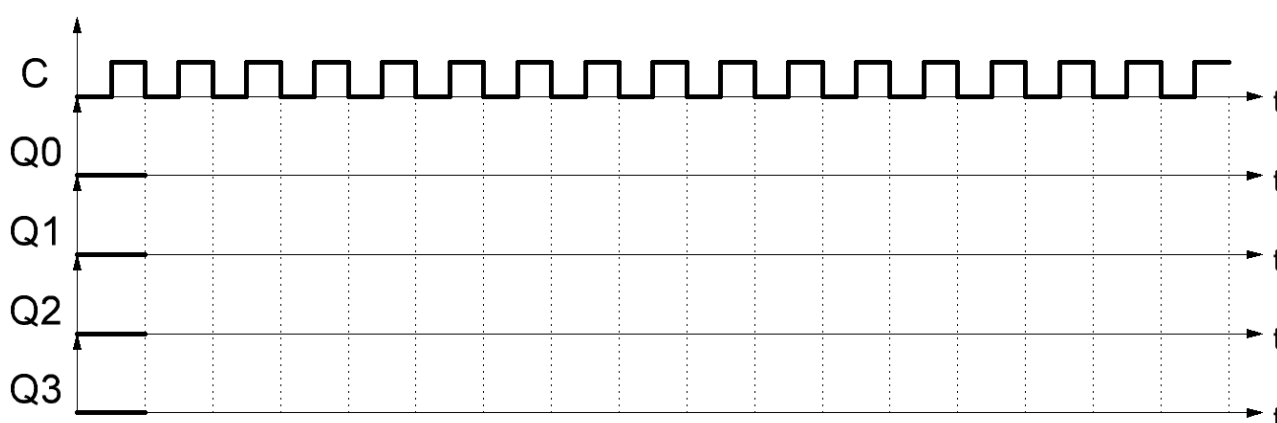


Figure 3



5. What does the circuit shown in [Figure 3](#) do?

6. Slight changes are made to the circuit shown in [Figure 3](#) in order to obtain the circuit shown in [Figure 4](#). What does this new circuit do? Explain your line of reasoning.

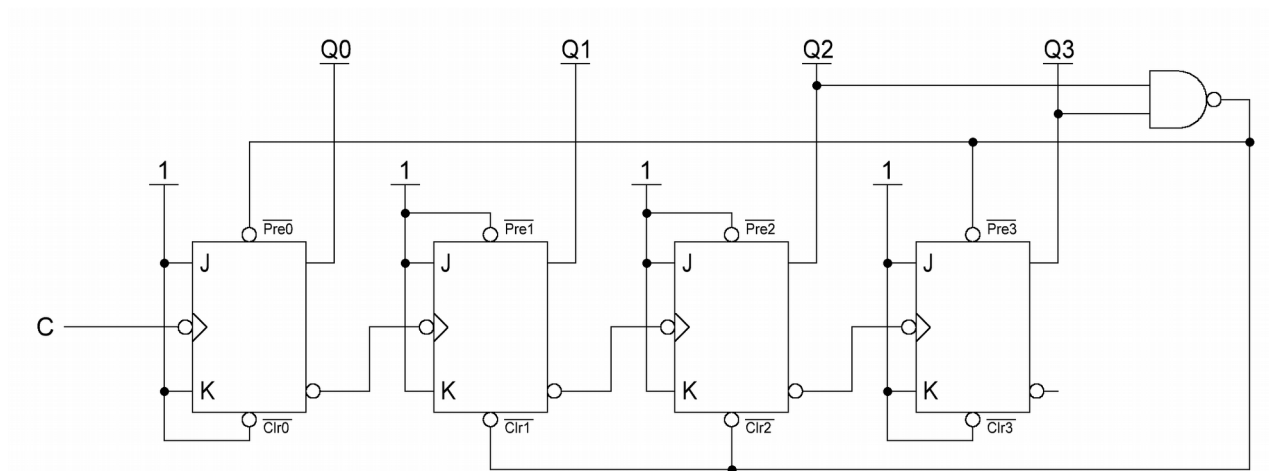
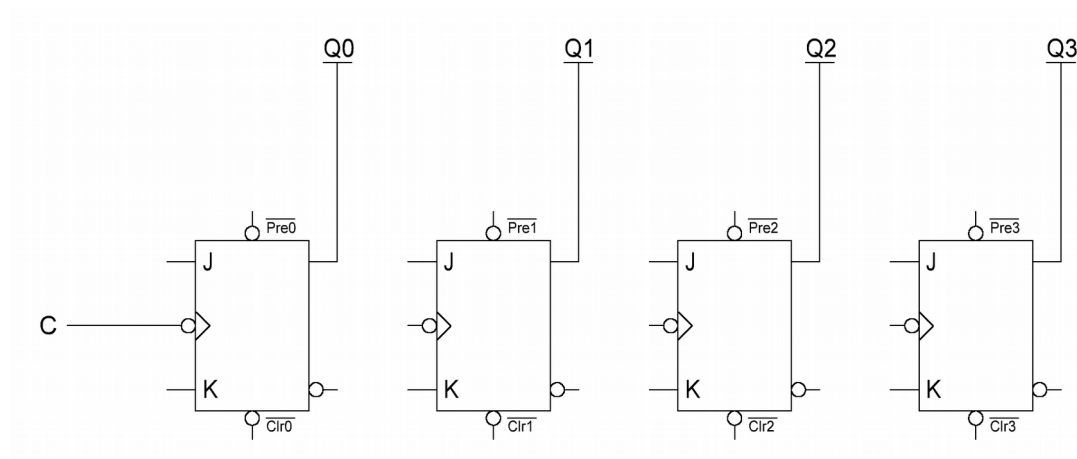
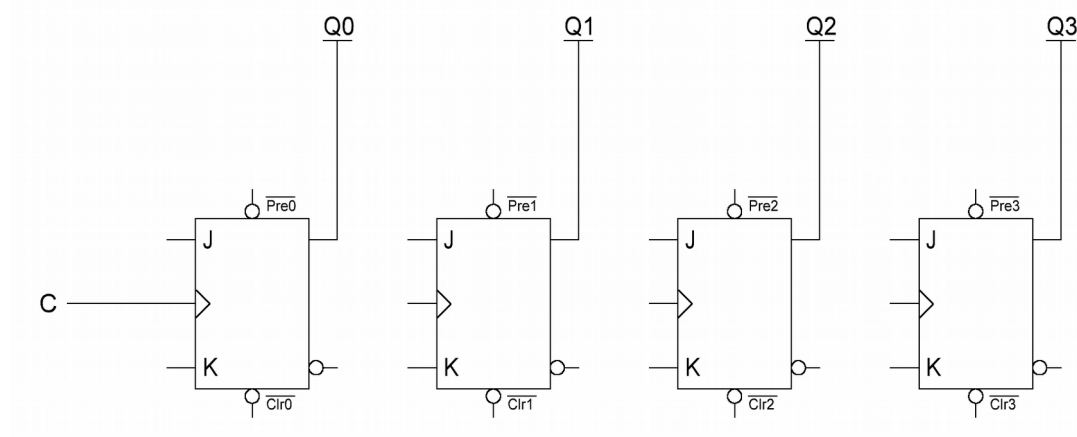


Figure 4

7. Wire the following flip-flops in order to design a modulo-10 asynchronous up counter.



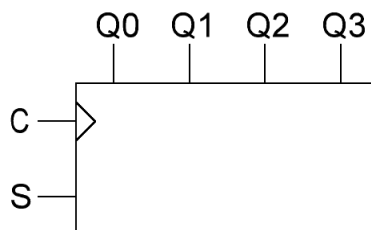
8. Wire the following flip-flops in order to design a modulo-13 asynchronous down counter.



Exercise 2

We want to design a modulo-16 up/down counter. That is to say, a circuit that has two different modes: an up-count mode and a down-count mode. The mode can be set with an S input:

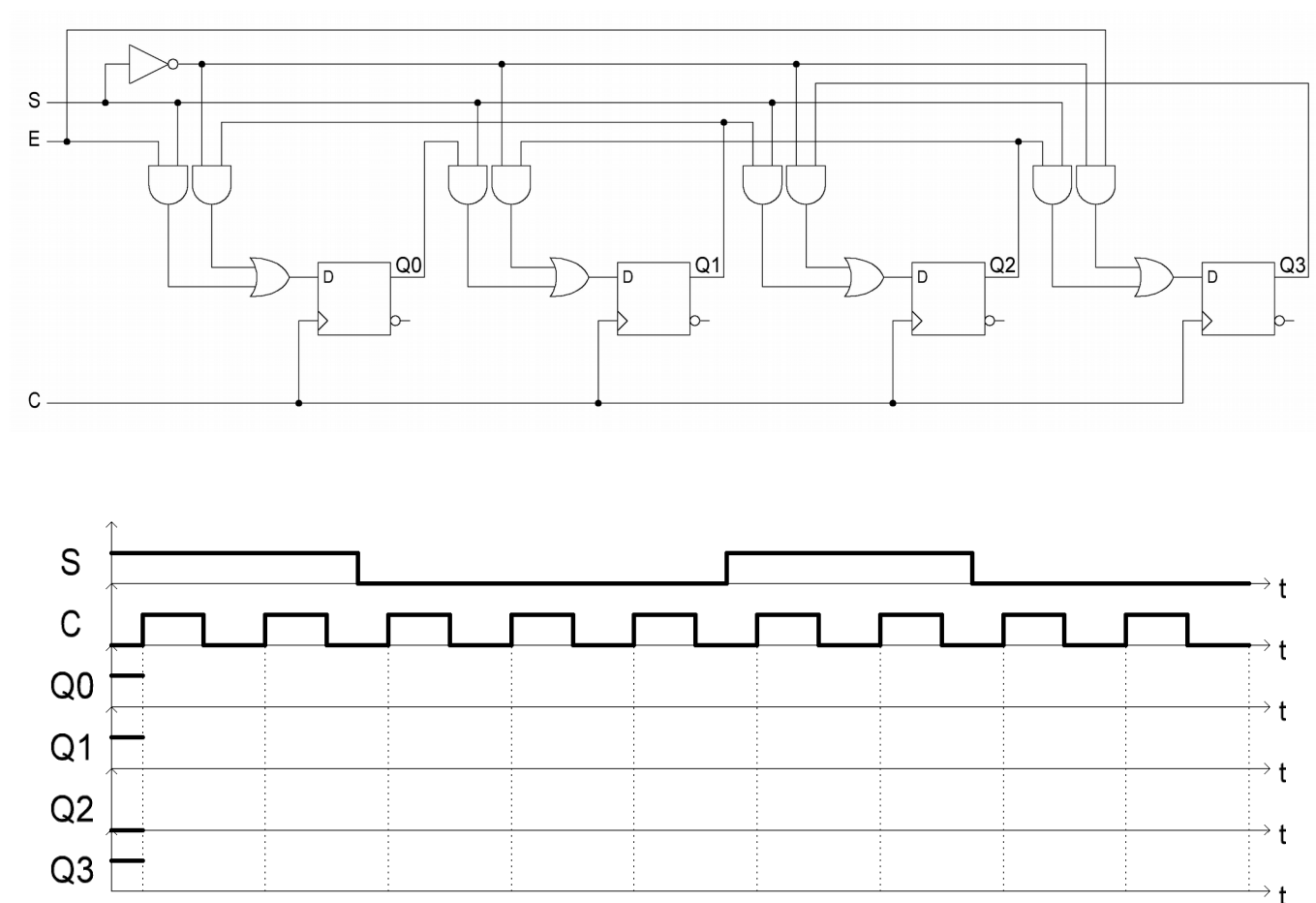
- $S = 0 \rightarrow$ up-count mode.
- $S = 1 \rightarrow$ down-count mode.



Draw the circuit diagram of the modulo-16 up/down counter. Use only positive-edge-triggered JK flip-flops and logic gates.

Exercise 3

Complete the timing diagram for the circuit below ($E = 0$).



Exercise 4

To begin with, you must design a modulo-7 synchronous counter using positive-edge-triggered JK flip-flops.

- Using the excitation table of a JK flip-flop, complete the table below.

Q2	Q1	Q0	J2	K2	J1	K1	J0	K0

- Obtain the most simplified expressions for $J0$, $K0$, $J1$, $K1$, $J2$ and $K2$.
- Draw the circuit diagram of the counter.

Lastly, you have to design a 3-bit synchronous Gray counter using negative-edge-triggered JK flip-flops.

- Complete the table below.

Q2	Q1	Q0	J2	K2	J1	K1	J0	K0

- Obtain the most simplified expressions for $J0$, $K0$, $J1$, $K1$, $J2$ and $K2$.