

10.1.1

$$x = (4, 3)$$

a)  $1 \times 2$  dimensions

$$b) \quad 5x = 5 \cdot 4 = 20, \quad 5 \cdot 3 = 15 \quad \begin{matrix} 5x = \\ (20, 15) \end{matrix}$$

$$c) \quad 3x = 3 \cdot 4 = 12, \quad 3 \cdot 3 = 9 \quad \begin{matrix} 3x = \\ (12, 9) \end{matrix}$$

$$d) \quad 5x + 3x = (20, 15) + (12, 9) = (32, 24)$$

$$e) \quad 8x = 5x + 3x = (32, 24)$$

$$f) \quad 4x - x = 3x = (12, 9)$$

$$g) \quad x^T \quad x = (4, 3) \quad x^T = \begin{pmatrix} 4 \\ 3 \end{pmatrix} \quad \text{new dimension } 2 \times 1$$

h)  $x + x^T$  are not definable, because they have different dimensions ( $1 \times 2, 2 \times 1$ ).

$$i) \quad \|x\| = \sqrt{x_1^2 + x_2^2} = \sqrt{4^2 + 3^2} = \sqrt{16 + 9} = \sqrt{25} = 5$$

10.1.2

a)  $4 \times 1$  dimensions

$$v = \begin{pmatrix} 3 \\ 7 \\ 0 \\ 11 \end{pmatrix}$$

$$b) \quad 2v = 2 \cdot \begin{pmatrix} 3 \\ 7 \\ 0 \\ 11 \end{pmatrix} = \begin{pmatrix} 6 \\ 14 \\ 0 \\ 22 \end{pmatrix}$$

$$c) \quad 5v + 2v = 5 \cdot \begin{pmatrix} 3 \\ 7 \\ 0 \\ 11 \end{pmatrix} = \begin{pmatrix} 15 \\ 35 \\ 0 \\ 55 \end{pmatrix} + \begin{pmatrix} 6 \\ 14 \\ 0 \\ 22 \end{pmatrix} = \begin{pmatrix} 21 \\ 49 \\ 0 \\ 77 \end{pmatrix}$$