



IBM Research

# A Graph-based Framework for Multi-Task Multi-View Learning

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# Motivation

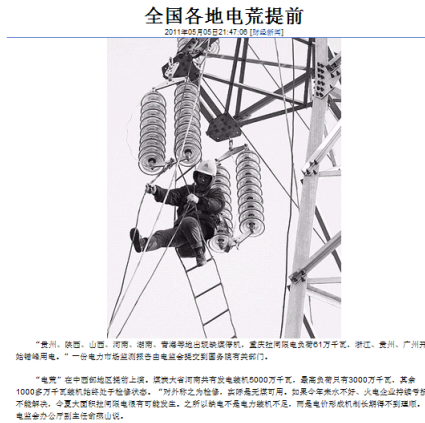
- Feature heterogeneity
  - A single task with features in multiple views
  - Multi-view learning
- Task heterogeneity
  - Multiple tasks related to each other in one way or another
  - Multi-task learning
- **Dual heterogeneity** in real applications
  - Feature heterogeneity & task heterogeneity
  - Shared views vs. task-specific views
  - ***Multi-Task Multi-View ( $M^2TV$ ) Learning***

# Main Contributions

- Problem definition
  - **$M^2TV$** : multiple related tasks with both shared and task-specific views
- Framework
  - **$GraM^2$** : a graph-based framework for  $M^2TV$
- Algorithm
  - **$IteM^2$** : an effective algorithm for solving  $GraM^2$

## Example 1: Image Classification

## Task 1: classification of images on Chinese web sites



Common view:  
image features  
e.g., color  
histogram

## Task 2: classification of images on English web sites



# Multi-task Multi-view Learning

## Chinese tokens

## English tokens

Task 1 specific view:  
TF-IDF representation  
of Chinese text content

Task 2 specific view:  
TF-IDF representation  
of English text content

## Example 2: Music Classification

## Task 1: classification of Chinese songs

## Task 2: classification of English songs

Common view:  
audio features  
e.g., pitch-class  
profile

ti: 爱的供养  
[ti: 爱核心主题曲]  
歌曲: 爱的供养  
歌手: 杨幂  
作词: 于正 作曲: 谭璇  
爱核心主题曲  
把你捧在手心虔诚地焚香  
洒下一段夜色将纶纶点亮  
不受落气回肠只为爱一场  
爱到最深处为了你笑得灿烂  
我愿尽一生一世来将你的目光  
只期盼你停住流转的时光  
请赐予我无限爱与被爱的力量  
让我能安心在幸福下安静的幻想  
music  
把你放在心上合起了手掌  
默默念去上指引我方向  
不求地久天长只求在身边  
爱着醉倒温柔乡轻轻低吟唱  
人世间有太多轻佻的欲望  
一回中头跌落你那时同样的模样  
回首发现早已踏出了红尘万丈

The wheels on the bus go round and round,  
round and round,  
round and round.  
The wheels on the bus go round and round,  
all through the town.

The wipers on the bus go Swish, swish, swish;  
Swish, swish, swish;  
Swish, swish, swish.  
The wipers on the bus go Swish, swish, swish,  
all through the town.

The horn on the bus goes Beep, beep, beep;  
Beep, beep, beep;  
Beep, beep, beep.  
The horn on the bus goes Beep, beep, beep,  
all through the town..

# Multi-task Multi-view Learning

## Chinese tokens

## English tokens

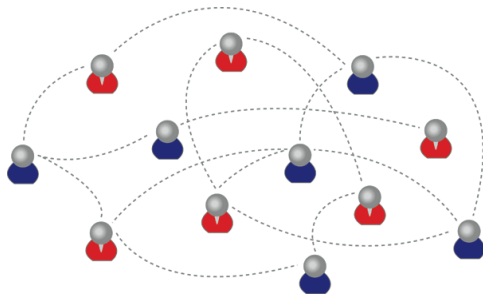
Task 1 specific view:  
TF-IDF representation  
of Chinese song lyric

Task 2 specific view:  
TF-IDF representation  
of English song lyric

# Example 3: Document Classification

## Task 1: classification of **Tweets**

Ben Tepfer: 8:14 PM Nov 14th via  
Twitter for iPhone from Eastside  
Syracuse  
URGENT: I just bit into a scone  
from @starbucks to find over 10  
staples baked into it. Please RT  
and be careful.



Task 1 specific view:  
social network for the  
Twitter user

Common view:  
TF-IDF  
representation

## Task 2: classification of **Conventional Documents**

RAISE your hand if you remember  
when Starbucks seemed cool.  
Anyone?  
Think back. To before the planet  
groaned with 17,000 Starbucks  
shops. Before the pumpkin spice  
lattes and the Ciao Amore CDs.

*e.g. NY Times*

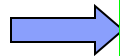
**Multi-task  
Multi-view  
Learning**



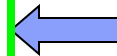
# Example 4: Watson Candidate-Answer Scoring

Task 1: scoring Chinese candidate answers

伊萨克 牛顿
威廉 坦普尔
帕拉姆
克里斯蒂安 惠更斯
哈雷彗星
爱德蒙 哈雷
粉红豹
彼得 塞勒斯



Common view:  
language-  
invariant  
features



Task 2: scoring English candidate answers

Isaac Newton
Wilhelm Tempel
HMS Paramour
Christiaan Huygens
Halley's Comet
Edmond Halley
Pink Panther
Peter Sellers



Chinese language-dependent features


Task 1 specific view

English language-dependent features


Task 2 specific view

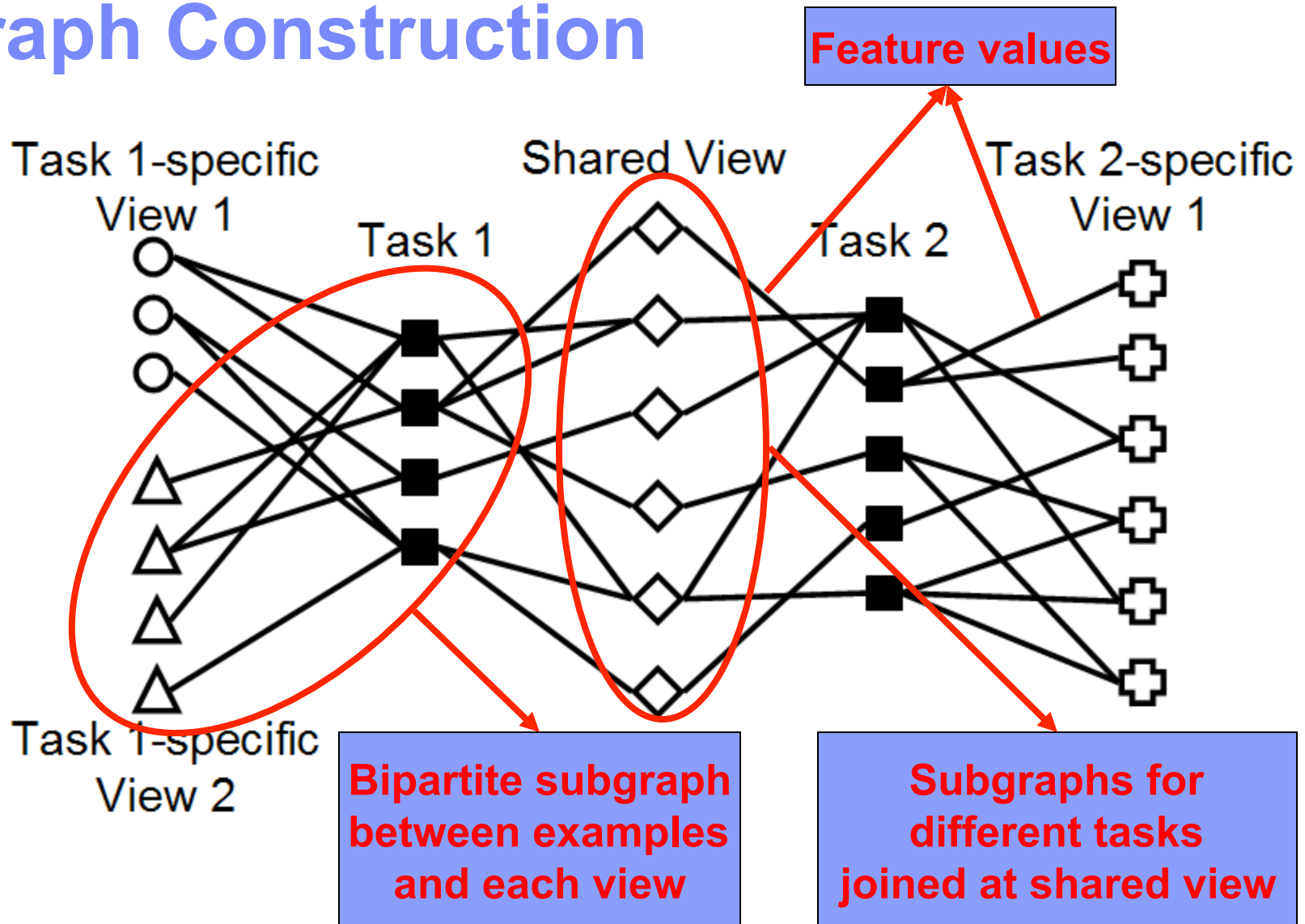
**Multi-task  
Multi-view  
Learning**

# Roadmap

- Motivation & examples
- *GraM<sup>2</sup>*: a graph-based framework
- *IteM<sup>2</sup>*: the proposed algorithm
- Experimental results
- Conclusion



# Graph Construction



# Objective Function

- Two types of functions
  - $g_i(\cdot)$ : functions defined on the examples
  - $f_{ik}(\cdot)$ : functions defined on the features
- Three types of constraints on the graph
  - Label consistency on the graph
    - Between  $g_i(\cdot)$  and  $f_{ik}(\cdot)$
  - Consistency with the label information
    - Between  $g_i(\cdot)$  and the known class labels
  - Similarity on the common views
    - Between  $f_{ik}(\cdot)$  of shared views for different tasks

# Interpretation of *GraM*<sup>2</sup>

$$Q(f, g) = \sum_{i=1}^T C_i + b \sum_{i=1}^T \sum_{j=1}^T \sum_{k \in S_{ij}} \|f_{ik} - f_{jk}\|^2$$

**Similarity  
on the  
common  
views**

$$C_i = \sum_{k=1}^{V_i} a_{ik} C_{ik} + \mu_i \|g_i - y_i\|^2$$

**Label consistency  
on the graph**

**Consistency with  
known label info**

$$h^* = [h_1^*, h_2^*]^T = \arg \min_{h \in \mathcal{H}} \|h\|_{\mathcal{H}}^2 + \sum_{i=1}^2 \mu_i \sum_{l=1}^{m_l} (h_i(x_{il}) - y_{il})^2$$

**Functions defined on BOTH  
examples and features**

# Roadmap

- Motivation & examples
- *GraM*<sup>2</sup>: a graph-based framework
- ***IteM*<sup>2</sup>: the proposed algorithm**
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# Basic Idea

- Iterative procedure for updating both  $g_i(\cdot)$  and  $f_{ik}(\cdot)$ 
  - Update  $f_{ik}(\cdot)$  for non-shared views
  - Update  $f_{ik}(\cdot)$  for shared views
  - Update  $g_i(\cdot)$  based on  $f_{ik}(\cdot)$  of all the views
- Assign class labels based on the sign of  $g_i(\cdot)$

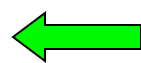
# Updating Shared Views

Indices of tasks sharing the  $k^{\text{th}}$  view with the  $i^{\text{th}}$  task

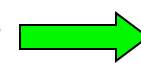
$$\frac{\partial Q(f, g)}{\partial f_{ik}} = 2a_{ik}f_{ik} - 2a_{ik}L_{ik}^T g_i + 4b \sum_{s \in I_{ik}} (f_{ik} - f_{sk})$$

Jointly update tasks sharing the  $k^{\text{th}}$  view

Each column of  $A_3$   
corresponds  $f_{ik}(\cdot)$   
of tasks sharing  
the  $k^{\text{th}}$  view



$$A_3 = A_2 A_1^{-1}$$



$$A_1^{-1} = \frac{1}{a^2 + 2rab}$$

$$\begin{bmatrix} a + 2b & 2b & \cdots & 2b \\ 2b & a + 2b & \cdots & \vdots \\ \vdots & \vdots & \ddots & 2b \\ 2b & \cdots & 2b & a + 2b \end{bmatrix}$$



$$d_k \times |I_k|$$

the  $i^{\text{th}}$  column set to  
 $a_{I_k(i)k} L_{I_k(i)k}^T g_{I_k(i)}$

# Properties of *IteM*<sup>2</sup>

- Optimality and convergence
  - Given sufficiently large number of iteration steps, *IteM*<sup>2</sup> will converge to the optimal solution of the objective function in *GraM*<sup>2</sup>
- Time complexity

$$- O(n_{iter} \left( \sum_{i=1}^T n_i \sum_{k=1}^{V_i} d_{ik} + d_S T^2 + V T^3 \right) + \sum_{i=1}^T n_i \log n_i)$$

Number of features  
in the  $k^{\text{th}}$  view of  
the  $i^{\text{th}}$  task

The total number  
of features in  
shared views

The total number  
of views



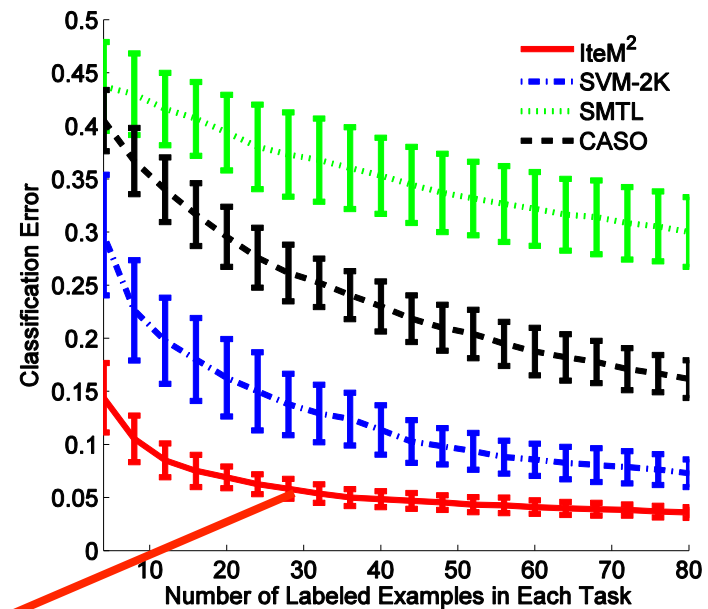
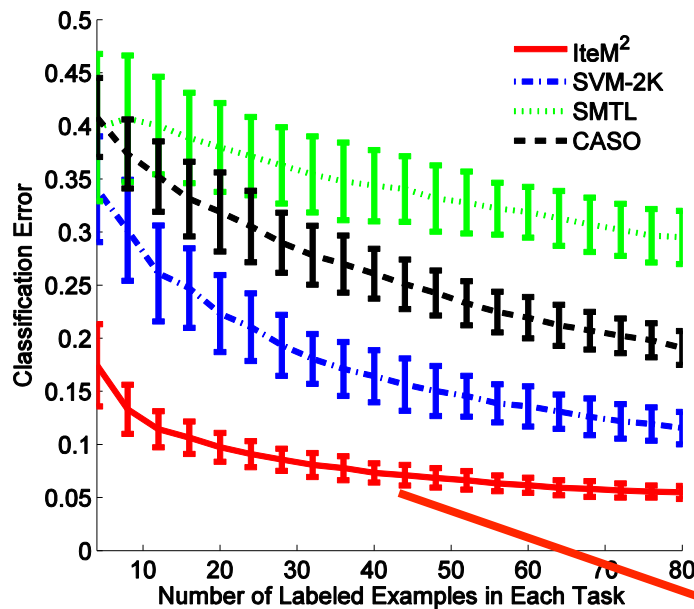
# Roadmap

- Motivation & examples
- *GraM*<sup>2</sup>: a graph-based framework
- *IteM*<sup>2</sup>: the proposed algorithm
- **Experimental results**
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# Two Tasks with Non-identical Views

- Data set: 20 newsgroups
- Common view: common vocabulary
- Task-specific view: task-specific vocabulary

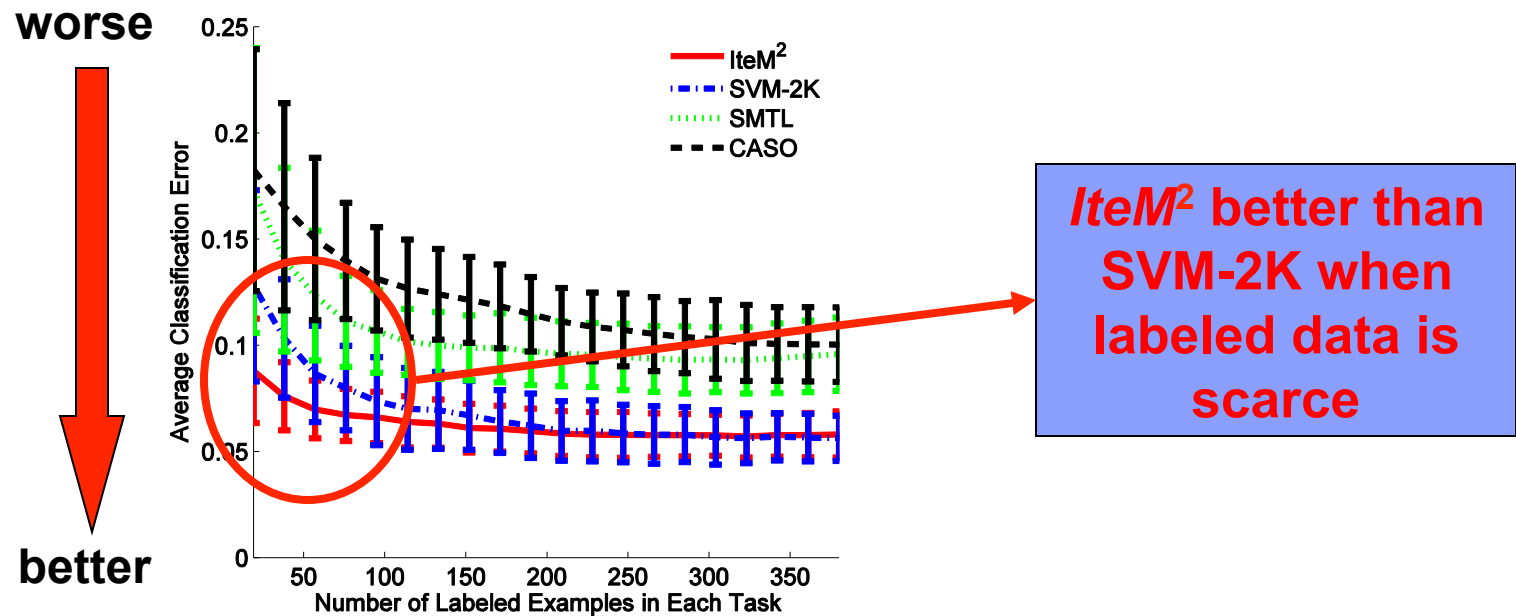
worse  
↓  
better



**Consistently better than competitors**

# Multiple Tasks with Identical Views

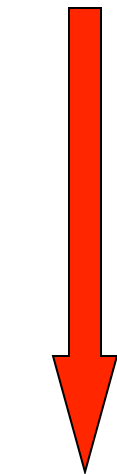
- Data set: WebKB data set
- Common views: words in the web page, anchor text, and title respectively



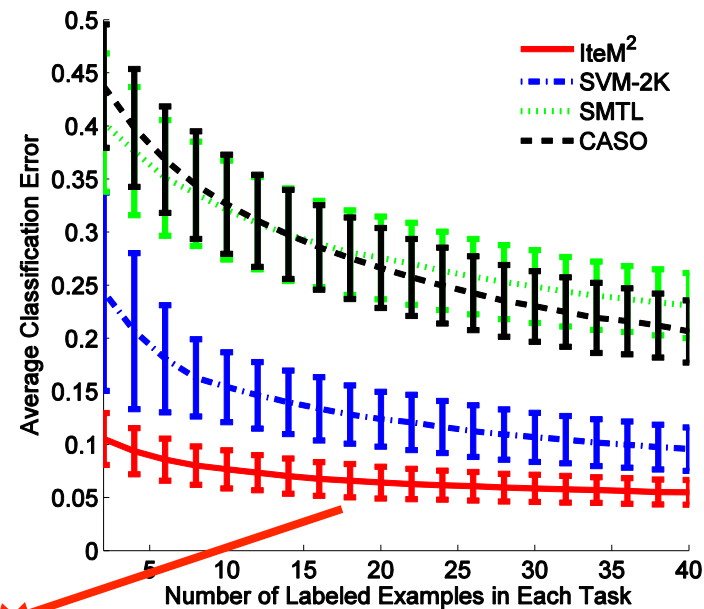
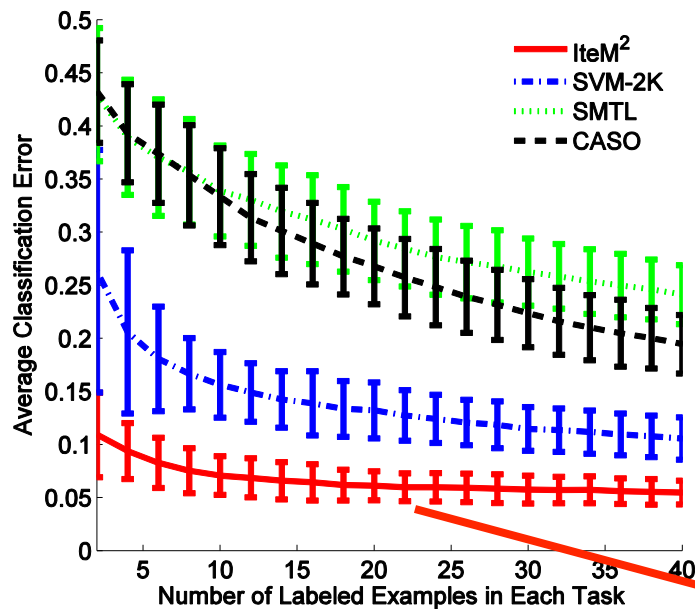
# Multiple Tasks and Non-identical Views

- Data set: ECML 2006 discovery challenge data set
- Common view: common vocabulary
- Task-specific view: task-specific vocabulary

worse



better



**Consistently better than competitors**

# Conclusion

- Multi-Task Multi-View ( $M^2TV$ ) Learning
  - Dual-heterogeneity: feature heterogeneity & task heterogeneity
- $GraM^2$ : a graph-based framework
  - Multi-partite graph capturing the relationship between examples and features
  - Objective function encodes similarity and consistency constraints
  - RKHS interpretation
- $IteM^2$ : an iterative procedure
  - Repeatedly update functions for examples and features