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11)

1) We will traverse the binary tree with Breadth-first search. We will push in the queue not just the nodes, but pairs of numbers - the node and the level. The first in the queue will be (root, 0). Whenever we push in the queue the children of the front of the queue its level will be the level of the front of the queue + 1. Also, each time we pop something from the queue we increment the position of the level in a direct table (we use direct table since the height of binary trees is usually not huge).

At the end we iterate over the direct table, starting at both ends and stopping the iteration when the 2 iterators meet in the middle. The values of the left iterator must increase, the values of the right iterator must decrease, and the values of the 2 iterators must be equal.

2) Node:

info: TValue
left: ↑ Node
right: ↑ Node

Binary Tree:

root: ↑ Node

3) function isDiamond(bt) is:

// pre: bt ∈ BinaryTree

// post: true

if bt.root = NIL then

end-if isDiamond ← false // just an assumption, can be changed

maxLevel ← 0

init(q) // initialise the queue

init(bt, 1000) // initialise the direct table with 1000 positions

q.push(bt.root, 0)

while isEmpty(q) = false execute:

front ← q.pop()

if [front.first].left ≠ NIL then

q.push([front.first].left, front.second+1)

end-if

if [front.first].right \neq NIL then

2. push ([front.first].right, front.second+1)

end-if

alt [front.second] \leftarrow alt [front.second] + 1

if front.second > maxLevel then

maxLevel \leftarrow front.second

end-if

end-while

prev $\leftarrow -1$

i $\leftarrow 0$

j \leftarrow maxLevel

ok \leftarrow true

while i < j execute

if prev $\neq -1$ then

if alt[i] \leq alt[prev] then

ok \leftarrow false

i \leftarrow j+1 // to stop the loop

end-if

if alt[i] \neq alt[j] then

ok \leftarrow false

i \leftarrow j+1

end-if

end-if

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prev $\leftarrow i$

$i \leftarrow i + 1$

$j \leftarrow j - 1$

end-while

is Diamond $\leftarrow ok$

end-function

4) The complexity comes from the traversal of the tree (BFS) and the traversal of the direct table. Even though the second traversal has best/worst case, the first one doesn't and since the first one is $\Theta(n)$ and the second one is $\Theta(n)$ in worst-case, the complexity of the algorithm will be $\Theta(n)$ (without best/worst cases).