CSC311 Project Final Report

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Part A

Q1 - KNN

1.(a)

Figure 1: Accuracy vs k for KNN Impute by User

1.(b)

Figure 2: Test accuracy with k*

1.(c)

The underlying assumption is that if question A is answered similarly by many students as question B, A's predicted response from specific students matches that of question B.


```
knn_impute_by_item:
Validation Accuracy: 0.607112616426757
Validation Accuracy: 0.6542478125882021
Validation Accuracy: 0.6826136042901496
Validation Accuracy: 0.6860005644933672
Validation Accuracy: 0.6922099915325995
Validation Accuracy: 0.69037538808919
```
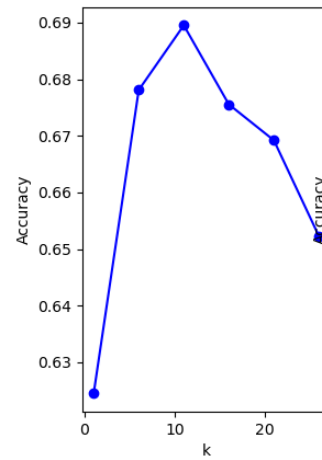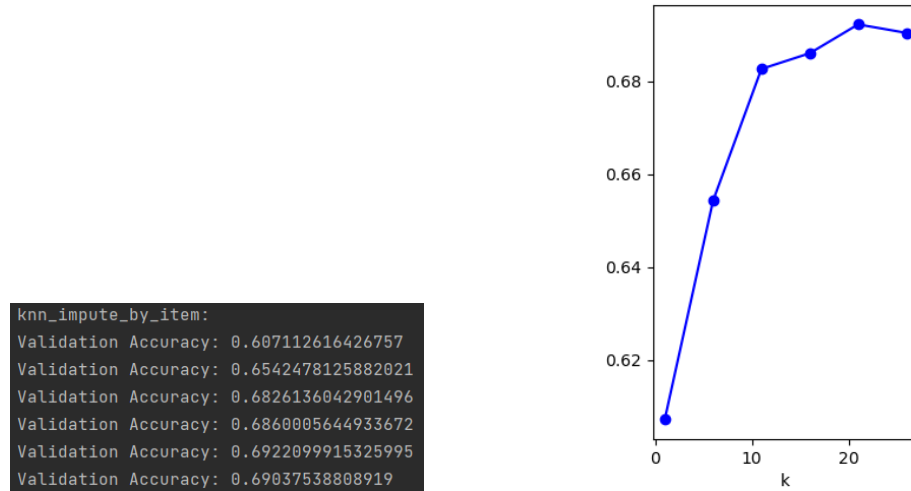
Figure 3: Accuracy vs k for KNN Impute by Item

```
Chosen argmax k*: 21 , Test accuracy: 0.6683601467682755
```

Figure 4: Test Accuracy with k*

1.(d)

The test accuracy for the user-based method (0.6842) is higher than that for the item-based method (0.6684). Therefore, the user-based collaborative filtering method performs better than the item-based collaborative filtering method in this case.

1.(e)

- Computationally expensive. KNN practically has no training process. With large datasets, as the number of students/questions grow, the time required to compute the distances and to identify the nearest neighbors at test time grows significantly.

- Curse of Dimensionality. When the sparse_matrix has too many missing values, it's hard to find good nearest neighbors, since most points will be about the same distances. This affects the prediction accuracy.

2

Q2 - IRT

2.(a)

$$p(c_{ij} = 1|\theta_i, \beta_j) = \frac{\exp(\theta_i - \beta_j)}{1 + \exp(\theta_i - \beta_j)} = \sigma(\theta_i - \beta_j)$$

log-likelihood:

$$\log p(C|\theta, \beta) = \sum_i \sum_j [c_{ij}(\theta_i - \beta_j) - \log(1 + \exp(\theta_i - \beta_j))]$$

The derivative of the log-likelihood with respect to θ_i:

$$\frac{\partial \log p(C|\theta, \beta)}{\partial \theta_i} = \sum_j [c_{ij} - \sigma(\theta_i - \beta_j)]$$

The derivative of the log-likelihood with respect to β_j:

$$\frac{\partial \log p(C|\theta, \beta)}{\partial \beta_j} = \sum_i [-c_{ij} + \sigma(\theta_i - \beta_j)]$$

2.(b)

```
# hyper-parameters
lr = 0.008
iterations = 100
```
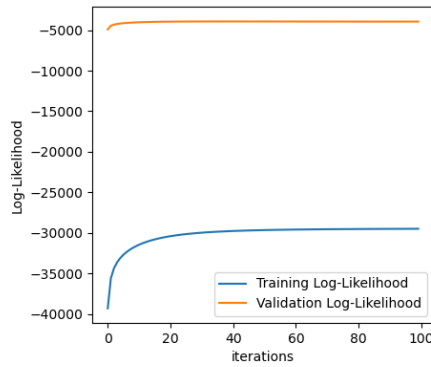
Figure 5: Hyper-Parameters

Figure 6: Training and Validation Log-Likelihoods vs Iteration

2.(c)

Validation Accuracy: 0.705193338978267
Test Accuracy: 0.7070279424216765

Figure 7: Final Validation & Test Accuracy

2.(d)

The three curves are all in S shape, as the sigmoid function. They represent the probability of correct responses as a function of student ability θ.
It shows that students with a high ability have a high probability of answering correctly.
Also, question with a high difficulty is skewed to the right, meaning it has a lower probability of being answered correctly.
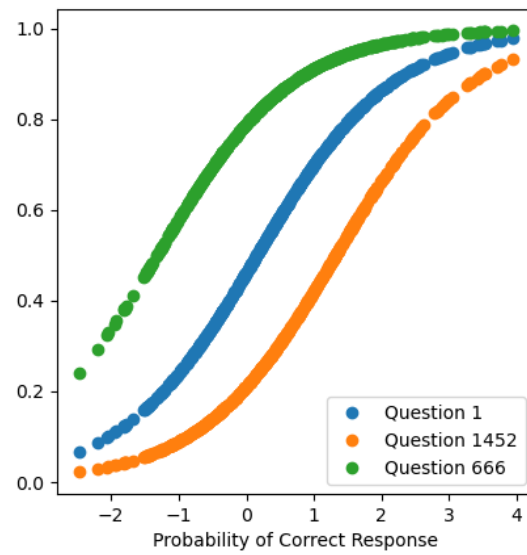
Figure 8: Probability of Correct Response vs Theta

4

Q3 - (i) Option 1: Matrix Factorization

3(i).(a)

```
Chosen argmax k*: 9
Validation accuracy: 0.6613039796782387
Test accuracy: 0.6587637595258256
```

Figure 9: SVD: Final Validation & Test Performance with chosen k

3(i).(b)

Filling the missing values with averages or zeros does not accurately reflect the data's underlying structure. There will be loss or distorsion of information.

3(i).(c)(d)(e)

```
Chosen argmax k*: 2,
Validation Accuracy: 0.6840248377081569
Test Accuracy: 0.6768275472763196
```

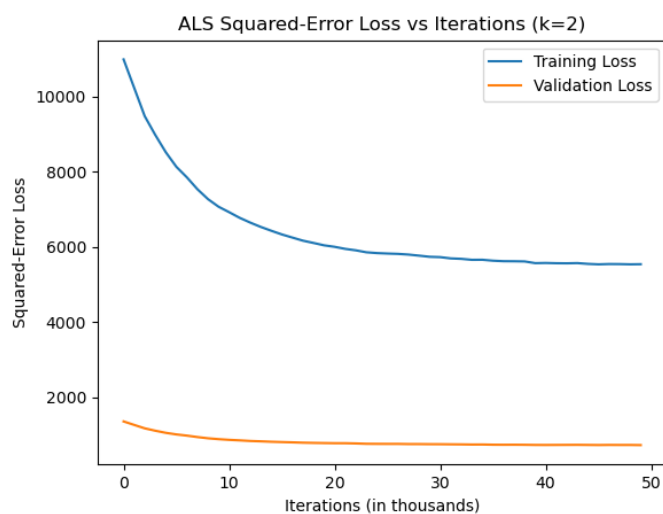Figure 10: ALS: Final Validation & Test Performance with chosen k

Figure 11: ALS: Squared-Error Loss vs Iterations

Q4 - Ensemble

Ensemble Process:

1. For each separate model, create different subsets of the training data of the same size of the original training data by sampling with replacement.

2. Train KNN, IRT, ALS. Report validation accuracy of each model. Use the models to generate predictions for validation and test data.

3. Using the three sets of predictions, calculate the mean of predictions.

4. Evaluate the ensembled prediction for final ensembled validation and test accuracy.

The ensemble does achieve better performance than individual models based on the final accuracy results. Because ensemble approach reduces the variance by combining the three models, which improved generalization.

```
KNN: Validation Accuracy: 0.6524132091447925
IRT: Validation Accuracy: 0.6971493084956252
ALS: Validation Accuracy: 0.6686423934518769
Final Ensembled Results:
Validation Accuracy: 0.69037538808919
Test Accuracy: 0.7011007620660458
```

Figure 12: Individual Model & Final Ensemble Accuracies

Part B