

REPRESENTATION OF DATA

Frequency distribution table:

x	1	2	3	4	5
f	4	7	2	9	4

$$\text{Mean: } \bar{x} = \frac{\sum fx}{\sum f} = \frac{(4 \times 1) + (7 \times 2) + (2 \times 3) + (9 \times 4) + (4 \times 5)}{26} = 3.08$$

Median: Make the cumulative frequency table

x	1	2	3	4	5
f	4	7	2	9	4
cf	4	11	13	22	26

$$\begin{aligned}\text{Median} &= \frac{1}{2}(n+1) = \frac{1}{2}(26+1) = \frac{27}{2} = 13.5^{\text{th}} \text{ observation} \\ &= 3.5\end{aligned}$$

Mode: Most frequently occurring value

$$= 4$$

$$\text{Variance: } \frac{\sum fx^2}{\sum f} - (\bar{x})^2 \quad \text{or} \quad \frac{\sum (x - \bar{x})^2}{n} \quad \text{or} \quad \frac{\sum x^2}{n} - (\bar{x})^2$$

$$\sigma^2 = \frac{(4 \times 1) + (7 \times 4) + (2 \times 9) + (9 \times 16) + (4 \times 25)}{26} = 1.82$$

$$\begin{aligned}\text{Standard Deviation} &= \sigma = \sqrt{\sigma^2} \\ &= \sqrt{1.82} \\ \sigma &= 1.35\end{aligned}$$

CONTINUOUS TABLE (FREQUENCY DISTRIBUTION TABLE)

time (t min)	$0 < t \leq 15$	$15 < t \leq 30$	$30 < t \leq 60$	$60 < t \leq 90$	$90 < t \leq 120$
no. of meetings	4	7	24	38	7
midpoints	7.5	22.5	45	75	105

$$\text{Mean : } \bar{x} = \frac{\sum fx}{\sum f} = \frac{(4 \times 7.5) + (7 \times 22.5) + (24 \times 45) + (38 \times 75) + (7 \times 105)}{80}$$

$$= 60.7$$

$$\text{Variance : } \frac{\sum fx^2}{\sum f} - (\bar{x})^2 = \sigma^2$$

$$\text{Standard Deviation : } \sqrt{\sigma^2}$$

Mode : Highest frequency density $\rightarrow \frac{\text{frequency}}{\text{class width}}$, i.e. $\frac{4}{15}$ for the first class
 ↳ the class with the highest frequency density is the modal class

$$\text{Median : } \text{Lower class boundary} + \left(\frac{\frac{n}{2} + \text{Cumulative frequency}}{\text{Frequency}} \right) \times \text{class width}$$