

HW 2: Solution for $2^{21} \bmod 18$

(4 points)

modexp (x, y, N)

if $y = 0$: return 1

$z = \text{modexp}(x, \text{floor}(y/2), N)$

if y is even: return $z^2 \bmod N$

else: return $x \cdot z^2 \bmod N$

x	y	y_{binary}	power of x	z	return value
2	21	1	x^1	16	$512 \bmod 18 = 8$
2	10	0	x^2	14	$196 \bmod 18 = 16$
2	5	1	x^4	4	$32 \bmod 18 = 14$
2	2	0	x^8	2	4
2	1	1	x^{16}	1	2
2	21		x^{21}		